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Présenté par : GRAIRIA Saad

Encadrant : Mr ATHMANi Allaeddine MC-A Université BADJI MOKHTAR-ANNABA

Jury de Soutenance :

DJEGHABA Kamel	Professeur	Badji Mokhtar-Annaba	Président
ATHMANI Allaeddine	MC-A	Badji Mokhtar-Annaba	Encadrant
MEZIGHECHE Nawel	MA-A	Université	Examinateur

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DEDICATION



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ABSTRACT

Unreinforced masonry buildings (URM) in Annaba, Algeria, face significant seismic vulnerability due to their construction before the implementation of seismic codes. This study focuses on evaluating the seismic vulnerability of URM structures by selecting a prototype made of stones from Old Annaba. Using the macro-element approach and 3D modelling in the software 3Muri©, the prototype's behaviour under seismic loads is analysed considering bending, shearing, and diagonal traction.

The research compares the test results of the unreinforced masonry building with a reinforced counterpart to assess the extent of damages and the effectiveness of reinforcement strategies. Fragility curves with a log-normal distribution are developed, incorporating displacement-based damage data from the modelling. These curves aid in understanding the seismic vulnerability of URM structures and guide retrofitting efforts and seismic design guidelines.

This study contributes to the knowledge of URM buildings' seismic behaviour in Annaba, supporting the assessment and enhancement of their resilience. The findings inform the preservation and rehabilitation of historic URM structures, ensuring their safety and sustainability in earthquake-prone regions.

Keywords: unreinforced masonry, seismic vulnerability, Annaba, macro-element approach, 3D modelling, seismic behaviour, fragility curves, displacement-based damage, retrofitting, seismic design, historic buildings, preservation, rehabilitation.

RESUMÉ

Les bâtiments en maçonnerie non armée (URM) à Annaba, en Algérie, sont confrontés à une vulnérabilité sismique importante en raison de leur construction avant la mise en œuvre des codes sismiques. Cette étude porte sur l'évaluation de la vulnérabilité sismique des structures de l'URM en sélectionnant un prototype en pierres du Vieux Annaba. A l'aide de l'approche macro-éléments et de la modélisation 3D dans le logiciel 3Muri©, le comportement du prototype sous charges sismiques est analysé en tenant compte de la flexion, du cisaillement et de la traction diagonale.

La recherche compare les résultats des tests du bâtiment en maçonnerie non renforcée avec un bâtiment de contrepartie renforcée pour évaluer l'étendue des dommages et l'efficacité des stratégies de renforcement. Des courbes de fragilité avec une distribution log-normale sont développées, incorporant des données de dommages basées sur le déplacement issues de la modélisation. Ces

courbes aident à comprendre la vulnérabilité sismique des structures URM et guident les efforts de modernisation et les directives de conception sismique.

Cette étude contribue à la connaissance du comportement sismique des bâtiments de l'URM à Annaba, soutenant l'évaluation et l'amélioration de leur résilience. Les résultats éclairent la préservation et la réhabilitation des structures historiques de l'URM, garantissant leur sécurité et leur durabilité dans les régions sujettes aux tremblements de terre.

Mots clés : maçonnerie non armée, vulnérabilité sismique, Annaba, approche macroélémentaire, modélisation 3D, comportement sismique, courbes de fragilité, endommagement par déplacement, réhabilitation, conception parasismique, bâtiments historiques, préservation, réhabilitation.

خلاصة

تواجه مباني البناء غير المدعمة (URM) في عنابة ، الجزائر ، ضعفًا زلزاليًا كبيرًا بسبب بنائها قبل تطبيق الرموز الزلزالية. تركز هذه الدراسة على تقييم الضعف الزلزالي لهياكل URM من خلال اختيار نموذج أولي مصنوع من الحجارة من عنابة القديمة. باستخدام نهج العناصر الكلية والنمذجة ثلاثية الأبعاد في برنامج 3 © Muri، يتم تحليل سلوك النموذج الأولي تحت الأحمال الزلزالية مع الأخذ في الاعتبار الانحناء والقص والجر القطر.

يقارن البحث نتائج الاختبار لمبنى البناء غير المدعم بنظير مقوى لتقييم مدى الأضرار وفعالية استراتيجيات التعزيز. تم تطوير منحنيات الهشاشة مع التوزيع اللوغاريتمي الطبيعي ، بدمج بيانات الضرر القائم على الإزاحة من النمذجة. تساعد هذه المنحنيات في فهم الضعف الزلزالي لهياكل URM وتوجيه جهود التعديل التحديثي وإرشادات التصميم الزلزالي.

تساهم هذه الدراسة في معرفة السلوك الزلزالي لمباني URM في عنابة ، ودعم تقييم وتعزيز مرونتها. تشير النتائج إلى الحفاظ على هياكل URM التاريخية وإعادة تأهيلها ، مما يضمن سلامتها واستدامتها في المناطق المعرضة للزلازل.

الكلمات المفتاحية: البناء غير المدعم ، الضعف الزلزالي ، عنابة ، نهج العنصر الكلي ، النمذجة ثلاثية الأبعاد ، السلوك الزلزالي ، منحنيات الهشاشة ، الضرر الناجم عن الإزاحة ، التعديل التحديثي ، التصميم الزلزالي ، المباني التاريخية ، الحفظ ، إعادة التأهيل.

TABLE OF CONTENTS

GENERAL INTRODUCTION	1
CHAPTER I REVUE ON HISTORICAL MASONRY BUILDINGS	3
I.1 Introduction	4
I.2 Material properties of masonry	4
I.2.1 The units	4
I.2.2 The mortar	11
I.3 Assembly of mortar and masonry	16
I.3.1 External mechanical deterioration	16
I.3.2 Internal mechanical deterioration	16
I.3.3 Chemical deterioration	17
I.3.4 Biodeterioration	17
I.4 Estimation of the mechanical properties of masonry	17
I.4.1 The Italian code NTC 18	17
I.5 Masonry building behaviours	21
I.5.1 Domain of vulnerability modelling	21
I.5.2 The seismic behaviour mechanisms	21
I.6 Seismic analysis ''pushover''	23
I.6.1 Why is pushover analysis used?	24
I.6.2 A brief overview of the technique:	24
I.7 The strengthening	33
I.7.1 Surface treatment	33
I.7.2 External reinforcement	35
I.8 Conclusion	40
CHAPTER II TREMURI MODELLING	41
II.1 Introduction:	42
II.2 Macro-element modelling:	
II.2.1 Macro-element approach:	
II.2.2 Equivalent frame	
II.2.3 Structural element behaviour	
II.2.4 The structure's three-dimensional assembly	47
II.3 Modelling masonry piers and spandrels	
II.4 Strength and failure criteria for urm panels implemented in tremuri program	
II.4.1 The failure modes	
II.4.1.1 Bending ultimate moment	
II 4.1.2 Shoon transvels and as versio suitonic	51

II.4.2	.2 Strength criteria	52
II.5	Wall modelling	55
II.6	Spatial modelling	57
II.7	The structure after modelling	61
II.8	Conclusion	
CHAPTEI	ER III CASE STUDY	63
III.1	Introduction	6/
III.2	Study case	
III.2	•	
III.2.	• •	
	•	
III.2.	•	
III.3	Study case and diagnosis	
III.3.		
III.4	Reference codes	
III.5	Actions	77
III.5.	5.1 Description of actions	77
III.5.	5.2 Permanent and variable loads	77
III.5.	5.3 General evaluation of the actions	78
III.6	The loads	79
III.7	The mechanical characteristics	80
III.7.	7.1 Masonry	80
III.7.	7.2 Timber	80
III.7.	7.3 Steel	81
III.7.	7.4 Floors	81
III.7.		
	Conclusion	
CHAPTE	ER IV STATIC VERIFICATION	83
IV.1	Introduction	
IV.2	Reference code	
IV.3 IV.3	analysis method	
IV.3	Model description	
IV.4	-	
IV	V.4.1.1 Mechanical behaviour of the masonry	86
IV	V.4.1.2 Wall with shear mechanism	87
IV	V.4.1.3 Wall with bending mechanism	88
IV	V.4.1.4 In the absence of residual resistance	89
IV.5	Loads	89
IV.5	5.1 Seismic load:	89
IV.5		
IV.6	Global static verification	90

IV.6.1	Slenderness of the masonry	
IV.6.2 IV.6.3	Load eccentricity	
IV.6.4	the results	
IV.6	.4.1 Wall: 1	86
IV.6	.4.2 Wall: 3	86
IV.6	.4.3 Wall: 6	88
IV.6	.4.4 Wall: 7	89
IV.6	.4.5 Wall: 8	90
IV.6	.4.6 Wall: 9	92
IV.6	.4.7 Wall: 10	92
	inds	
	onclusion	
CHAPTE V	SEISMIC PERFORMANCE ANALYSIS	96
V.1 Ir	ntroduction	97
V.2 Se	eismic spectrum assessment	97
V.2.1	Site selection	98
V.2.2	Reconnaissance and soil studies	98
V.2.3	Modelling and calculation methods	98
V.2.4	Seismic zone classification	98
V.2.5	Classification Of Works According to Their Importance	99
V.2.6	Site classification	100
V.2.7	Calculation response Spectrum	100
V.2.8	Observance of Algerian seismic regulations	102
V.3 P	ushover analysis description	104
V.4 D	ata validation	105
V.4.1	Domain resistance calculation	105
V.5 R	esults	109
V.5.1	Result details	110
V.5.2	Results legend	111
V.5.3	Seismic analysis no. 4 Direction X	112
V.5.4	Seismic analysis no. 5 Direction Y	119
V.6 A	ssessment of the performance point (x direction)	123
V.6.1	Graphical ''using excel table'':	123
V.6.2	Numerical:	125
V.6.3	Finds	126
V.7 A	ssessment of the performance point (Y direction)	126
V.7.1	Graphical ''using excel table''	126
V.7.2	Numerical	128
V.7.3	Finds:	129
V.8 V	ulnirability analysis:	129

V.8.	1 Fragility and vulnerability functions	129
V.8.	1 Finds	134
V.9	Conclusion	134
СНАРТЕ	R VI REINFORCEMEN ANALYSIS	136
VI.1	Introduction	137
VI.2	Types of reinforcement used	138
VI.2	.1 Wall frames	138
VI.2	.2 Frcm systems	138
VI.3	Reinforcement type characteristics	139
VI.3	.1 Reinforcements frcm (walls)	139
VI.3	.2 Reinforcements wall (Steel frames)	140
VI.3	.3 Reinforcements horizontal elements (Steel frame "tie rod ")	140
VI.4	Masonry with FRCM reinforcement	141
VI.4	.1 Compression bending	141
VI.4	.2 Shear	142
VI.5	Static reinforcement verifications	143
VI.5	.1 Wall: 1	143
VI.5	.2 Wall: 6	144
VI.5	.3 Wall: 7	146
VI.5	.4 Wall: 10	148
VI.6	Seismic vulnerability analysis	149
VI.6	.1 Results	150
VI.7	Assessment of the performance point (x direction)	162
VI.7	.1 Graphical ''using excel table''	162
VI.7	.2 Numerical	162
VI.8	Assessment of the performance point (Y direction)	163
VI.8	.1 Graphical ''using excel table''	163
VI.8	.2 Numerical	163
VI.9	Vulnerability analysis	164
VI.9	.1 Analytical functions for fragility curve	164
V.1.	1 Damage distribution of the studied structure	165
VI.9	-	
VI.10	Conclusion	
GENE	RAL CONCLUSION	168

LIST OF FIGURES

FIGURE I 1 DIFFERENT TYPES OF MORTAR AND THEIR CLASSIFICATIONS "1"	12
FIGURE I 2. DIFFERENT TYPES OF MORTAR AND THEIR CLASSIFICATIONS "2"	13
FIGURE I 3. MASONRY CONSTRUCTION COMPONENTS	15
FIGURE I 4. DIFFERENT SHEAR MODES OF URM WALL	22
FIGURE I 5. IN-PLANE AND OUT-OF-PLANE FORCES	23
FIGURE I 6. STRUCTURE CAPACITY CURVE	24
FIGURE I 7. GLOBAL RESPONSE AND PERFORMANCE	25
FIGURE I 8. DEVELOPMENT OF THE CAPACITY CURVE	26
FIGURE I 9. THE DIFFERENT METHODS UTILIZED TO DISTINGUISH THE PERFORMANCE POINT	27
FIGURE I 10 CONVERSION TO ADRS SPECTRA (ATC 40)	28
FIGURE I 11 SCHEMATIC REPRESENTATION OF CAPACITY SPECTRUM METHOD (ATC 40)	29
FIGURE I 12.DETERMINATION OF HYSTERETIC	30
FIGURE I 13. REDUCTION OF DEMAND SPECTRUM	31
FIGURE I 14 INTERSECTION POINT OF DEMAND AND CAPACITY SPECTRUMS WITHIN ACCEPTABLE TO	LERANCE
(ATC 40)	32
FIGURE I 15 THE CONCEPT FOR A "SAWTOOTH" CAPACITY SPECTRUM (ATC 40)	32
FIGURE I 16 STRENGTHENING OF MASONRY WALLS BY APPLICATION OF SINGLE AND DOUBLE SIDED	
REINFORCED CONCRETE (RC) JACKETS	34
FIGURE I 17 STRENGTHENING OF MASONRY WALLS USING FRP STRUCTURAL REPOINTING	34
FIGURE I 18 FABRIC REINFORCED CEMENTITIOUS MATRIX (FRMC)	35
FIGURE I 19. POST-TENSIONING STRENGTHENING SYSTEM	
FIGURE I 20. STEEL RING-FRAME STRENGTHENING TECHNIQUE	37
FIGURE I 21. THE REINFORCED CORE TECHNIQUE	38
FIGURE I 22. TIE BARS MADE OF IRON TENSION MEMBERS	38
FIGURE I 23. THE RETROFITTING TECHNIQUES	39
FIGURE II 1. MEF AND THE EFM	43
FIGURE II 2. SHEMA OF MACROELEMENTS TAKEN FROM LAGOMARSINO ET AL (2008B)	44
FIGURE II 3. STRUCTURE EQUIVALENT FRAME IDENTIFICATION	45
FIGURE II 4. ILLUSTRATION OF EFFECTIVE HEIGHT IDENTIFICATION METHOD TAKEN FROM DOLCE (1	.991) 45
FIGURE II 5. IDENTIFICATION OF FAILURE MODES FOR A MICROELEMENT TAKEN FROM (SERGIO LAG	OMARSINO,
2013)	47
FIGURE II 6. 3D ASSEMBLING OF MASONRY WALLS: CLASSIfiCATION OF 3D AND 2D RIGID NODES AN	D OUT-OF-
PLANE MASS SHARING. (SERGIO LAGOMARSINO, 2013)	48
FIGURE II 7. ELEMENT BEHAVIOUR CURVE	49
FIGURE II 8.DIFFERENT TYPES OF FAILURES (RAFFAELLO, 2012)	50

FIGURE II 9.STRENGTH CRITERION IN BENDING-ROCKING	51
FIGURE II 10. TURNŠEK AND CAČOVIC SHEAR STRENGTH AND STRENGTH CRITERIA COMPARISON	52
FIGURE II 11. THE DIVISIONS OF WALL FRAME	55
FIGURE II 12. WALL MODEL NODES AND THE ECCENTRICITIES	56
FIGURE II 13. COMPONENTS DISPLACEMENTS ACCORDING TO DOF	58
FIGURE II 14. THE FORCES TRANSMITTED BY THE MACRO-ELEMENTS	59
FIGURE II 15. THE REFERENCE ELEMENT	60
FIGURE II 16 3D VIEW OF THE BUILDING AFTER MODELLING AND THE MACROELEMENTS STRUCTURE	MECH 61
FIGURE III 1. MAIN FACADE	65
FIGURE III 2 MASS GROUNDING PLAN	66
FIGURE III 3 SITUATION PLAN	66
FIGURE III 4 GROUND FLOOR PLAN AND BLOCKS DIVISIONS	69
FIGURE III 5 ARCHITECTURAL PLAN CUT AA'	70
FIGURE III 6 ARCHITECTURAL PLAN CUT BB'	70
FIGURE III 7 ARCHITECTURAL PLAN CUT CC'	71
FIGURE III 8 MATERIALS AND ARCHITECTURE PLAN FIRST FLOOR	73
FIGURE III 9 MATERIAL PLAN 1ST FLOOR AND 2ND FLOOR	73
FIGURE III 10.RDC SURVEY PLAN	74
FIGURE III 11 1ST FLOOR PLAN VIEW	75
FIGURE III 12 ROOF PLAN VIEW	76
FIGURE III 13 FLOOR CONCEPT	81
FIGURE IV 1 3D VIEW OF THE STRUCTURE MODEL	84
FIGURE IV 2 WALL BEHAVIOUR CURVE V	VITH SHEAR
MECHANISM	87
FIGURE IV 3 WALL BEHAVIOUR CURVE WITH BENDING MECHANISM	88
FIGURE IV 4 WALL BEHAVIOUR CURVE IN CASE OF ABSENCE OF RESIDENTIAL RESISTANCE	89
FIGURE IV 5 THE STRUCTURE WALLS NUMBERS	92
FIGURE IV 6 WALL 1 ELEMENT VERIFICATION	86
FIGURE IV 7 WALL 3 ELEMENT VERIFICATION	86
FIGURE IV 8 WALL 6 ELEMENT VERIFICATION	88
FIGURE IV 9 WALL 7 ELEMENT VERIFICATION	89
FIGURE IV 10 WALL 8 ELEMENT VERIFICATION	90
FIGURE IV 11 WALL 9 ELEMENT VERIFICATION	92
FIGURE IV 12 WALL 10 ELEMENT VERIFICATION	92
FIGURE V 1 RISK RSSESSMENT FORMWORK	97
FIGURE V 2 THE ELASTIC RESPONSE SPECTRUM FOR A= 0.2	103
FIGURE V 3 WALL 10 DEFORMATIONS RESULT FOR X DIRECTION	112
FIGURE V 4 WALL 10 RESISTANCE DOMAIN DIAGRAM	114

IGURE V 5 WALL 7 DEFORMATIONS RESULT FOR X DIRECTION	114
GURE V 6 WALL 7 RESISTANCE DOMAIN DIAGRAM	117
GURE V 7 PLAN DEFORMED SHAPE FOR X DIRECTION	118
IGURE V 8 PUSHOVER CURVES FOR X DIRECTION	118
IGURE V 9 WALL 8 RESISTANCE DOMAIN DIAGRAM	119
GURE V 10 WALL 8 RESISTANCE DOMAIN DIAGRAM	121
IGURE V 11 PLAN DEFORMED SHAPE Y DIRECTION	122
IGURE V 12 PUSHOVER CURVES Y DIRECTION	122
IGURE V 13 MDOF CAPACITY CURVE FOR X DIRECTION	123
IGURE V 14 SDOF CAPACITY CURVE FOR X DIRECTION	124
IGURE V 15 BI-LINEAR EQUIVALENT CAPACITY CURVE X DIRECTION	124
IGURE V 16 INTERSECTION OF THE CAPACITY CURVE AND THE DEMAND X DIRECTION	125
IGURE V 17 MDOF CAPACITY CURVE Y DIRECTION	127
IGURE V 18 SDOF CAPACITY CURVE Y DIRECTION	12
IGURE V 19 BI-LINEAR EQUIVALENT CAPACITY CURVE Y DIRECTION	12
IGURE V 20 INTERSECTION OF THE CAPACITY CURVE AND THE DEMAND Y DIRECTION	128
IGURE V 21 FRAGILITY CURVES STAGES	130
IGURE V 22 FRAGILITY CURVE (X DIRECTION)	132
IGURE V 23 FRAGILITY CURVE (Y DIRECTION)	132
IGURE V 24 DAMAGE HISTOGRAM (X DIRECTION)	133
IGURE V 25 VULNERABILITY HISTOGRAM (Y DIRECTION)	134
IGURE VI 1 3D VIEW AFTER REINFORCEMENT	137
IGURE VI 2 WALL 10 RESISTANCE DOMAIN DIAGRAM AFTER REINFORCEMENT	153
IGURE VI 3 WALL 7 RESISTANCE DOMAIN DIAGRAM AFTER REINFORCEMENT	156
IGURE VI 4 PLAN DEFORMED SHAPE FOR X DIRECTION AFTER REINFORCEMENT	157
IGURE VI 5 PUSHOVER CURVES FOR X DIRECTION BEFORE AND AFTER REINFORCEMENT	157
IGURE VI 6 WALL 8 RESISTANCE DOMAIN DIAGRAM	160
IGURE VI 7 PLAN DEFORMED SHAPE FOR Y DIRECTION AFTER REINFORCEMENT	162
IGURE VI 8 PUSHOVER CURVES FOR Y DIRECTION BEFORE AND AFTER REINFORCEMENT	162
IGURE VI 9 INTERSECTION OF THE CAPACITY CURVE AND THE DEMAND X DIRECTION AFTER REINF	FORCEMENT
	162
IGURE VI 10 INTERSECTION OF THE CAPACITY CURVE AND THE DEMAND Y DIRECTION AFTER REIN	NFORCEMENT
	163
IGURE VI 11 FRAGILITY CURVE FOR X DIRECTION AFTER REINFORCEMENT	164
IGURE VI 12 FRAGILITY CURVE FOR Y DIRECTION AFTER REINFORCEMENT	164
IGURE VI 13 DAMAGE HISTOGRAM AFTER REINFORCEMENT (X DIRECTION)	165
IGURE VI 14 DAMAGE HISTOGRAM AFTER REINFORCEMENT (Y DIRECTION)	16!

LIST OF TABLES

Table I 1. Types of Masonry Units (Masonry-Roof - Floor Construction, 2020)	5
TABLE I 2. REFERENCE RANGES FOR DIFFERENT MASONRY MATERIAL PARAMETERS (SEBOUI HATEM, 2022)	18
TABLE I 3. CORRECTION FACTORS FOR DIFFERENT PARAMETERS OF MASONRY TYPES (SEBOUI HATEM, 2022)	19
TABLE I 4. KNOWLEDGE LEVELS ARE BASED ON AVAILABLE INFORMATION AND CORRESPONDING VALUES OF	F THE
CONFIDENCE FACTORSFOR MASONRY BUILDINGS (SEBOUI HATEM, 2022)	19
TABLE II 1. STRENGTH CRITERIA FOR URM PANELS IMPLEMENTED IN TREMURI PROGRAM (SERGIO LAGOMARSII	NO,
2013)	52
TABLE II 2. THE MECHANICAL CHARACTERISTICS OF STEEL FRAMES IMPLEMENTED IN TREMURI PROGRAM	54
TABLE II 3. THE MECHANICAL CHARACTERISTICS OF WALL PANEL IMPLEMENTED IN TREMURI PROGRAM	54
TABLE III 1 BUILDING BLOCK DIVISIONS	67
TABLE III 2 . DIVISIONS DIMENSIONS AND OPENINGS	68
TABLE III 3. THE STRUCTURE ELEMENTS	72
TABLE III 4. THE USED MATERIAL TABLES	74
TABLE III 5 . SOME MATERIALS PROPRE WEIGHTS	78
Table III 6. Floor loads	79
TABLE III 7 . BALCONY LOADS	79
TABLE III 8. ROOF SLOPE LOADS	79
TABLE III 9. MASONRY ELEMENT MECHANICAL CHARACTERISTICS	80
TABLE III 10. MATERIALS COEFFICIENTS	80
TABLE III 11. TIMBER MECHANICAL CHARACTERISTICS	80
TABLE III 12 STRUCTURAL STEEL MECHANICAL CHARACTERISTICS	81
Table III 13 Floor dimensions	81
TABLE III 14 LOOR MECHANICAL CHARACTERISTICS	81
TABLE III 15 ROOF MATERIALS	82
TABLE III 16 THE RESISTANCE DIRECTION OF THE FLOOR	82
TABLE IV 1 THE BEHAVIOUR OF THE MASONRY IN SHEAR AND THE RELATED LEVEL OF DAMAGE	87
TABLE IV 2 THE BEHAVIOUR OF THE MASONRY IN BENDING MECHANISM AND THE RELATED LEVEL OF DAMAGE	ъ́Е 88
TABLE IV 3 THE LEGEND TABLE FOR VERIFICATION OF ELEMENT STATUS	92
TABLE IV 4 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 1	86
TABLE IV 5 VERTICAL LOAD BEARING RESISTANCE VERIFICATION FOR WALL 1	86
TABLE IV 6 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 3	87
TABLE IV 7 VERTICAL LOAD BEARING RESISTANCE VERIFICATION FOR WALL 3	87
TABLE IV 8 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 6	88
TABLE IV 9 VERTICAL LOAD BEARING RESISTANCE VERIFICATION FOR WALL 6	88
TABLE IV 10 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 7	89
TARLE IV 11 VERTICAL LOAD REARING RESISTANCE VERIFICATION FOR WALL 7	90

TABLE IV 12 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 8	90
TABLE IV 13 VERTICAL LOAD BEARING RESISTANCE VERIFICATION FOR WALL 8	91
TABLE IV 14 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 9	92
TABLE IV 15 VERTICAL LOAD BEARING RESISTANCE VERIFICATION FOR WALL 9	92
TABLE IV 16 SLENDERNESS AND ECCENTRICITY VERIFICATION FOR WALL 10	93
TABLE IV 17 VERTICAL LOAD BEARING RESISTANCE VERIFICATION FOR WALL 10	93
TABLE V 1. THE SITES CLASSIFICATIONS	100
TABLE V 2. THE ZONES ACCELERATION	100
TABLE V 3. SITES PERIODS	101
TABLE V 4. QUALITY FACTORS INDEX.	101
TABLE V 5. WEIGHTING COEFFICIENT	102
TABLE V 6 DIRECTION OF THE EARTHQUAKE	
TABLE V 7 SUMMARY OF VERIFICATION EQUATIONS FOR MASONRY WALL	109
TABLE V 8 VERIFICATION OF THE CRITICAL DIRECTION OF THE EARTHQUAKE	110
TABLE V 9 PUSHOVER CRITICAL DIRECTION OF THE EARTHQUAKE	110
TABLE V 10 COLOURS LEGEND	111
TABLE V 11 WALL 10 ANALYSIS DAMAGE RESULTS X DIRECTION	112
TABLE V 12 WALL 10 INPUT CONDITIONS	113
TABLE V 13 WALL 10 GEOMETRY	113
TABLE V 14 WALL 10 MECHANICAL CHARACTERISTICS	113
TABLE V 15 WALL 10 APPLIED FORCES FOR X DIRECTION	113
TABLE V 16 WALL 10 RESISTANCE FORCES VERIFICATIONS FOR X DIRECTION	114
TABLE V 17 WALL 7 ANALYSIS DAMAGE RESULTS X DIRECTION	
TABLE V 18 WALL 7 INPUT CONDITIONS	
TABLE V 19 WALL 7 GEOMETRY	116
TABLE V 20 WALL 7 MECHANICAL CHARACTERISTICS	116
TABLE V 21 WALL 7 APPLIED FORCES FOR X DIRECTION	116
Table V 22 Wall 7 resistance forces verifications for X direction	116
TABLE V 23 WALL 8 DEFORMATIONS RESULT FOR Y DIRECTION	119
TABLE V 24 WALL 8 INPUT CONDITIONS	119
TABLE V 25 WALL 8 GEOMETRY	120
TABLE V 26 WALL 8 MECHANICAL CHARACTERISTICS	120
TABLE V 27 WALL 8 APPLIED FORCES FOR Y DIRECTION	120
Table v 28 wall 8 resistance forces verifications for y direction	120
TABLE V 29 PERFORMANCE POINT X DIRECTION NUMERICAL METHOD DATA	126
TABLE V 30 PERFORMANCE POINT Y DIRECTION NUMERICAL METHOD DATA	129
Table v 31. Correspondence between damage level $\mathbf{D}_{s\kappa}$ and damage grades \mathbf{D}_{k} related	ED TO STRUCTURAL
AND NON-STRUCTURAL DAMAGE, (SERGIO LAGOMARSINO, ET AL,2006)	133
TABLE VI 1 BLOCK MECHANICAL CARACTERISTICS	139
TABLE VI 2 PIERS ELEMENT TYPE OF REINFORCEMENT	139

TABLE VI 3 PIERS FRCM GEOMETRICS	139
TABLE VI 4 FRCM ON PIERS MECHANICAL CHARACTERISTICS	139
TABLE VI 5 SPANDREL ELEMENT TYPE OF REINFORCEMENT	140
TABLE VI 6 SPANDREL FRCM GEOMETRICS	140
TABLE VI 7 FRCM ON SPANDREL MECHANICAL CHARACTERISTICS	140
TABLE VI 8 WALL FRAME REINFORCEMENT CHARACTERISTICS FOR WALLS	140
TABLE VI 9 TIE ROD REINFORCEMENT CHARACTERISTICS FOR HORIZONTAL ELEMENTS	140
Table vi 10 wall 1 static state after reinforcement	143
TABLE VI 11 WALL 1SLANDERNESS AND ECCENTRECITY VERIFICATION AFTER REINFORCEMENT	144
TABLE VI 12 WALL 1 VERTICAL LOAD BEARING VERIFICATION AFTER REINFORCEMENT	144
TABLE VI 13 WALL 6 STATIC STATE AFTER REINFORCEMENT	144
TABLE VI 14 WALL 6 SLANDERNESS AND ECCENTRECITY VERIFICATION AFTER REINFORCEMENT	144
TABLE VI 15 WALL 6 VERTICAL LOAD BEARING VERIFICATION AFTER REINFORCEMENT	145
TABLE VI 16 WALL 7 STATIC STATE AFTER REINFORCEMENT	146
TABLE VI 17 WALL 7 SLANDERNESS AND ECCENTRECITY VERIFICATION AFTER REINFORCEMENT	146
TABLE VI 18 WALL 7 VERTICAL LOAD BEARING VERIFICATION AFTER REINFORCEMENT	147
TABLE VI 19 WALL 10 STATIC STATE AFTER REINFORCEMENT	148
TABLE VI 20 WALL 10 SLANDERNESS AND ECCENTRECITY VERIFICATION AFTER REINFORCEMENT	148
TABLE VI 21 WALL 10 VERTICAL LOAD BEARING VERIFICATION AFTER REINFORCEMENT	148
TABLE VI 22 VERIFICATION OF THE CRITICAL DIRECTION OF THE EARTHQUAKE AFTER REINFORCEMENT	150
TABLE VI 23 PUSHOVER CRITICAL DIRECTION OF THE EARTHQUAKE AFTER REINFORCEMENT	
TABLE VI 24 WALL 10 DYNAMIC STATE AFTER REINFORCEMENT	151
TABLE VI 25 WALL 10 ANALYSIS DAMAGE RESULTS X DIRECTION AFTER REINFORCEMENT	151
Table vi 26 wall 10 input conditions	
Table vi 27 wall 10 geometry	152
TABLE VI 28 WALL 10 MECHANICAL CHARACTERISTICS	152
TABLE VI 29 WALL 10 REINFORCEMENT TYPOLOGY APPLIED	152
TABLE VI 30 WALL 10 APPLIED FORCES FOR X DIRECTION AFTER REINFORCEMENT	152
TABLE VI 31 WALL 10 RESISTANCE FORCES VERIFICATIONS FOR X DIRECTION AFTER REINFORCEMENT	153
TABLE VI 32 WALL 7 DYNAMIC STATE AFTER REINFORCEMENT	154
TABLE VI 33 WALL 7 ANALYSIS DAMAGE RESULTS X DIRECTION AFTER REINFORCEMENT	154
Table vi 34 wall 7 input conditions	154
TABLE VI 35 WALL 7 GEOMETRY	155
TABLE VI 36 WALL 7 MECHANICAL CHARACTERISTICS	155
TABLE VI 37 WALL 7 REINFORCEMENT TYPOLOGY APPLIED	155
TABLE VI 38WALL 7 APPLIED FORCES FOR X DIRECTION AFTER REINFORCEMENT	155
TABLE VI 39 WALL 7 RESISTANCE FORCES VERIFICATIONS FOR X DIRECTION AFTER REINFORCEMENT	156
TABLE VI 40 WALL 8 DYNAMIC STATE AFTER REINFORCEMENT	158
TABLE VI 41 WALL 8 ANALYSIS DAMAGE RESULTS Y DIRECTION AFTER REINFORCEMENT	158
Table vi 42 wall 8 input conditions	158

Table vi 43 wall 8 geometry	. 159
Table vi 44 wall 8 mechanical characteristics	. 159
TABLE VI 45 WALL 8 APPLIED FORCES FOR Y DIRECTION AFTER REINFORCEMENT	. 159
Table vi 46 wall 8 resistance forces verifications for y direction after reinforcement	. 159
TABLE VI 47 PERFORMANCE POINT X DIRECTION NUMERICAL METHOD DATA AFTER REINFORCEMENT	. 162
TABLE VI 48 PERFORMANCE POINT Y DIRECTION NUMERICAL METHOD DATA AFTER REINFORCEMENT	. 163
Table vi 49. Correspondence between damage level \mathbf{D}_{SK} and damage grades \mathbf{D}_{K} related to	
STRUCTURAL AND NON STRUCTURAL DAMAGE.	. 165
Table vi 50 comparaison of the damage histograms before and after reinforcement for both	
SEISMIC DIRECTIONS	. 166

THE LIST OF ABBREVIATIONS

1 is the length of the panel
t is the thickness
σ_0 is the average compression tension
N is the axial compressive action (assumed positive in compression)
N_u is the maximum axial compressive action of the panel an it is equal to 0.85 f_m 1 t -fm is the average resistance in compression of the masonry.
E Young's modulus
Eh Young's modulus horizontal
G Shear modulus
W load weight
Fm Mean compressive strength
fvm0 Mean shear strength
fvlim shear strength (limit) (2.2 MPa)
fk the characteristic values or the Characteristic strength
γM partial factor
fma;m Mean compressive strength
fh;m Mean compressive strength horizontal
fb Mean compressive strength brick element
fma;v;o;m Mean initial shear strength
Fu masonry compressive strength
μma;m Bed-joint friction coefficient
M is the resistance to limb
H is the height of the frame
L is the length of the panel

T is the thickness

 Σ_0 is the average compression tension

N is the axial compressive action (assumed positive in compression)

Nu is the maximum axial compressive action of the panel an it is equal to 0.85 fm 1 t

H'p is assumed as the maximum value between the axial load n acting on spandrel and hp

Hp is the minimum value between the tensile strength of elements coupled to the spandrel and $0.4f_{hu}dt$

c friction coefficient and cohesion of mortar joint

φ interlocking parameter

σs entity of compressive stresses acting at the end-sections of the spandrel)

1' length of compressed part of cross section

το masonry shear strength

b stress distribution factor as function of slenderness

J, w: modulus of inertia and modulus of resistance

GENERAL INTRODUCTION

Algeria, a nation steeped in a profound cultural legacy, boasts a remarkable abundance of masonry structures that bear witness to its historical and architectural heritage. From the ancient Berber civilizations to the Islamic influences and the French colonial period, Algeria's heritage reflects a tapestry of diverse cultural traditions. The architectural marvels scattered across the country serve as tangible embodiments of this captivating heritage, embodying the stories of the past and the enduring spirit of the Algerian people.

The masonry structures found throughout Algeria stand as enduring testaments to the nation's rich history. These structures, ranging from grand palaces and mosques to humble dwellings and fortifications, encapsulate the architectural prowess and craftsmanship of their respective eras. They symbolize the cultural identity of Algeria, preserving the narratives of its ancient civilizations, conquerors, and cultural interactions.

However, amidst the allure and historical significance of these masonry structures, concerns arise regarding their preservation and longevity. Algeria faces unique challenges in safeguarding its architectural heritage. The absence of dedicated research and limited efforts in reinforcing these structures have left them vulnerable to deterioration and potential loss. Furthermore, the lack of comprehensive codes or guidelines specific to the Algerian context adds complexity to the task of analyzing and rehabilitating masonry structures.

Analyzing masonry structures proves to be an intricate task due to the need for detailed modelling using methods like the element finite method, which can be time-consuming and labour-intensive. However, owing to the complex nature of the material and the dearth of standardized methodologies. In this thesis, we direct our attention to one such remarkable structure, the School of Asla Hocine in Annaba. This iconic building is a distinguished heritage masonry edifice in Algeria. The paramount objective of our study is to conduct a comprehensive seismic assessment and rehabilitation investigation of this venerable building. To achieve this goal, we employ the macroelement method "Equivalent Frame Method," an internationally recognized approach substantiated by the esteemed Italian

3muri software. The thesis is meticulously structured into six chapters, each dedicated to distinct facets of the assessment and rehabilitation process. Chapter 1 undertakes extensive bibliographic research, meticulously scrutinizing masonry structures, elucidating their constituent elements, appraising the mechanical characteristics of masonry walls, and probing dynamic analysis methods, including the renowned pushover analysis technique and viable reinforcement methodologies. Chapter 2 focuses intently on the modelling hypotheses and methodology that underpin our study, elucidating the advantages and rationale underpinning the adoption of the Equivalent Frame Method. Chapter 3 provides a comprehensive exposition of the School of Asla Hocine, encompassing its architectural and structural characteristics, constituting the indispensable foundation for subsequent analytical undertakings. Chapter 4 meticulously executes the static verification of the structure, meticulously scrutinizing its stability and ensuring compliance with rigorous safety standards. Progressing further, Chapter 5 delves extensively into seismic and vulnerability analyses, comprehensively scrutinizing the structure's response to seismic forces, identifying potential vulnerabilities, and discerning the fragility and extent of potential damage. Finally, Chapter 6 meticulously delineates an array of meticulous reinforcement strategies, propounding the proposed measures to fortify the structure's resilience, subsequently followed by a rerun of the static, seismic, and vulnerability analyses to ascertain the efficacy and impact of the reinforcement endeavours. This comprehensive study strives to contribute significantly to the preservation and safeguarding of Algeria's invaluable masonry heritage, furnishing valuable insights and recommendations to guide future undertakings in the assessment and rehabilitation of comparable structures.

CHAPTER I REVUE ON HISTORICAL MASONRY BUILDINGS

I.1 Introduction

Masonry structure material refers to the materials used to build a masonry construction, often employing blocks or bricks composed of concrete, clay, stone, or glass. The material attributes of the masonry construction, including the units, mortar, and assembly, determine the building's strength, durability, and overall performance.

Masonry buildings are recognized for their strength and durability, making them a popular choice for a variety of applications, including residential, commercial, and industrial development. The material features of the masonry construction can be adapted to specific uses, such as load-bearing capacity, resistance to weather conditions, and thermal performance.

Compressive strength, water absorption, thermal expansion, and resistance to weathering and erosion are all important material attributes of a masonry construction. The compressive strength of the masonry unit and mortar is crucial to the structure's load-bearing capability, while water absorption influences durability and weather resistance. Thermal expansion is vital to consider when constructing a structure to handle temperature fluctuations, and resistance to weathering and erosion influences the structure's lifetime and maintenance requirements.

Overall, a masonry building's material qualities are a significant concern in its design and construction, and careful material selection may assist to guarantee that the structure achieves the specified performance standards and has a long service life.

I.2 MATERIAL PROPERTIES OF MASONRY

Units in masonry construction are the building blocks used to create material properties of masonry structures, including the unit, mortar, and assembly. The unit refers to the building blocks used, while the mortar acts as the bonding agent. The masonry assembly involves arranging and bonding these components. Considering these properties is crucial for durable and robust masonry construction.

I.2.1 The Units

The structure. They can be made of materials such as bricks, concrete blocks, or stone blocks. The size, shape, and material of the units impact the design, strength, and aesthetic appeal of the masonry. Factors such as dimensions, compressive strength, and compatibility with mortar should be considered for structural integrity and durability. Adhering to building codes and standards is essential for successful masonry construction.

Table I 1.types of masonry units (MASONRY-ROOF - FLOOR CONSTRUCTION, 2020)

Sun-dried or unburnt clay bricks

Un-dried or unburned bricks are less durable and are typically employed in temporary buildings. They are made in three stages: clay, molding, and drying. They are exposed to sunshine after molding and dried utilizing heat from the sun. These bricks are less resistant to water and fire, making them unsuitable for permanent buildings.



Brick masonry construction

Burnt clay bricks

A "brick" is an artificial structural element that takes the shape of a rectangular block of clay. Bricks of any form or size may be made and there are various types.

Burnt bricks are classified into four types: first class bricks, second class bricks, third class bricks, and fourth class bricks.

Brick masonry construction makes use of first-class burnt clay bricks. For less important construction, third class bricks are used in masonry. Second class bricks are best for masonry construction that is plastered as it lacks finish compared with first class bricks.

The overall tensile strength offered by the brick masonry is less and is irrespective of the class of brick chosen. Overall performance depends on the size, position, and number of openings provided to the masonry structure.



First Class Bricks)



Second Class Bricks



Third Class Bricks



Fourth Class Bricks

Fly ash bricks

Fly ash bricks are made from fly ash and water and have superior qualities than clay bricks. They are lightweight and resistant to freeze-thaw cycles, with good fire



insulation, high strength, consistent diameters, decreased water penetration, and no soaking required before use in masonry construction.

Concrete bricks

Concrete bricks are made from concrete that contains cement, sand, coarse particles, and water. They are used to create masonry and framed structures, facades, and fences, and they have an outstanding visual presence.

Concrete bricks may be made onsite, reducing the amount of mortar required, and providing a variety of colors.



Engineering bricks

Engineering bricks have a high compressive strength and are utilized in applications that need strength, frost resistance, acid resistance, low porosity, and damp proof courses.



Sand lime or calcium silicate bricks

Calcium silicate bricks are often known as sand lime bricks because they are comprised of sand and lime. These bricks are used in the construction industry for a variety of applications, including decorative work in buildings, masonry work, and so on.



Stone masonry construction

Stone is the most durable, strong and weatherresistant construction material compared with any others. These are less affected by daily wear and tear. Masonry structures made out of stone hence last for a longer period. It has a life period of 300 to 1000 plus years. Due to it's numerous advantageous, it is widely used in masonry construction.

Rubble masonry is again

classified into:

Stone masonry has two main classifications: -rubble masonry -ashlar masonry Random Rubble masonry

Is rubble masonry that uses either undressed or hammer dressed stones. Furthermore, random rubble masonry is classified into two types:

Coursed:

The stones used in this form of brickwork are of varying sizes.

This is the most basic and least expensive type of stone masonry. The masonry work in coursed random rubble masonry is done in courses such that the stones in each course are of identical height.



The stones used in this form of brickwork are of varying sizes. This is the most basic and least expensive type of stone masonry. The coarses are not maintained on a regular basis in uncoursed random rubble masonry. The bigger stones are put first, with spalls or sneeks filling in the gaps between them



Coursed random rubble masonry



uncoursed random rubble masonry

Uncoursed or Coursed Square Masonry

The stone blocks of this style are hammered into roughly square shapes. In most cases, the facing stones are hammer-dressed. As quoins, large stones are utilized. The use of chips in bedding is avoided as much as possible.



Coursed Square Masonry

Coursed:

Straight bed and side stones are utilized in this form of construction. The stones are normally squared before being hammer dressed or straight cut. The work in coursed square rubble masonry is done in varied depth courses.

Uncoursed:

Stones with straight bed and sides are utilized in this form of construction. The stones are normally squared before being hammer dressed or straight cut.

Different sizes of stones with straight edges and sides are put on face in many unusual patterns in uncoursed square rubble brickwork.



Uncoursed Square Masonry

Flint rubble masonry

This form of brickwork is prevalent in locations where flint is abundant.

As indicated below, flint stones ranging in thickness from 8 to 15cm and length from 15 to 30cm are put in the facing in the shape of coursed or uncoursed masonry.



Polygonal Rubble Masonry

The stones in this form of brickwork are crudely processed to an irregular polygonal shape. The stones should be set in such a way that lengthy vertical joints in face work are avoided and joints are broken as much as



feasible. Small stone chips, as seen in the image, should not be utilized to support the stones on the face.

Dry Rubble Masonry

In the form of random rubble masonry without cement, this type of construction is the cheapest, and this type of masonry is utilized in the building of retaining walls of earthen dams and canal slopes. As indicated below, the hallow areas left around and stones should be closely packed with smaller stone pieces.



Ashlar Fine Masonry

Ashlar Masonry

It is well dressed (cut, worked) masonry, which can be either an individual stone that has been treated till squared or masonry made from such stone. It is the finest stone masonry unit, which is usually cuboid or trapezoidal. Is again classified into:

Ashlar masonry is a style of stonework in which finely cut and precisely shaped stones are laid in a uniform pattern to create a smooth and elegant surface. The type of stone used is typically a high-quality, finely-grained stone such as granite, limestone, or marble. The stones are cut to a specific size and shape and laid in rows with carefully controlled joints to create a clean, precise appearance.



Ashlar Fine Masonry

Ashlar Block in Course

Ashlar blocks in course construction are accurately cut and shaped and the bricks laid in a running bond pattern, with each block offset from the one below it. This creates a strong and stable wall that is able to withstand the forces of nature and the weight of the structure it supports.



Ashlar Block in Course

Ashlar Chamfered Masonry

Durable and elegant finish that requires skilled craftsmen to create. The blocks are cut at a consistent angle and laid in horizontal courses with tightly controlled joints, creating a smooth and even surface. The result is a durable and elegant finished product that can withstand the test of time.



Ashlar Rough Tooled Masonry

Ashlar rough tooled masonry is a rustic and natural look for buildings in rural areas. It creates irregular marks and grooves on the surface of the stone, giving it a rustic and natural appearance. The rough tooling must be done with great care to ensure that the blocks fit together tightly and create a stable wall. It also gives the building a sense of age and character, while providing a durable and long-lasting surface.



Rock or Quarry Faced Masonry

The rough surface of rectangular blocks of stone is obtained by chipping or carving the surface with a hammer and chisel or other hand tools. This is utilized in the construction of buildings that need to have a rough and natural appearance, such as country residences, lodges, or structures in rural or mountainous settings. The stone chipping or carving must be done with great care to ensure that the blocks fit firmly together and form a sturdy wall.



I.2.2 The Mortar

Sand, water, and a binder (such as cement or lime) are combined uniformly to form mortar, which has the proper consistency. It is employed to repair gaps, level races, and create consistent bedding. The first mortars were made of clay or clay-straw combinations, and they have developed through the years to become gypsum mortar and lime mortar. And so on.

CHAPTER I MASONRY BIBLIOGRAPHIC RESEARCH

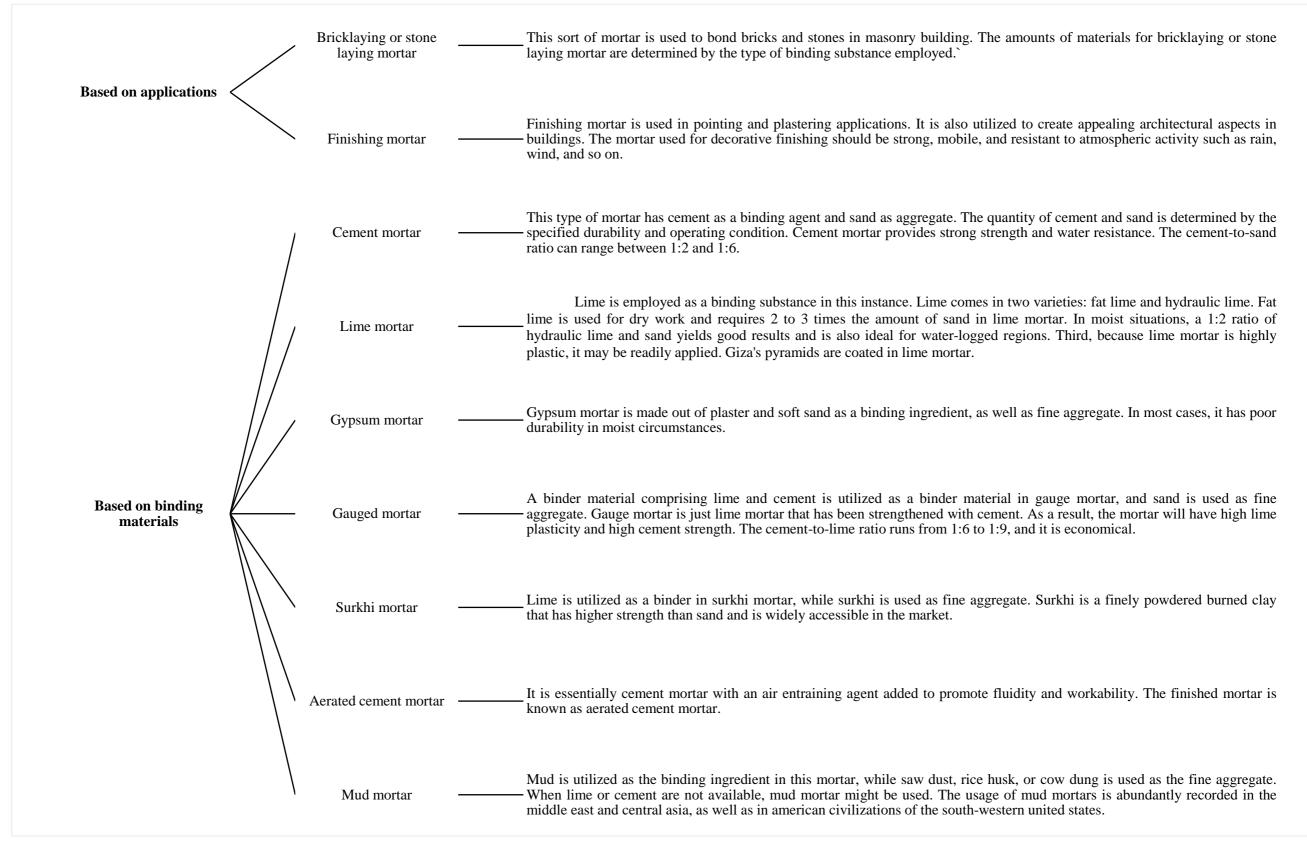


Figure I 1different types of motar and their classifications "1"

CHAPTER I MASONRY BIBLIOGRAPHIC RESEARCH

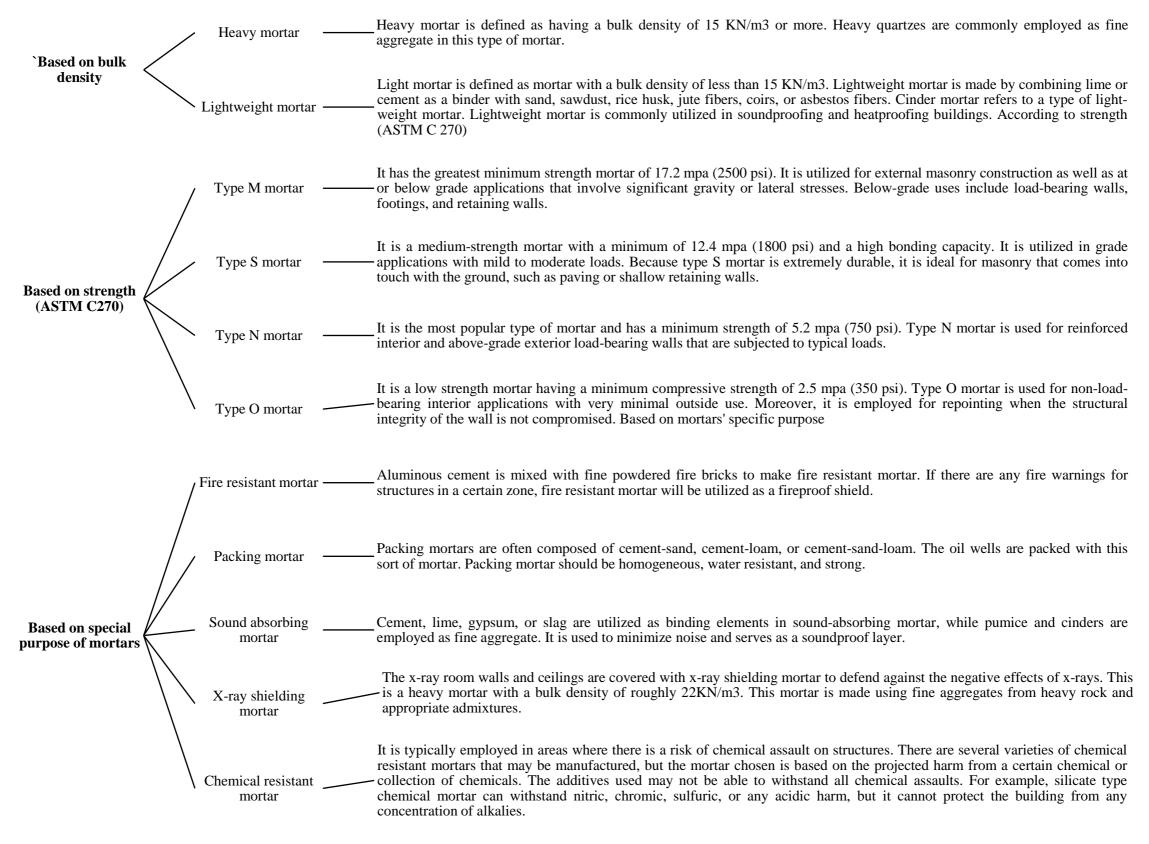


Figure I 2 different types of motar and their classifications "2"

An outline of the broad history of mortar is useful for context. Not all mortars are created equal. It was found thousands of years ago that burning certain clays and stones created compounds that were ideal for use as mortar binders. Cement was made by burning limestone with clay. Lime was created by burning purer limestone.

The success and performance of the cements and limes created varied greatly. Some of the variations were produced by the different compositions of the minerals burnt, while others were induced by the different procedures utilized. There are several variables in the process of producing cement or lime, as well as numerous variations in the rock or mineral resources utilized. It is a highly specialized study of industrial technology and chemistry.

For thousands of years, lime has been the primary binder in mortars throughout the Western world. Cements have been employed in certain places and for specific types of masonry, but they have been utilized less broadly. The reason for this is that excellent lime (produced by burning limestone in a certain method) works extremely well in masonry walls. It is quite robust (with the correct sand), incredibly flexible (it even cures its own cracks), and enables moisture to pass through readily (while repelling water on the exterior).

The best mortar limes are manufactured from exceptionally high-calcium limestone. Perhaps because high-calcium limestone is not widely available, and because it was not widely known before 1900 how to control all the variables in the process of making good lime, it was easily outsold by Portland cement, a scientifically formulated product that hardens quickly and can be made almost anywhere.

It's no surprise that, with the industrial revolution of the nineteenth century, Portland cement began to be mass-produced by a few and became widely relied on. This highly standardized substance was invented in the 1870s and had begun to replace lime as the primary binder for mortar by the 1920s and 1930s.

Masons had completely forgotten how to make or use lime as a binder in their mortars by the 1960s.

Lime mortar science and use has made a resurgence in recent years, owing mostly to the efforts of a few tradespeople. People are rediscovering the fundamentals of lime mortar, realizing that it is, in fact, the greatest mortar for human-scale construction and repair.

Finally, in order to improve systematic reading comprehension, we have summarized the text as follows:

CHAPTER I MASONRY BIBLIOGRAPHIC RESEARCH

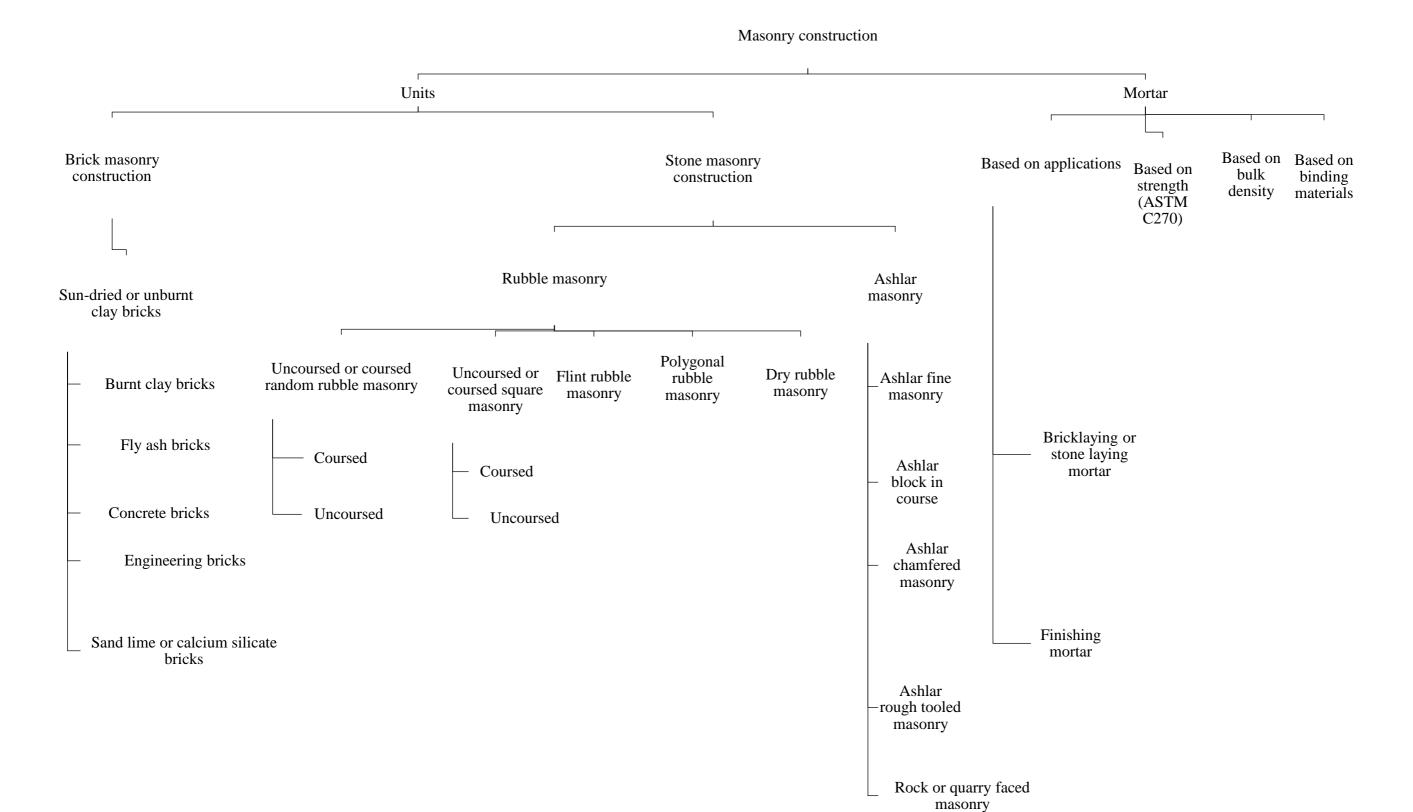


Figure I 3 masonry construction component

I.3 ASSEMBLY OF MORTAR AND MASONRY

According to (Valek, 2003) the interaction between mortar and masonry is an effect between them which results in some physical or chemical change to one or both of them. It is as an evaluation of compatibility performance. Bad interaction means that incompatible materials or repair techniques were applied. It results in deterioration and accelerated weathering of masonry material. However, the use of an incompatible mortar or treatment does not mean bad interaction a priori, it merely brings about conditions favourable for deterioration. The deterioration itself happens through environmental agents. For example, a dense cement mortar containing salts used for repointing of porous sandstone masonry may not cause any bad interaction without the presence of moisture in very dry ageing conditions. Water or moisture is needed for a chemical and most physical deterioration processes to take place (Collepardi 1990). Sumlnarised by Amoroso & Fassina (1983), water is the main cause of degradation mechanisms for masonry materials.

A way of studying building materials from a conservation science point of view is to study their damage lnechanisms and their deterioration (e.g. Torraca in Porous Building Materials, 1988). Possibly the best model for scientific studies of deterioration of masonry materials is based on a review of literature on deterioration of porous materials published by ICCROM in 1976 (Stambolov and van Asperen de Bore 1976). Torraca (1988) later on in 'Porous Building Materials' described material deterioration under the following categories:

I.3.1 External Mechanical Deterioration

This is caused by excess of stress with respect to the strength of the material (load, thermal expansion, stress caused by transport or working techniques, dynanlic load and vibration). When excessive stress occurs, the material cracks and even small hair-cracks can lead, in combination with other deterioration factors, to accelerated deterioration.

I.3.2 Internal Mechanical Deterioration

This is sonletinles called physical deterioration and is mostly due to a physical variation of water inside masonry like evaporation, capillary flow. A large stress can arise inside the pore structure whenwater freezes and crystals of ice or minerals are formed within the originally water filled pores damage caused by salt crystallisation and efflorescence or similar effects.

I.3.3 Chemical Deterioration

This is mostly connected with a reaction between sulphate and the other compounds in the masonry (Collepardi 1990) Chemical coivosioll almost always requires the presence of water (Torraca 1988). Water can play two roles in chemical corrosion:

- (A) water in the form of liquid and vapour is chemically active
- (B) water in the form of liquid acts as a transport medium for other components

Water which has been in contact with other solid material of the same kind is not chemically active (rising damp) but it can still act as a transport medium for other deterioration agents, e.g. See physical deterioration. The danger of chemical corrosion increases with atmospheric pollution and acid rains (Charola 1986).

I.3.4 Biodeterioration

This can be caused by bacteria, algae and/or fungi which produce acid. Lichens can also penetrate into several millimetres of the surface of the material. Moss commonly grows on the surface of alkaline inaterials (lime mortar, torraca 1988). Roots of higher vegetation can penetrate deeply into joints and cause deterioration of the masonry.

I.4 ESTIMATION OF THE MECHANICAL PROPERTIES OF MASONRY

There are several methods for evaluating the mechanical properties of historic masonry buildings. There are two sorts of approaches: direct and indirect. In the first approach, mechanical properties are extracted directly from the material by in-situ or laboratory studies.

(Due to political and administrative constraints, a lack of testing instruments, and a lack of access to construction components, there is a lack of interest in research and restoration of historic masonry structures in Algeria. Access to building components is restricted to a few state agencies).

The attributes are retrieved indirectly in the second method through a correlation methodology from databases that provide comparable estimates or from component qualities. Which this approach is based on a visual examination as well as knowledge of the construction type and the morphology of the wall, in condition.

The Italian codentc18 is used for correlation processes.

I.4.1 The Italian Code Ntc 18

As (SEBOUI Hatem, 2022) said ,The main mechanical characteristics of various types of ancient masonry, whose mechanical attributes rely on knowledge levels, or KLS, are referenced in the Italian Code (NTC, 2018).

The reference values for the masonry qualities under the most typical situations in historic URM structures are shown in Table 1.

The multipliers mentioned in Table 2 should be used to adjust the design material specifications for masonry with superior characteristics.

Each knowledge level has a confidence factor (CF) value assigned to it, as shown in Table 3.

Table I 2. Reference ranges for different masonry material parameters (SEBOUI Hatem, 2022).

Masonry typology	Compression strength fm(mpa) Min – max	Shear strength $\tau 0 \text{(kpa)}$	Young modulus Em (mpa) Min – max	Shear modulus Gm (mpa) Min –max	Weight density Wm (kN/m3)
Irregular stone masonry (pebbles, erratic, irregular Stones)	1.0 - 1.8	20 - 32	690 - 1050	230 - 350	19
Uncut stone masonry with facing walls of limited Thickness	2.0 - 3.0	35 - 51	1020 - 1440	340 - 480	20
Cut stone with good bonding	2.6 - 3.8	56 - 74	1500 - 1980	500 - 660	21
Soft stone masonry such as tuff and limestone	1.4 - 2.4	28 - 42	900 - 1260	300 - 420	16
Dressed rectangular stone masonry	6.0 - 8.0	90 - 120	2400 - 3200	780 - 940	22
Solid brick masonry with lime mortar	2.4 - 4.0	60 - 90	1200 - 1800	400 - 600	18

Table I 3. Correction factors for different parameters of masonry types (SEBOUI Hatem, 2022)

Masonry typology	Good mortar quality	Joint thickness <10 mm	Regular Courses of bricks	Transverse connection	Wide or poor internal core	Grout injection	Reinforced plaster
Irregular stone masonry(pebbles, erratic,)	1.5	-	1.3	1.5	0.9	2	2.5
Uncut stone masonry with facing walls of limited thickness	1.4	1.2	1.2	1.5	0.8	1.7	2
Cut stone with good bonding	1.3	-	1.1	1.3	0.8	1.5	1.5
Soft stone masonry (tuff, limestone)	1.5	1.5	ı	1.5	0.9	1.7	2
Dressed rectangular stone masonry	1.2	1.2	ı	1.2	0.7	1.2	1.2
Solid brick masonry with lime mortar	1.5	1.5	-	1.3	0.7	1.5	1.5

Table I 4. Knowledge levels are based on available information and corresponding values of the confidence factors for masonry buildings (SEBOUI Hatem, 2022)

Knowledge levels	Geometry	Constructive details	Material properties	Analysis methods	CF
KL1	Geometric survey of masonry, masonry, floor, vaults, staircase. Identification of the loads on each wall element, identification of the type of foundation. Identification of cracks and	Limited in-situ inspection	Limited in situ investigations: - Strength: minimum value from table 2. - Modulus of elasticity: average value of the interval of Table 2 Extensive in situ investigations:	All methods	1.35

KL2	deformation.		- Strength: average	1.20
		Eutonoise and	value from Table 2.	
		Extensive and comprehensive in-	- Modulus of	
		situ inspection	elasticity: average	
		2-10F	value of the tests or	
			the interval in Table	
			2.	
			Comprehensive in	
			situ investigations	
			Case a) availability of	
			at least three	
			experimental values	
			of the strength:	
			- Strength: average	
			experimental value.	
			- Modulus of	
			elasticity: average	
			value of the tests or	
			the interval in Table	
			2.	
			Case b) availability of	
			2 experimental values	
			of the strength:	
			- Strength: if the	
			average experimental	
			value is within the	
KL3			range of Table 2, take	1.00
			the average value	
			from the table; if the average experimental	
			value is higher or	
			lower than the range	
			of Table 2, taking the	
			experimental value,	
			- Modulus of	
			elasticity: same value	
			as LK3 Case a. Case	
			c) availability of a	
			single experimental	
			value of the strength:	
			- Strength: if the	
			average experimental	
			value is within the	
			range of Table 2 or	
			higher, take the	

	average value of the	
	table; if the average	
	experimental value is	
	lower than the range	
	of table 2, it takes the	
	minimum value of the	
	table,	
	- Modulus of elasticity: same value as LK3 Case c.	

I.5 MASONRY BUILDING BEHAVIOURS

I.5.1 Domain Of Vulnerability Modelling

Under the domain of vulnerability modeling, many modeling methodologies for seismic capability of brick buildings have been presented. The goal of structural modeling is to generate seismic resistance characteristics for the MDOF (Multi-degree of freedom) or ESDOF (Equivalent single degree of freedom), such as strength, stiffness, and deformation capacity. These parameters are utilized as input to the structural demand analysis. The capacity curve, which defines the building's lateral force-deformation resistance, is a common result of structural modeling.

Vertical walls resist gravity loads, whereas horizontal parts (diaphragms) distribute gravity loads and transfer inertial seismic lateral forces to the walls.

I.5.2 The Seismic Behaviour Mechanisms

Masonry buildings often display three-dimensional reaction behavior when subjected to earthquake ground motion impacts. The primary processes that a masonry building shows when subjected to dynamic seismic stresses are classified as **in-plane** mechanisms and **out-of-plane** mechanisms. The building's three-dimensional reaction is comprised of an interplay between those two systems. Yet, because to the inherent challenges in investigating such complicated interactions, the difference between the two main processes is widely used to simplify the problem.

The walls that are parallel to the primary direction of ground shaking are referred to as in-plane walls. Because of their orientation, these walls offer the building's lateral load resistance and endure in-plane deformation and stresses. Windows and door apertures are generally perforated into in-plane walls. Seismic

damage to masonry walls, as well as laboratory testing, revealed that masonry walls subjected to in-plane loads can exhibit typical sorts of behaviors associated with multiple failure modes, flexural and shear failures, or a mix of both.

When the horizontal load causes tensile flexural cracking at the corners, the wall begins to act as a virtually rigid body rotating about the toe. Diagonal shear failure is commonly defined by the creation of a diagonal fracture that begins in the center of the wall and spreads to the corners. In the case of a regular brickwork design, the fracture usually travels through the mortar joints, although it can also move through the blocks. Another type of failure mode is sliding shear failure, which occurs when a horizontal bed joint plane fails, generally at one of the wall's extremities. Unfortunately, this failure is only conceivable for extremely squat walls.

The diagonal cracking shear failure is the most typically found in-plane failure mechanism in postearthquake damage assessments, particularly in ancient brick and stone masonry buildings.

The development of various failure mechanisms is determined by multiple elements, including the geometry of the wall, boundary conditions, outgoing axial load, physical properties of the masonry constituents (compression and shear strength of masonry), and masonry geometrical properties (block aspect ratio, masonry pattern). It should be emphasized that distinguishing the presence of a certain kind of mechanism is difficult since two or more failure mechanisms may occur with interactions between them.

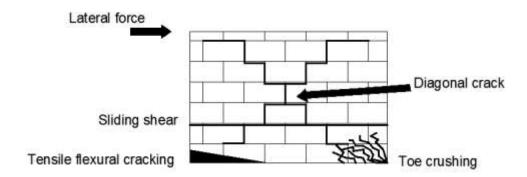


Figure I 4. Different shear modes of URM wall

Flexural failure Predominates in slender walls, while diagonal cracking predominates in intermediate slender walls over flexure and bed joint sliding as vertical stress increases. At rising degrees of vertical compression and increasing ratios Of mortar and block strengths, cracking via blocks continues to prevail to diagonal cracking propagating through mortar joints.

• (Shear failure mode emerges in constrained masonry structures owing to in-plane seismic loads (acting parallel to the plane of the wall), whereas flexural failure mode may develop due to either in-plane or out-of-plane loads (acting perpendicular to the plane of the wall.

- Horizontal cracking at the mortar bed joints on the tension side of the wall characterizes flexural failure induced by in-plane lateral stresses.)
- In unreinforced masonry walls, the out-of-plane shear failure mechanism a bending alone.
- According to the elastic theory of plates, the condition of primary stresses in a simply supported
 rectangular plate (panel) under an out-of-plane point load is tension-tension, with the largest
 tensile stress located at the center of the panel and on the tension side. As a result, cracking of the
 panel under out-of-plane stresses begins in the center and spreads to the supports.

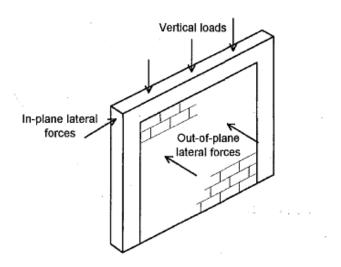


Figure I 5. in-plane and out-of-plane forces

I.6 SEISMIC ANALYSIS "PUSHOVER"

The nonlinear static pushover analysis method is an approximate method in which the structure is subjected to an increasing lateral load until a target displacement is reached.

The pushover analysis consists of a series of elastic analyses, superimposed to approximate a capacity curve or shear force curve at the base - displacement at the top.

The first step is to apply the gravitational and lateral force which results from a behavior law of the bilinear or trilinear type, the lateral load is increased in an iterative manner until reaching a first plastification of an element (appearance of plastic patella). By taking into account the new state of equilibrium due to the reduction of the stiffness, the process continues until having a limit displacement at the top of the structure or until an instability.

When the dominating response is that of the fundamental mode, the displacement of a system with numerous degrees of freedom can be nearly equal to that of a system with a single degree of freedom.

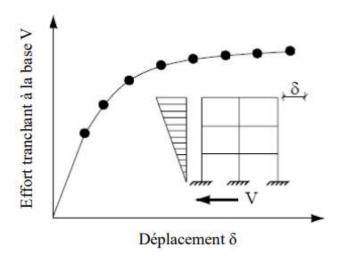


Figure I 6. structure capacity curve

I.6.1 Why Is Pushover Analysis Used

Reasonable estimates of inelastic deformation or damage in structures are required for performance-based methods.

Elastic Analysis is incapable of providing this data.

Nonlinear dynamic response history analysis can provide the necessary information, but it can be time-consuming.

I.6.2 A Brief Overview Of The Technique

A pushover analysis is divided into two sections. Initially, the "Capacity Curve" or pushover is computed by applying incremental static loads to an inelastic model of the structure. Second, this curve is used in conjunction with another "Demand" tool to calculate goal displacement.

I.6.2.1.1 The capacity curve

- 1) The Structural Analytical Model will include gravity loads, known sources of inelastic behaviour such as material constraints and plasticity effects, as well as P-Delta effects.
- 2) The modal properties such as periods and mode shapes, modal participation factors, and effective modal mass will also be computed.
- 3) The lateral inertial forces will be distributed according to the assumed distribution and a pushover curve generated:

The choice of the seismic force distributions is up to the designer, the available options are: • **uniform**: distribution of forces, deduced from a uniform trend of accelerations along the height of the construction;

Static forces: proportional distribution to static forces

$$Fi = Fh. zi. \frac{Wi}{\sum zj. Wj}$$

Modal distribution: this distribution is an alternative to "static forces" and is calculated on the basis of the identified significant modes following the calculation of modal forms. At the bottom right side, a panel allows to select which distribution to use between static and modal forces.

- 4) The model allows for evaluation of the structure's behaviour under dynamic loading (Convert the Pushover Curve to the First Mode Capacity Curve for low and medium height's buildings).
- 5) Reduce the complexity of the capacity curve (Use bilinear approximation)

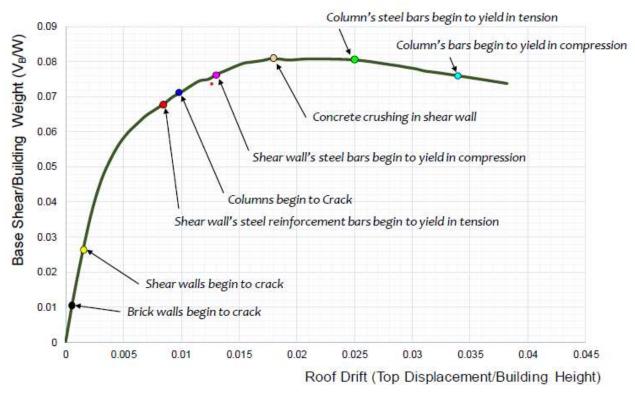


Figure I 7. Global Response and Performance

The structure's nonlinear static analysis yields a "pushover curve," as seen on the left. The sign above the curve shows that the lateral load pattern for this curve was upper triangular. Different pushover curves will be produced by various load patterns, such as uniform or proportional to first mode shape.

The pushover curve on the right is a simplified first mode bilinear variant. This curve is termed a "Capacity Curve", or "Capacity Spectrum". The values on the capacity curve's X and Y axes are modal acceleration and modal displacement.

Capacity Spectrum should transform to Another form of pushover curve (SA-SD form).

The first approach discussed is the so-called Demand Capacity Spectrum approach. This approach is detailed in the ATC 40 publication.

I.6.2.1.2 The demand curve

The output will be from;

A response spectrum in the form of displacement-acceleration, which reflects the seismic hazard level. And it will be a 5% damped ELASTIC spectrum modified for site effects, expected performance and equivalent damping. The displacement and associated acceleration will be graphed to represent the seismic loading on a structure.

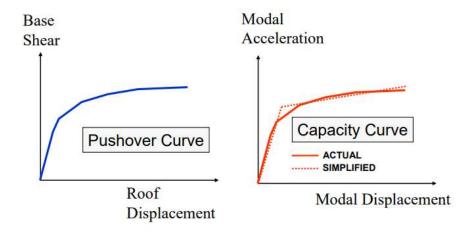


Figure I 8. Development of the Capacity Curve

Using the following equations, the Capacity Curve is transformed to a Capacity Spectrum relationship:

$$Sa = \frac{Vi}{\propto m * w} \qquad Sd = \frac{u}{PF1 * \emptyset ij}$$

When M is the total mass of the building, Øij is the modal amplitude at storey level "i" for mode "j", PF1 is a participation factor, and m is the modal mass coefficient, which are provided by:

$$PF1 = \frac{\{\emptyset\}^{T}[M]\{I\}}{\{\emptyset\}^{T}[M]\{\emptyset\}} \qquad \qquad \alpha_{M} = \frac{\left[\sum_{J=1}^{N} \text{Mi* } \emptyset \text{ij }\right]^{2}}{\sum_{I=1}^{N} \text{Mi } \sum_{J=1}^{N} \text{Mi* } \emptyset^{2} \text{Ij}}$$

PFI = modal participation factor for the first natural mode.

 \propto_1 =Modal mass coefficient for the first natural mode.

M = mass assigned to level I.

 \emptyset_{i} = amplitude of mode 1 at level i.

V= base shear.

u = roof displacement (V and the associated u make up points on the capacity curve).

 S_a =spectral acceleration.

S_d =spectral displacement (Sa and the associated Sd make up points on the capacity spectrum).

I.6.2.1.3 Target displacement using an elastic spectrum

Many methods have been known in that field as:

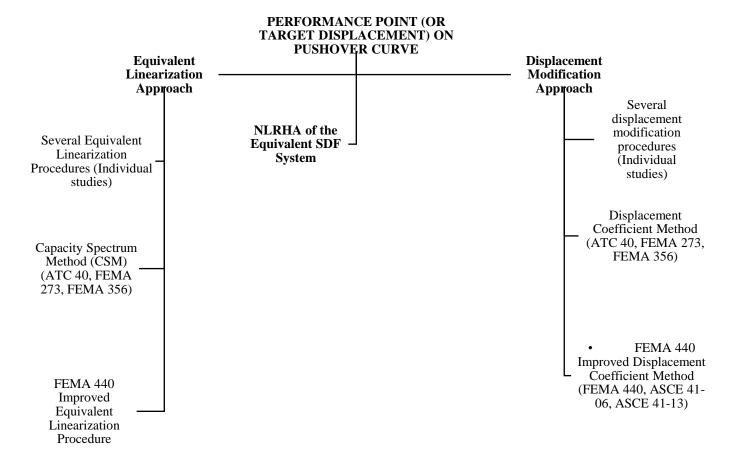


Figure I 9. the different methods utilized to distinguish the Performance Point

I.6.2.1.4 Method of equivalent linearization

Capacity spectrum approach (csm) (atc 40, fema 273, fema 356):

Conversion the Demand Spectrum to ADRS spectra

"Application of the Capacity-Spectrum technique requires that both the demand response spectra and structural capacity (or pushover) curves be plotted in the spectral acceleration vs. Spectral displacement domain. Spectra plotted in this format are known as Acceleration-Displacement Response Spectra (ADRS) after Mahaney et al., 1993.

Every point on a response spectrum curve has associated with it a unique spectral acceleration, Sa' spectral velocity, Sv' spectral displacement, sd' and period, T. To convert a spectrum. From the standard Sa vs T format found in the building code to ADRS format, it is necessary to determine the value of Sdi for each point on the curve, Sai, Ti. This can be done with the equation:

$$S_{di} = \frac{Ti^2}{4\pi^2} S_{ai} g$$

Tandard demand response spectra contain a range of constant spectral acceleration and a second range of constant spectral velocity. Spectral acceleration and displacement at period T_i are given by:

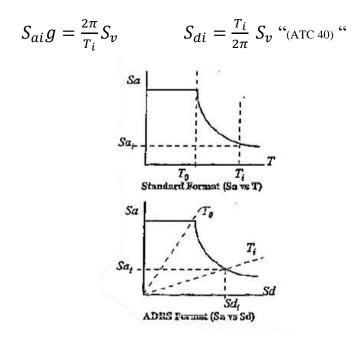


Figure I 10 Conversion to ADRS spectra (ATC 40)

According to (ATC 40) "The capacity spectrum method A, B, C (8.2.2.1) reduce the elastic spectrum to intersect the capacity curve in spectral coordinates to find a performance point ap, dp, the equal distance point a*, d*, is good starting point for the alternative process.

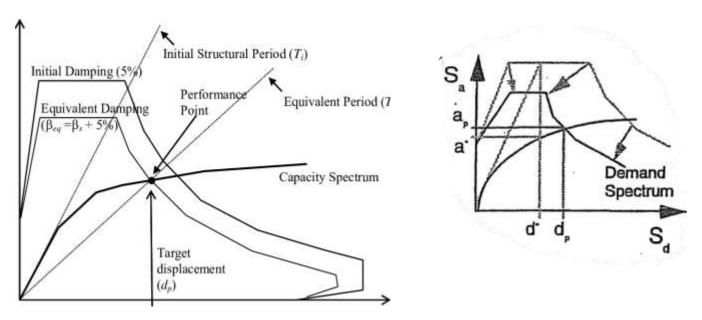
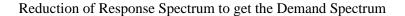


Figure I 11 Schematic representation of Capacity Spectrum Method (ATC 40)

Demand Spectrum should take Another form of response spectrum (ADRS Form) reduced based on effective damping (i.e., original inherent damping + additional hysteretic damping).



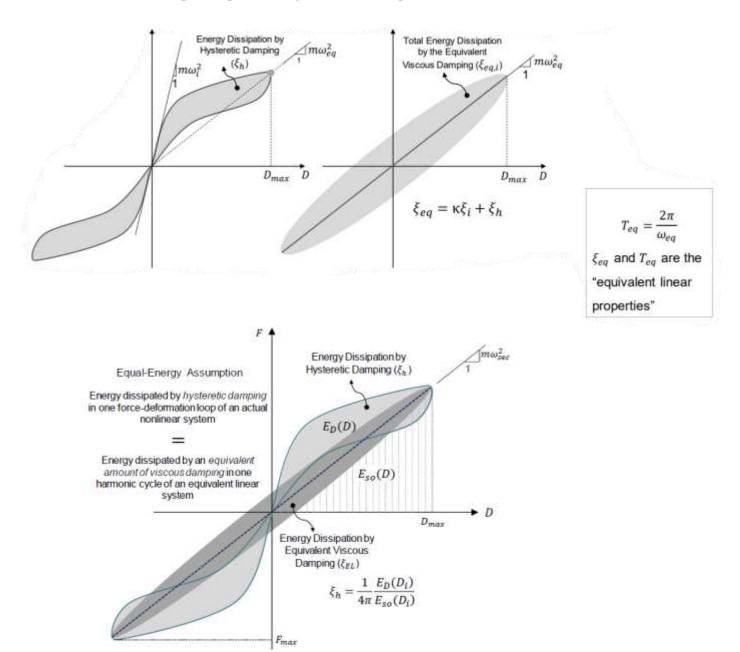


Figure I 12.Determination of Hysteretic

An Equivalent Linear System with Elongated Period and Additional Damping is the transformed form of.

A nonlinear SDF system with initial circular natural frequency ωi , and with initial inherent viscous damping ξi .

Reduction of Demand Spectrum

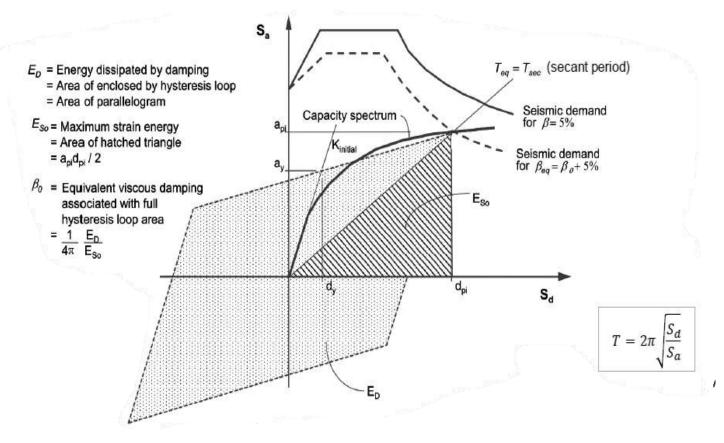


Figure I 13. Reduction of Demand Spectrum

Estimation of Damping and Reduction of 5 percent Damped Response Spectrum The damping that occurs when earthquake ground motion drives a structure into the inelastic range can be viewed as a combination of viscous damping that is inherent in the structure and hysteretic damping. Hysteretic damping is related to the area inside the loops that are formed when the earthquake force (base shear) is plotted against the structure displacement. (ATC 40)

To anticipate target displacement, the Demand Curve is utilized in conjunction with the Capacity Curve. To obtain the goal displacement, a trial-and-error approach is commonly utilized (ATC 40).

When the displacement at the intersection of the demand spectrum and the capacity spectrum, d_i , is within 5 percent $(0.95dpi \le di \le 1.05 dpi)$ of the displacement of the trial performance point, a_{pi} , d_{pi} , d_{pi} becomes the performance point. If the intersection of the demand spectrum and the capacity spectrum is not within the acceptable tolerance, then a new a_{pi} , d_{pi} point is selected and the process is repeated. The performance point represents the maximum structural displacement expected for the demand earthquake ground motion. When the capacity spectrum is a "sawtooth" curve, that is, the final composite capacity spectrum is constructed from several

different capacity spectra which account for strength degradation of elements, special care must be taken in determining the performance point. The bilinear representation of the capacity spectrum, that is used to determine the reduction factors for the 5 percent damped spectrum, is constructed for a single capacity spectrum curve, not the composite curve. For the analysis to be acceptable, the bilinear representation must be for the same single capacity spectrum curve that makes up the portion of the composite capacity spectrum where the intersection point occurs (ATC 40).

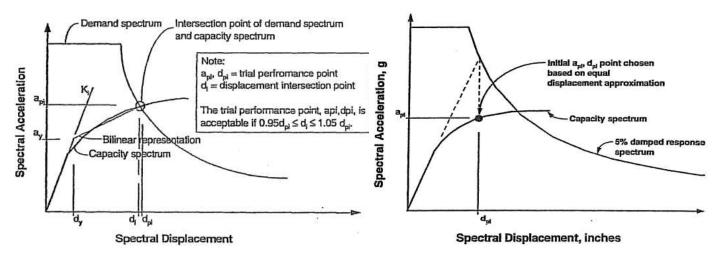


Figure I 14 Intersection point of Demand and capacity spectrums Within Acceptable Tolerance (ATC 40)

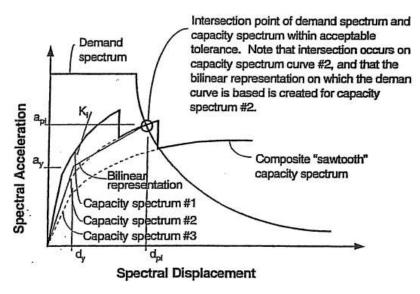


Figure I 15 The concept for a "sawtooth" capacity spectrum (ATC 40)

I.7 THE STRENGTHENING

Masonry buildings comprise a major share of existing structures worldwide. The experience of earthquakes has demonstrated that unreinforced masonry constructions may be significantly vulnerable to seismic activity. Several techniques for retrofitting masonry structures to increase seismic performance have been developed and applied during the last few decades. Surface treatment and external reinforcement are the two most common procedures for retrofitting masonry buildings.

I.7.1 Surface Treatment

The following methods can be used to reinforce masonry walls:

I.7.1.1.1 Adding reinforced concrete jackets to one or both sides of a wall

Reinforced concrete (RC) jackets are a technique for reinforcing masonry structures that involves applying jackets to one or both faces of masonry walls. This approach is utilized for both brick and stone masonry walls. To use reinforcing jackets, the plaster must first be removed from the walls. The mortar joints between the bricks have been cleaned. If there are any cracks in the masonry walls, they are first grouted. Anchor ties are placed in predrilled holes. The drill surface is cleaned and hydrated, then cement slurry is applied to the masonry surface and drills. The concrete is placed in two layers, separated by reinforcing mesh. Steel anchors hold the reinforcing mesh on both sides of the wall together. These anchors are soldered to the mesh or linked together using tying wire. The typical overall thickness of RC jackets is between 30mm and 100mm. The thickness of concrete layers is determined by the manner of application.

Reinforced Concrete Jacketing Guidelines for Masonry Wall Strengthening:

- The horizontal and vertical reinforcement should be no less than 0.25% of the jacket portion.
- The minimum reinforcement used to reinforce the ends of the wall should be 0.25% of the jacket section.
- The ties at the well ends shall have a minimum diameter of 8 mm and a maximum spacing of 150 mm.
- Dowels spaced no more than 600 mm apart in both directions must be used to secure the jacket to the previous concrete.

It is also significant that the jacket be capable of transferring forces to slab diaphragms. This may be accomplished by inserting epoxy grouted anchors and diagonal connecting bars through slab holes.

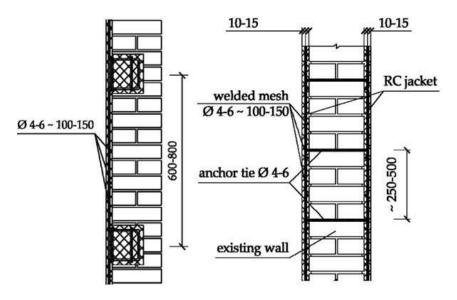


Figure I 16 Strengthening of Masonry Walls by Application of Single and Double sided reinforced concrete (RC) jackets

I.7.1.1.2 Frp structural repointing for masonry wall strengthening.

When compared to the usage of FRP laminates, structural repointing of masonry walls offers benefits. Because surface preparation (sandblasting and puttying) is not required, this method of masonry wall strengthening is straightforward. Also, the masonry's elegance is kept.

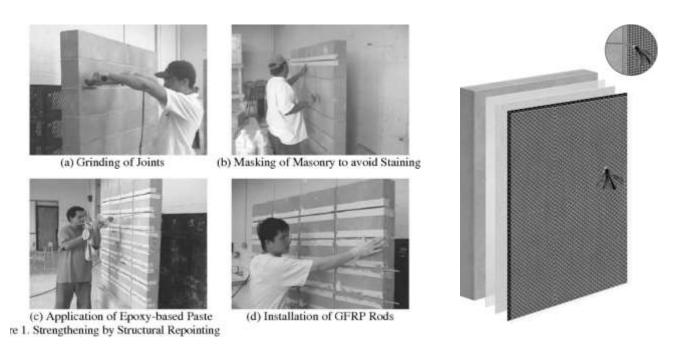


Figure I 17 Strengthening of Masonry Walls using FRP Structural Repointing

I.7.1.1.3 Fabric reinforced cementitious matrix (frmc)

Emerges as an alternative reinforcing technology for improving the mechanical characteristics of masonry buildings against seismic events. Fabric Reinforced Cementitious Matrix (FRCM) is a composite material composed of a mesh embedded in an inorganic mortar matrix that evolved as an alternative to the organic matrix of FRP (Fibre Reinforced Polymers). Because of its lower hazardous emissions, higher fire resistance, water vapor permeability, compatibility with inorganic substrates, and removability capability. On the other hand, FRCM composites have two technical drawbacks that must be overcome: first, the high stiffness of commonly used synthetic fiber meshes makes energy dissipation against cyclic loading difficult, resulting in stress concentration on the existing structure; and second, obtaining these used synthetic fibers has a high environmental and financial cost.



Figure I 18 Fabric Reinforced Cementitious Matrix (FRMC)

I.7.2 External Reinforcement

I.7.2.1.1 Post-tensioning strengthening

The post-tensioning strengthening technique is based on applying external pressures to masonry structural elements in order to counterbalance some or all of the effects of external stresses.

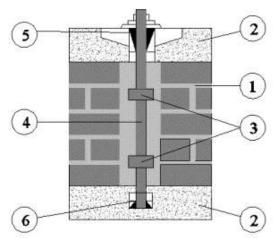
Strengthening using PT is very effective and cost-effective for big masonry walls and masonry dome structures, and it has been used successfully to enhance bending and shear resistance and reduce excessive deflections.

Post-tensioning in masonry provides a simple and possibly cost-effective structural method. Post-tensioning procedures may be used on a variety of masonry elements, including bonded and unbonded reinforcing walls that can be ungrouted, partially grouted, or completely grouted. When grout is used in the cells housing the post-tensioning (PT) bars in unbonded PT masonry walls, the PT bar is encased in a PVC tube and so is not

embedded in or bonded to the grout. An unbonded PT bar is intended to provide a restoring force to restore the wall to its original vertical alignment following a seismic event, hence eliminating residual drifts.

Externally or internally, the P-T strengthening method involves drilling vertical cores in the center of a masonry wall and inserting FRP tendons positioned inside a duct along the cores. FRP tendons are lightweight and strong, making them ideal for posttensioning applications. CFRP and aramid FRP are the most often used composite materials in P-T strengthening systems for masonry constructions.

The CFRP tendons feature fibers that are aligned in the longitudinal direction of the tendon, whereas aramid FRP tendons vary in strength according on the manufacturer.



1 - masonry; 2- reinforced concrete element; 3- threaded sleeve; 4 - FRP tendon; 5- stressing anchorage; 6- end of anchorage.

Figure I 19. Post-tensioning strengthening system

I.7.2.1.2 A steel ring-frame around the new opening

Certainly, steel frames are frequently selected over alternative brick wall strengthening solutions due to various advantages they provide. One of the primary benefits is their great reversibility, which means they may be quickly removed if necessary without causing harm to the existing brickwork. This is especially important in the case of historic buildings or structures that must be preserved.

Steel frames are also relatively easy to install, which can save time and labor costs compared to other techniques. Moreover, steel frames may give a high level of stiffness and strength without significantly increasing the self-weight of the structure, which is critical in buildings with weight limits or in seismic zones where excessive building weight can contribute to greater seismic loads.

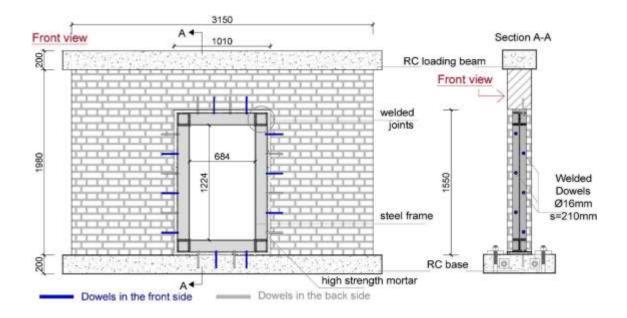


Figure I 20. steel ring-frame strengthening technique

I.7.2.1.3 The reinforced core technique

Is a strengthening method for masonry walls that involves adding vertical and/or horizontal reinforced concrete or steel columns within the core of the wall. This technique can be used to increase the load-carrying capacity of the wall and enhance its resistance to lateral loads, such as wind or seismic forces. To implement the reinforced core technique, vertical or horizontal holes are drilled into the masonry wall at regular intervals, and then reinforcing bars or steel columns are inserted into the holes and anchored into the surrounding masonry with grout or epoxy. The columns or bars are then connected at the top and bottom with steel plates or beams to create a rigid framework that reinforces the wall.

The reinforced core technique can be particularly effective in increasing the shear capacity of masonry walls, which is important in seismic design. This technique can also help mitigate the effects of cracking or spalling in the masonry by redistributing the load and reducing the stresses in the wall.

It's important to note that the reinforced core technique should only be implemented by a qualified contractor or structural engineer who has experience with this method. The proper design and installation of the reinforcement elements are critical to ensure the effectiveness and safety of the technique.

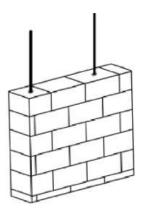


Figure I 21. The reinforced core technique

I.7.2.1.4 Tie rod strengthening

Is a type of structural element that is commonly used to provide lateral stability and support to masonry walls. It is essentially a steel rod or bar that is anchored into the masonry at both ends, and it is designed to resist tensile forces that can cause the wall to bow or bulge outward.

Tie rods are often used in pairs, with one rod running horizontally near the top of the wall and the other running diagonally from the top of the wall to a point near the base. The rods are usually connected to steel plates or anchors that are embedded into the masonry at each end, and they are tightened to a specified tension to provide the necessary support and stability to the wall.

The use of tie rods is particularly important in areas with high wind or seismic activity, as it can help to prevent masonry walls from collapsing or buckling under lateral loads. Tie rods can also be used to repair existing masonry walls that have become unstable or damaged over time.



Figure I 22. tie bars made of iron tension members

CHAPTER I MASONRY BIBLIOGRAPHIC RESEARCH

The retrofitting techniques used for masonry walls in the italian code ATC18

Fiber Reinforced Polymers Near-Surface Mounted Steel reinforcement Grout injection Traditional techniques Reinforced concrete jackets (FRP) (NSM) reinforcement This technique involves the NSM reinforcement involves Grout injection involves The italian code also FRP composites can be This technique involves the application of reinforced the insertion of steel bars or drilling holes into the traditional recognizes applied to the surface of the installation of steel frames, concrete layers to the exterior FRP strips into grooves that masonry walls and injecting retrofitting techniques such as masonry walls in the form of plates, or strips that are of the masonry walls to are cut into the surface of the grout or other materials into the use of steel tie rods, sheets or strips to increase the anchored to the masonry walls improve their strength and masonry walls and then filled the holes to fill voids and traditional masonry wall's strength and ductility. to provide additional support -stiffness. The concrete jackets with epoxy. This technique improve the wall's strength -techniques such as FRP can be particularly useful and strengthen the structure. are typically applied in can improve the wall's and stiffness. This technique buttressing, and the use of for strengthening masonry The steel reinforcement can multiple layers and can be flexural and shear strength can be used to increase the lime-based mortars walls that have limited space be applied horizontally or used to increase the wall's and can be particularly useful wall's shear strength and improve the strength and or access for other retrofitting vertically and can be used in resistance to both seismic and for walls with limited space or resistance to lateral loads. durability of the masonry techniques. conjunction with other non-seismic loads. access. walls. retrofitting techniques.

Figure I 23. the retrofitting techniques

I.8 CONCLUSION

In chapter 1 of the masonry bibliographic research, various aspects related to material properties and the assembly of masonry were discussed. The chapter covered topics such as the properties of masonry units and mortar, as well as the mechanical deterioration of masonry due to external and internal factors. Additionally, and we explored the estimation of mechanical properties of masonry, focusing on the italian code ntc18.

Moving forward, also we delved into masonry building behaviors, specifically emphasizing the domain of vulnerability modeling and seismic behavior mechanisms. The chapter touched upon the seismic analysis technique known as pushover analysis, providing an explanation for its utilization in the field. Furthermore, and introduced the concept of strengthening masonry structures, including techniques such as surface treatment and external reinforcement.

By investigating these diverse aspects, chapter 1 laid the foundation for a comprehensive understanding of masonry, enabling further exploration and analysis in subsequent chapters. The acquired knowledge will prove invaluable in comprehending the behavior and performance of masonry structures, ultimately contributing to the advancement of research and practices in this field.

CHAPTER II TREMURI MODELLING

II.1 INTRODUCTION:

3muri program is intended for nonlinear, pushover, and static analysis of masonry and mixed-material structures. 3muri employs a novel calculation approach (equivalent framework method "EFM") that can offer more information on the structure's real behaviour in terms of seismic stresses. The approach entails dividing the entire structure into macro-elements in order to determine the equivalent frame. 3muri provides a drawing area for structure insertion, an interface for selecting the calculation model and its answers, and a post processor for presenting the findings by showing the evolution of the building's state. During the push analysis, a calculation report is generated.

The reference seismic code is: seismic: Eurocode 8, and static: Eurocode 6

The program 3muri is a software created to execute the following analysis on masonry buildings:

- · Non-linear static seismic analysis
- · Analysis of vertical loads
- ·Kinematic analysis of masonry elements
- ·Local verification of structural and non-structural elements
- ·Management tool for retrofits on the structure

II.2 MACRO-ELEMENT MODELLING:

Micro-scale models and macro-scale models can be used to categorize the precise structural models utilized in simulation-based methodologies (calderini et al., 2009). The structure is discretized into finite elements in the micro-scale models, while the material level constitutive models are inelastic. Masonry piers and spandrels are modelled with force-deformation relationships at the structural member level in the macro-scale models, which discretize the structure into an equivalent frame model with main structural elements. The usage of micro-scale models is mostly restricted to the prediction of the behaviour of specific structural components (such as piers or spandrels) and the validation of the structural level accuracy of the macro-models due to their large computational complexity and expertise requirements.

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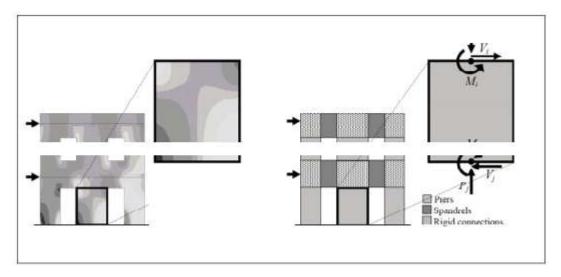


Figure II 1. Mef AND THE EFM

II.2.1 Macro-element approach:

Macro-element modelling is a numerical modelling approach in structural mechanics that uses enormous components to represent the behaviour of a complicated system. This method divides the structure into many macro-components, which are huge elements that comprise a major portion of the structure. Each macro-element is represented by a mixture of many sorts of simpler finite elements.

Macro-element modelling provides various benefits over other numerical modelling approaches, including a large reduction in the number of elements required to describe a particular structure, resulting in a significant reduction in computing time. Furthermore, for complicated structures such as reinforced concrete structures or complex metal structures, macro-element modelling can produce more precise and dependable results.

The design of a non-linear macroelement, representing a complete masonry panel, allows for the representation of a cinematic model describing deformation and damage mechanisms with a limited number of degrees of freedom. The macroelement proposed by gambarotta and lagomarsino is made up of three parts, which are depicted in the figure below. The two border sections 1 and 3, whose height is infinite, show a concentration of deformations caused by axial forces and flexion momentums. While at the middle 2 of height h, the concentrated effects are due to shear transversal forces.

To define the whole kinematic model of the macroelement, the three degrees of freedom of the nodes i and j corresponding to the interface of 1 and 3 must be considered. The following approximations can be used to simplify the kinematics of the following model:

U1 = ui et u2 = uj because the ends parts are infinitely stiff in shear.

 $W1 = w2 = \delta$ et $\phi 1 = \phi 2 = \Phi$ because the core section has infinite axial and bending rigidity.

With w and u the axial and transverse displacements; φ rotation; δ and Φ represent the axial displacement and rotation of the central body respectively.

A vector with eight degrees of freedom describes the kinematics; $A_T = \{ui \ wi \ \phi i \ uj \ wj \ \phi j \ \delta \ \Phi\}$

Which is set for each macroelement. Because the brick wall has a relatively low tensile strength, it is also important to represent the element overturning. A mono-lateral elastic contact between surfaces 1 and 3 is used to describe the overturning mechanism (lagomarsino et al., 2008b).

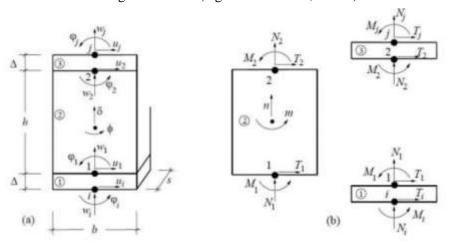


Figure II 2. Shema of macroelements taken from Lagomarsino et al (2008b)

II.2.2 Equivalent frame

The calculation code utilizes the EFM by macro elements approach to represent the masonry structure. This method enhances our understanding of seismic behaviour by dividing the structure into spandrels and piers. Each spandrel and pier are modelled as a unidirectional element, featuring rigid sections at the extremities and a deformable middle section to capture nonlinear characteristics. This approach

allows for a detailed analysis of the structural response and provides insights into the important nonlinear aspects of the masonry system.

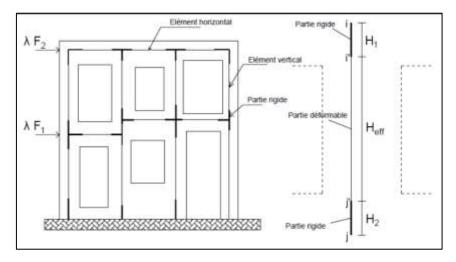


Figure II 3. Structure equivalent frame identification

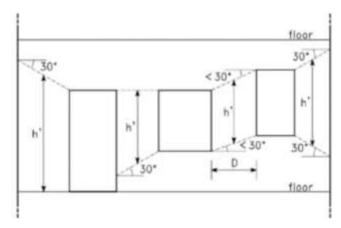


Figure II 4. Illustration of effective height identification method Taken from Dolce (1991)

$$H_{Eff} = H' + \left(\frac{1}{3}\right) \frac{D(\overline{H} - H')}{H'}$$

Definition of the effective height of the masonry walls (dolce, 1989).

Ultimate displacement of the reinforcement frame:

The yield and ultimate displacements of the frames are calculated using the expressions of the relative rotation capacity reported in circular no. 7 of 21 January 2019 (expressions (c8.7.2.7a) and (c8.7.2.1) respectively).

Strength of the reinforcement frame:

The resistance of the frame in the horizontal direction t is calculated using the relation:

$$T = \frac{2M}{h}$$
 In which:

M is the resistance to limb

H is the height of the frame

It is verified that this resistance does not exceed the maximum shear strength assessed according to the indications of the ministerial decree of 17.1.2018 (expression (4.1.29)).

Rigid elements at the ends, also known as rigid nodes, are intact components that convey vertical loads and inertial forces to the core section. The irregularity of the openings occasionally causes uncertainty in defining the effective height of the trumeau. Dolce (1991) provided a technique for determining the effective height that assumes a maximum inclination of 30° of the cracks from the corners of the openings, ensuring a steady rise in the height of the exterior pillars with regard to the dimensions of the opening. This approach was utilized in the creation of 3muri software; it handles the problem of irregular apertures as well as determining the effective height of an exterior pillar.

II.2.3 Structural element behaviour

After modelling the walls in an equivalent frame, it is essential to examine the behaviour of each element in order to derive the overall reaction of the structure. Masonry is the assembling of mortar and bricks, which results in a non-linear behaviour due to the intrinsic properties of the materials. The 3muri computation program employs a kind of basic and non-linear modelling of the elements to arrive at a result in terms of stiffness, resistance, and final displacement capacity.

To get reliable results of the structure's behaviour, as predicted by the capacity curve (force-displacement), it is necessary to consider the various ways of probable rupture of the macro-elements; there are two types of rupture for the trumeaux:

- 1) inflectional, which takes the shape of swinging rupture and.
- 2) shear, which manifests as sliding failure and diagonal tensile failure.

These forms of behaviour are fundamentally revealed in the center section by modelling the wall using macro-elements. Because of the multiple stress states that operate on them, a wall made of macro-elements might exhibit distinct failure behaviours for each partition. The axial force applied to a trumeau is important since it enables the collapse process to be identified. During the push analysis, an increase in horizontal load causes a redistribution phenomenon. As a result, depending on the progress of the nonlinear static analysis, the vertical load might assume different values for each trumeau. The maximum displacement must therefore be determined since beyond this value, the shear wall loses its resistance.

The identification of a macroelements failure process is thus dependent on the geometry of the panel, the intensity of the axial stress, and the mechanical properties of the material utilized. It should be emphasized that the forces only act at the node level. The shear and bending stiffness determine the elastic branch (the inclined section of the capacity curve). It is derived mostly from the shear's geometric and mechanical characteristics.

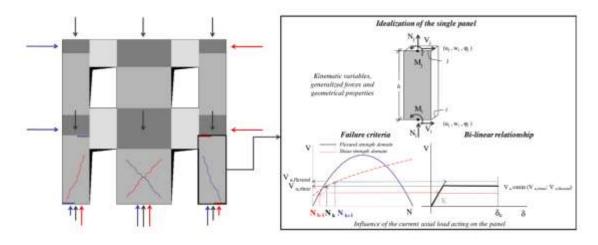


Figure II 5. Identification of failure modes for a microelement Taken from (Sergio Lagomarsino, 2013)

II.2.4 The structure's three-dimensional assembly

According to (Sergio Lagomarsino, 2013), some assumptions about the behaviour of the structure and the earthquake must be introduced into 3d modelling of masonry structures. Only when the structural parts are appropriately integrated in such a manner that the structure acts like a box can a complete reaction to earthquakes be achieved. In order to construct the many structural parts of a structure, a global coordinate system must be defined. The walls are defined by coordinates and the angle between the x axis and the plane of the wall. The equivalent framework approach was used to represent the walls. Lintels and macroelements are the two main types of elements.

A global cartesian coordinate system (x, y, z) is defined in order to create a 3d model. The coordinates of one point and the angle established with the global x axis are used to identify the wall vertical planes. In this manner, the walls may be represented as plane frames in the local coordinate system, while internal nodes can remain 2-dimensional nodes with 3 degrees of freedom. Three-dimensional nodes are utilized in corners and where two or more walls cross. They have 5 degrees of freedom (D.O.F.) In the global coordinate system (ux, uy, uz, ox, oy). Due to the membranous behaviour used for walls and floors, the rotating degree of freedom around the vertical z axis may be neglected.

These nodes may be created by assembling 2d stiff nodes acting in each wall plane and projecting the local D.O.F. Along global axes. The assemblage is then obtained by condensing the degrees of freedom

of two 2-dimensional nodes and assuming full coupling among the connected walls. This technique is highly effective for reducing the total number of D.O.F. And performing nonlinear analyses with a reasonable processing effort, even in the case of big and complicated building models.

Because the 2d nodes have no degrees of freedom along the orthogonal direction to the wall plane, the nodal mass component related to out-of-plane degrees of freedom is shared with the corresponding degrees of freedom of the two nearest 3d nodes of the same wall and floor.

This technique enabled the adoption of simplification hypotheses in the development of static studies with three acceleration components along the three primary directions and 3d dynamic analyses with three simultaneous input components.

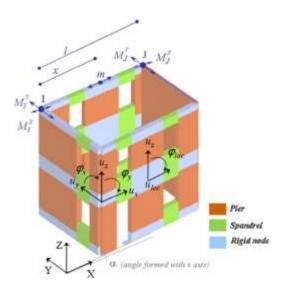


Figure II 6. 3D assembling of masonry walls: classification of 3D and 2D rigid nodes and out-of-plane mass sharing. (Sergio Lagomarsino, 2013)

II.3 MODELLING MASONRY PIERS AND SPANDRELS

A non-linear beam element model has been implemented in 3muri for modelling masonry piers and spandrels. Its main features are:

Initial stiffness given by elastic (cracked) properties;

Bilinear behaviour with maximum values of shear and bending moment as calculated in ultimate limit states;

Redistribution of the internal forces according to the element equilibrium;

Detection of damage limit states considering global and local damage parameters;

Stiffness degradation in plastic range;

Ductility control by defining maximum drift (δu). The maximum drift can be different for shear or axial bending. The regulations provide for different limit values depending on the failure type.

$$\mathcal{S}_{\mathbf{m}}^{\mathrm{DI}} = \frac{\triangle_{\mathbf{m}}}{h_{\mathbf{m}}} = \mathcal{S}_{u}$$

Element expiration at ultimate drift without interruption of global analysis.

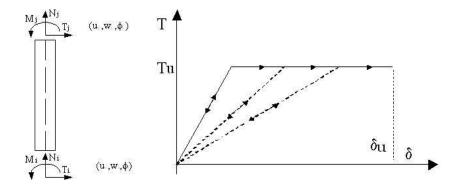


Figure II 7. Element BEHAVIOUR CURVE

Non-linear beam degrading behaviour

The elastic behaviour of this element is given by:

$$\begin{cases} Ti \\ Ni \\ Mi \\ Tj \\ Nj \\ Mj \end{cases} = \begin{bmatrix} \frac{12EJ}{H^3(1+\psi)} & 0 & -\frac{6EJ}{H^2(1+\psi)} & -\frac{12EJ}{H^3(1+\psi)} & 0 & -\frac{6EJ}{H^2(1+\psi)} \\ 0 & \frac{EA}{H} & 0 & 0 & -\frac{EA}{H} & 0 \\ -\frac{6EJ}{H^2(1+\psi)} & 0 & \frac{EJ(4+\psi)}{H(1+\psi)} & \frac{6EJ}{H^2(1+\psi)} & 0 & \frac{EJ(2+\psi)}{H(1+\psi)} \\ -\frac{12EJ}{H^3(1+\psi)} & 0 & \frac{6EJ}{H^2(1+\psi)} & \frac{12EJ}{H^3(1+\psi)} & 0 & \frac{6EJ}{H^2(1+\psi)} \\ 0 & -\frac{EA}{H} & 0 & 0 & \frac{EA}{H} & 0 \\ -\frac{6EJ}{H^2(1+\psi)} & 0 & \frac{EJ(4+\psi)}{H(1+\psi)} & \frac{6EJ}{H^2(1+\psi)} & 0 & \frac{EJ(2+\psi)}{H(1+\psi)} \end{bmatrix} = \begin{pmatrix} Ui \\ Wi \\ \phi i \\ Uj \\ Wj \\ \phi j \end{pmatrix}$$

Where

$$\psi = 24(1+v)X\left(\frac{H}{H}\right)^2 = 24\left(1 + \frac{E - 2G}{2G}\right)1.2\frac{B^2}{12H^2} = 1.2\frac{B^2}{12H^2}$$

The nonlinear behaviour is activated when one of the nodal generalized forces reaches its maximum value estimated according to minimum of the following strength criteria: flexural-rocking, shear-sliding or diagonal shear cracking.

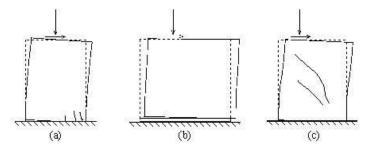


Figure ii 8.different types of failures (Raffaello, 2012)

Masonry in-plane failure modes: flexural-rocking (a), shear-sliding (b) e diagonal-cracking shear (c) (magenes et al., 2000)

II.4 STRENGTH AND FAILURE CRITERIA FOR URM PANELS IMPLEMENTED IN TREMURI PROGRAM

II.4.1 The failure modes

II.4.1.1 Bending ultimate moment

The resistance to compression bending can be evaluated by a parabolic curve which relates the normal stress and the ultimate moment, according to the hypothesis of material with no tensile strength. The ultimate bending moment is defined as:

$$M_{U} = \frac{L^{2}T\Sigma_{0}}{2} \left(1 - \frac{\Sigma_{0}}{0.85F_{M}} \right) = \frac{Nl}{2} \left(1 - \frac{N}{N_{U}} \right)$$

Where:

- -L is the length of the panel,
- -T is the thickness,
- $-\Sigma_0$ is the average compression tension
- -N is the axial compressive action (assumed positive in compression)
- -Nu is the maximum axial compressive action of the panel an it is equal to 0.85 fm l t

-Fm is the average resistance in compression of the masonry.

This approach is based on a no-tension material where a non-linear reallocation of the stress is performed (rectangular stress-block with factor = 0.85)

In existing building, the average resistance fm is to be divided by the "confidence factor" fc according to the structural knowledge level.

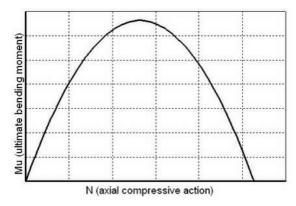


Figure II 9.Strength criterion in bending-rocking

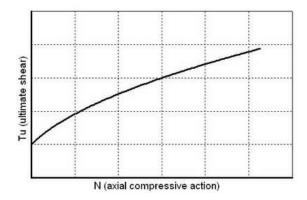
II.4.1.2 Shear turnšek and cačovic criteria

According to Italian code, only for existing building, the shear failure can be computed according to turnšek and cačovic criterion; the ultimate shear is defined as:

$$Vu = lt \frac{1.5T_0}{B} \sqrt{1 + \frac{\Sigma_0}{1.5T_0}} = lt \frac{F_T}{B} \sqrt{1 + \frac{\Sigma_0}{F_T}} = lt \frac{1.5T_0}{B} \sqrt{1 + \frac{N}{1.5T_0Lt}}$$

Where f_t and τ_0 are the design value of tension resistance in diagonal cracking of masonry and its shear value, b is a coefficient defined according to the ratio of height and length of the wall:

$$B = \begin{cases} 1.5 & \frac{H}{L} > 1.5 \\ \frac{H}{L} & 1 \le \frac{H}{L} \le 1.5 \\ 1 & \frac{H}{L} < 1 \end{cases}$$



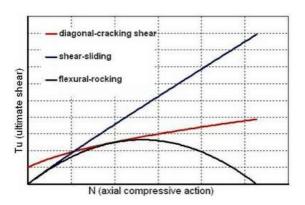


Figure ii 10. Turnšek and cačovic shear strength and strength criteria comparison

II.4.2 Strength criteria

Table ii 1. Strength criteria for urm panels implemented in tremuri program (Sergio Lagomarsino, 2013)

Failure mode and element type			Strength domain	Note	
		Piers	$M_{U} = \frac{Nl}{2} \left(1 - \frac{N}{0.85 F_{U} Lt} \right)$	Fu masonry compressive strength, l length of section, t thickness	
Rocking/crushing		Spandrels	$\begin{aligned} M_{U} &= \frac{Dh'p}{2} \bigg[1 - \frac{H'P}{0.85F_{Hu}Dt} \bigg] \\ Mu &= f(N, \frac{F_{Tu}}{F_{Hu}}Uc, Ut) \\ F_{Tu} &= min\left(\frac{F_{Bt}}{2}; c + U\Sigma_{S}\Phi\right) \end{aligned}$	H'p is assumed as the maximum value between the axial load n acting on spandrel and hp. Hp is the minimum value between the tensile strength of elements coupled to the spandrel (such as r.c. Beam or tierod) and 0.4fhudt, where fhu is the	
	Bed		$V_{U,bjs} = L'Tc + UN \le V_{U,blocks}$	compression strength of masonry in horizontal direction, the limit domain	
	joint sliding	Spandrels	$V_U = htc$	is obtained by assuming an elasto- perfectly plastic constitutive law with limited ductility both in tension (ut) and compression (uc) and an	
Shear	Diagonal cracking	Piers / spandrels	$V_{U.dc_{-1}} = lt \frac{1.5T_0}{B} \sqrt{1 + (\frac{1}{1.5T_0Lt})}$ $V_{U.dc_{-2}} = \frac{1}{B} (Lt\hat{c} + \hat{u}n) \le V_{U,block}$	equivalent tensile strength for spandrel f _{tu} (f _{bt} tensile strength of bricks; land c friction coefficient and cohesion of mortar joint, respectively; φ interlocking parameter; σs entity of compressive stresses acting at the end-sections of the spandrel) Coulomb criterion with: l' length of compressed part of cross section. A limit value (v _u , blocks) is imposed to take into account in approximate way the failure modes of blocks, h height	

	of spandrel transversal section
	(assumed only in case of a strut-and-
	tie mechanism may develop)
	το masonry shear strength, b stress
	distribution factor as function of
	slenderness
	Coulomb-type criterion with: $\hat{\mathbf{u}}$ and $\hat{\mathbf{c}}$
	equivalent cohesion and friction
	parameters, related to the interlocking
	due to mortar head and bed joints,
	(with $b = 1$). The introduction of b , is
	implicitly justified by some
	comments on the shear stress
	distribution; a similar corrective
	factor is proposed

The calculation procedure is based on the comparison between the as installed and the as designed (introduction of a new opening).

The expression <u>"as installed"</u> means the schematization of the entire wall <u>before</u> the opening is made.

The expression <u>"as designed"</u> means the schematization of the entire wall <u>after</u> the opening has been made.

The comparison is made with respect to the variations of: · resistance of the wall system

- \cdot Stiffness of the contained wall system (at the regulatory level there is no limit to this variation, alternative technical documentation suggests \pm 15%)
 - · Deformation work, representative of the overall behaviour of the wall

The identification of the stiffness, strength and deformation work of the wall is carried out by calculating the contribution of the individual elements.

The mechanical characteristics of the individual elements can be calculated with the following formulations:

Table II 2. The MECHANICAL CHARACTERISTICS OF STEEL FRAMES IMPLEMENTED IN TREMURI PROGRAM

	Strength domain	Note
Stiffness	$K_{T} = \frac{12e j}{H^{3}}$	E: elastic modulus of the upright of
Resistance	$V_{T} = \frac{2F_{Yk}W}{\Gamma_{M}H}$	the steel frame J, w: modulus of inertia and modulus of resistance
Elastic limit displacement	D_{Y} . telaio $= \frac{V_{Telaio}}{K_{Telaio}}$	H: height of the upright

Table II 3. The MECHANICAL CHARACTERISTICS OF WALL PANEL IMPLEMENTED IN TREMURI PROGRAM

	Strength domain	Note
Stiffness	$K_{M} = \frac{G l t}{1.2 h} \cdot \frac{1}{1 + \left(\left(\frac{1}{1.2}\right) \frac{G}{E} \left(\frac{H}{L}\right)^{2}\right)}$	
Shear resistance	$V_{M} = l t \frac{Q.5T_{0}}{B} . \sqrt{1 + \frac{\Sigma_{0}}{1.5T_{0}}}$	
Axial bending resistance	$D_{Mpf} = \frac{P t \Sigma_0}{H} \left(1 - \frac{\Sigma_0}{0.85. F_M} \right)$	E, g: elastic modules H, l, t: height, length and thickness of the panel
Elastic limit displacement assuming vt=min (vmt, vmpf)	$D_Y + V_T/K_M$	the paner
Ultimate displacement of a wall panel that is in crisis due to shear	$D_{\rm U} = 0.005 {\rm h}$	
Ultimate displacement of a wall panel that is in crisis due to axial bending	$D_{U} = 0.01 h$	

II.5 WALL MODELLING

Dividing the wall into vertical areas which correspond to the various levels, and noting the location of the openings, the portions of masonry, masonry piers, and spandrel beams, where deformability and damage are concentrated, can be determined. This can be verified by observing the damage caused be real earthquakes, and with experimental and numerical simulations. These areas are modelled with finite two-dimensional macro-elements, which represent masonry walls, with two nodes and three degrees of liberty per node (ux, uz, roty) and two additional internal degrees of liberty.

The resistant portions of the wall are considered as rigid two-dimensional nodes with finite dimensions, to which the macro-elements are connected. The macro-elements transfer the actions along the level's three degrees of liberty, at each incident node. In the description of each single wall, the nodes are identified by a pair of coordinates (x, z) in the level of the wall. The height, z, corresponds to that of the horizontal structures. The degrees of liberty are solely ux, uz, and roty (for two-dimensional nodes).

Thanks to the division of elements into nodes, the wall model becomes completely comparable to that of a frame plan.

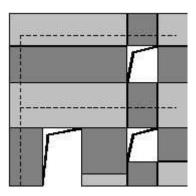


Figure II 11. The DIVISIONS OF WALL FRAME

During assembly of the wall, the possible eccentricities between the model nodes and the ends of the macro-elements are considered. Given the axes that are the center of mass for the elements, these cannot coincide with the node. Hence in the rigid blocks, it is possible that eccentricity may be found between the model node and that of the flexible element.

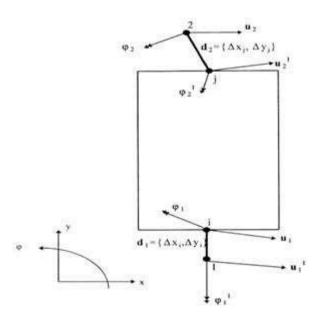


Figure II 12. Wall MODEL NODES AND THE ECCENTRICITIES

Structural modelling also requires the possibility of inserting beams, (elastic prisms with constant sections), identified in the level by the position of the two edge nodes. Once the length (prevalent dimension), the area, the inertial moment, and the elastic module are known, it is possible to reconstruct the rigidity matrix, applying elastic joint rules, and assuming that they remain indefinitely in the elastic field, the normal formulation of elastic joints are applied (petrini, et al., 2004; corradi dell'acqua, 1992).

In addition to the presence of actual beams (architraves or r.c. Tie beams), the model assumes the presence of tie rod structures. These metallic structures completely lack bending rigidity and lose all effectiveness if they are compressed. This detail adds an additional nonlinear element to the model. The total rigidity of the system must decrease if a stretched tie rod is compressed, and it must increase in the opposite case.

Another characteristic of these elements is the possibility to assign an initial deformation $\epsilon 0$, which determines a force fc= ea ϵ_0 . From a static point of view, once the overall vector of the precompression forces fc is determined, it is enough to apply it to the structure as if it were an external load.

The rigidity matrix for elements without bending rigidity is easily found by eliminating all the limits that contain j from the element matrix. To manage the non-linearity, all of the elastic contributions due to the tie rods must be kept distinct. At each step, it must be verified if the tie rod that previously was stretched is now compressed or vice versa. If the situation changes, the total rigidity matrix for the model must be corrected. (Raffaello, 2012)

II.6 SPATIAL MODELLING

In spatial modelling, the walls are resistant elements, with regards to vertical and horizontal loads. On the other hand, the horizontal structures (floors, vaults, ceilings) transfer their vertical loads to the walls and divide the horizontal actions onto the incident walls. In this way, the structure is modelled by assembly of the level structures: the walls and the horizontal structures, both lacking bending rigidity outside of the level.

The procedure for modelling macro-elements for masonry walls which receive forces from their own level was illustrated above. This instrument constitutes an important starting point for modelling of the overall behaviour, based on the behaviour of the walls on their level. In any case, extension of the procedure to three-dimensional modelling is not simple. The correct strategy is that of conserving the modelling of the walls on their level and assembling them with the horizontal structures, including those for which the membrane behaviour is modelled. In this way, the model of the structure takes on mass and rigidity on all of the three-dimensional degrees of liberty. At the same time, it locally takes into account the individual degrees of liberty of the levels (two-dimensional nodes).

In this way, an essential structural model is created, without adding the complication of computation of the response outside of the local level. This can of course be verified later. Once a single overall reference is established for the structural model, the local references are introduced for each wall. It is assumed that the walls rest on the vertical plane and they are found in the plan of the generic wall i through the coordinates of a point, the origin of the local reference oi (xi, yi, zi), with respect to an overall cartesian reference system (x, y, z).

The angle i is computed with respect to axis x.

In this way, the local reference system for the wall is unambiguously defined and the macroelement modelling can take place with the same modality used for the levels.

Macro-elements, such as beams and tie rods, maintain the behaviour of the level and do not require reformulation.

Connection nodes, belonging to a single wall, maintain their degrees of liberty at the local reference level. Nodes that belong to more than one wall (localized in the incidences of the walls) must have degrees of liberty in the overall reference (three-dimensional nodes). These nodes, due to the hypothesis that ignores the bending rigidity of the walls, do not need a rotational degree of liberty around the z axis, as they are not connected to any element able to provide local rotational rigidity limits. Three-dimensional rigid nodes, representing angle iron or hammer situations, are obtained as an assemblage of virtual two-dimensional rigid nodes identified in each of the incident walls. These have displacement components generalized using

five degrees of liberty: three displacement ux, uy and uz. Two rotational ϕ x and ϕ y. The relationships between the five displacement and rotation components of the three-dimensional node and the three for the fictitious two-dimensional node, belonging to the single wall are given by:

$$\begin{cases} U = U_X Cos\theta + U_Y Son\theta \\ \Omega = U_Z \\ \Phi = \Phi_X Sin\theta - \Phi_Y Cos \Theta \end{cases}$$

In which u, w, and φ indicate the three displacement components according to the degrees of liberty found in the fictitious node that belongs to the generic wall facing the plan according to angle φ . Similarly, the forces applied to the three-dimensional nodes are displaced according to the directions identified by the middle level of the walls and then applied to the macro-elements in their level of resistance.

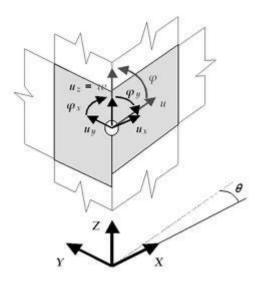


Figure II 13. Components DISPLACEMENTS ACCORDING TO DOF

The reactive forces transmitted by the macro-elements that belong to the individual walls to the fictitious two-dimensional nodes are carried over to the overall reference based on

$$\begin{cases} F_X = F_H^1 \text{Cos}\Theta_1 + F_H^2 \text{Cos}\Theta_2 \\ F_Y = F_H^1 \text{Son}\Theta_1 + F_H^2 \text{Son}\Theta_2 \\ F_Z = F_V^1 + F_V^2 \\ M_Y = -M^1 \text{Cos}\Theta_1 - M^2 \text{Cos}\Theta_2 \end{cases}$$

In which, as seen in the figure, the boundaries with apex 1 and 2 respectively make reference to the force limits corresponding with the virtual nodes identified in the walls 1 and 2 to which the three-dimensional node belongs.

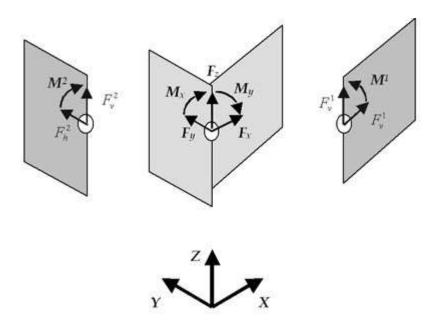


Figure II 14. The FORCES TRANSMITTED BY THE MACRO-ELEMENTS

In this way, modelling of the wall can take place on the level, recovering that described in the preceding chapter. The nodes that only belong to a single wall remain two-dimensional. They maintain only three degrees of liberty, rather than five.

The floors, modelled as finished orthotropic membrane three-node elements, with two degrees of liberty per node (displacements ux and uy), are identified with a warping direction, with respect to that characterized by an elastic module e1. E2 is an elastic model with a direction perpendicular to the warping, while v is the poisson coefficient and g2,1 is the elasticity tangential model. E1 and e2 represent the degree of connection that the floor, thanks to the effects of the tie beams and tie rods, exercises on the element nodes on the level of the wall. G2,1 represent the shear rigidity of the floor on its level and the division of the actions among the walls depends on this.

It is possible to position a floor element connecting it to the three-dimensional nodes. This is because the floor element functions principally to divide the horizontal actions between the various walls in proportion to their rigidity and its own. In this way it makes the model three-dimensional in a way that brings it close to the true structural performance.

The finished reference element to be considered is the level element, in a level state of tension, with three nodes.

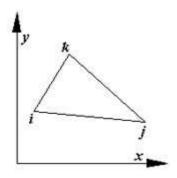


Figure II 15. The REFERENCE ELEMENT

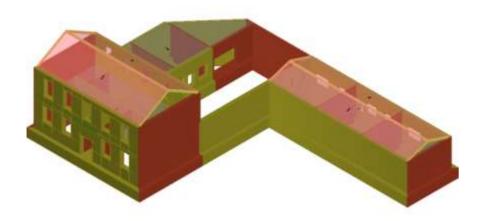
The rigidity matrix involves the individual three-dimensional incidental nodes on the floor. The contribution of the vertical loads, self or borne, is attributed in terms of nodal mass added to all the nodes, including those with three degrees of freedom, that belong to the incident walls at the height of the level of the floor. This added mass is calculated based on the area of influence of each node, taking into account the warping direction of the floor. (Raffaello, 2012)

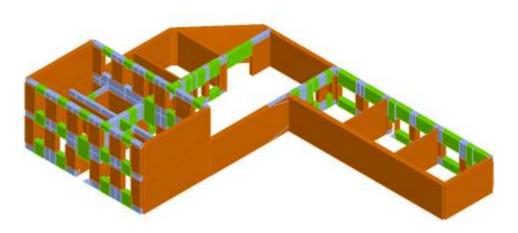
CHAPTER II

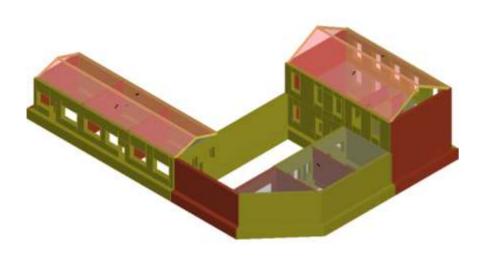
TREMURI MODELLING

II.7 THE STRUCTURE AFTER MODELLING

The masonry structure was effectively modelled using the macro element method. Through successful meshing and division into equivalent frames, including spandrels and piers, the analysis captured the structure's behaviour accurately. This approach offers advantages in terms of efficiency and accuracy, providing valuable insights into the structural response and facilitating targeted evaluations for strengthening or rehabilitation purposes.







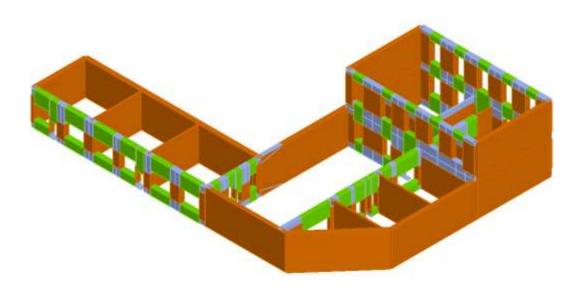


Figure II 16 3D VIEW OF THE BUILDING AFTER MODELLING AND THE MACROELEMENTS STRUCTURE MECH

II.8 CONCLUSION

Chapter II of the Masonry Bibliographic Research delves into tremuri modelling, focusing on different approaches and techniques. The chapter covers macro-element modelling, including the macro-element approach and the concept of an equivalent frame. It also explores the behaviour of structural elements and the three-dimensional assembly of masonry structures.

Further discusses the modelling of masonry piers, spandrels, and walls. It highlights the importance of considering spatial modelling to accurately represent the three-dimensional nature of masonry structures.

Additionally, addresses the strength and failure criteria for unreinforced masonry (URM) panels implemented in the Tremuri program. It examines various failure modes and strength criteria, providing insights into the structural behaviour of URM panels.

Overall, Chapter II provides valuable information and techniques for modelling tremuri, enabling researchers and practitioners to analyse and design masonry structures more effectively, particularly in seismic contexts. It offers advanced capabilities such as seismic analysis, pushover analysis, vulnerability assessment, and performance evaluation. With Tremuri, engineers can accurately model the behaviour of masonry buildings under seismic loads, assess their vulnerability to earthquakes, and evaluate their performance based on various criteria. The software provides visualizations and reporting features to effectively communicate analysis results. Overall, Tremuri is a valuable resource for engineers involved in the seismic assessment and design of masonry structures.

III.1 INTRODUCTION

Annaba is a city in northeastern algeria close to the mediterranean sea. The city has a long history, with human occupancy reaching back to ancient times. Annaba's beautiful masonry structures are one of its most noticeable attractions. Overall, annaba's masonry structures reflect the city's rich history and cultural legacy. They serve as a reminder of the great workmanship and architectural brilliance of those who created them, and they continue to astonish and inspire visitors to the city.

Here are 10 outstanding examples of masonry architecture in annaba:

- St. Augustine basilica this great church, built in the late nineteenth century, combines byzantine and romanesque architectural elements. The façade of the basilica is ornamented with exquisite brickwork, while the inside features stunning vaulted ceilings and brilliant stained-glass windows.
- Palace of the bey built in the 18th century, this palace served as the residence of the local ruler.
 The building's exterior is clad in beautiful masonry and mixes french, ottoman, and islamic style features. The inside is lavishly adorned with ornate furniture and magnificent tilework.
- La gare d'annaba built in the early twentieth century, this train station exhibits a unique combination of french and islamic architectural elements. The façade of the station is distinguished by its red brickwork and ornate masonry.
- St. Jean baptiste church built in the early twentieth century, this church combines neo-gothic and romanesque architectural styles. The outside of the structure is clad in granite and has a big rose window and a high bell tower.
- Sidi bou merouane mosque built in the 14th century, this mosque combines andalusian, moorish, and ottoman architectural elements. The front is distinguished by beautiful brickwork, while the inside features magnificent tilework and decorative ornamentation.
- St. Augustine's college built in the early twentieth century, this structure combines french and
 islamic architectural elements. The outside of the building is distinguished by its red brickwork and
 exquisite masonry.
- St. Joseph's church built in the early twentieth century, this church combines neo-gothic and romanesque architectural styles. The outside of the structure is clad in granite and has a high bell tower.
- The khelifa palace was built in the 18th century and served as the residence of the local governor.
 The exterior is clad in beautiful masonry and displays a blend of french, ottoman, and islamic style elements.

• Dar el hamra - this ancient edifice originates from the 18th century and was formerly the home of a wealthy merchant. The exterior of the building is adorned with elaborate masonry, while the inside is adorned with beautiful tilework.

 Governor's palace - built in the early twentieth century, this palace functioned as the local governor's house. The building's exterior is clad in elaborate masonry and shows a combination of french and islamic architectural elements.

These masonry buildings are only a small sample of the stunning architecture found throughout annaba. They serve as a tribute to the skill and inventiveness of the individuals who created them, as well as to the city's rich history and heritage of culture.

These structures exhibit a range of architectural styles, including byzantine, romanesque, gothic, and islamic, and are all examples of annaba's excellent masonry artistry.

III.2 STUDY CASE

III.2.1 Presentation of the asla hocine primary school

The elementary school "assela hocine" dates from the colonial era. It was erected in 1923 and is located in the city center, namely at the level of the anatole france- wheat market. It dates from the second phase of the colonial period, and it is the first secular, public school built on virgin ground within the second enclosure.





Figure III 1. main facade

III.2.2 Urban study

Although our intervention's field of action is confined to the building, it is critical to place it in its urban setting and define its interaction with its external environment in order to function within its boundaries.

III.2.2.1 Location and service of buildings

> The situation in relation to the city:

The project is located in the heart of downtown annaba at the wheat market -place anatole france.

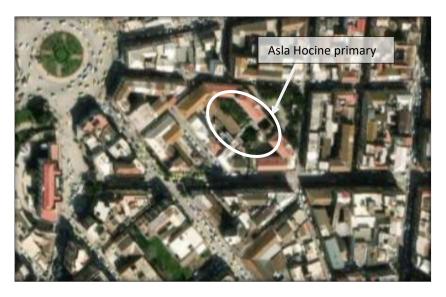


Figure III 2. mass grounding plan

III.2.2.2 Immediate environment



Figure III 3. situation plan

III.2.3 Architectural study

The architectural analysis allows for the listing of existing spaces and their potential for use, the comparison of the surfaces offered with the program's demands, the understanding of the layout of the places and their operation, and the projection of the new image by comparing it to the previous appearance.

III.2.3.1 Limits and accessibility

- North side: the street zanine el arbi and the elementary school of the same name.
- South side: assela hocine and the elementary school for girls.
- East side: the street al kods and the place anatole france.
- West side: djemaa saci street and the civil protection.

III.2.3.2 Implantation

III.2.3.2.1Siting types and structure dimensions

The elementary school is divided into three sections:

Table III 1 building block divisions

Bloc	Descriptions	Heights
(r+1) comprises the main entry haccess to the courtyard, the administration, the kitchen, the ground floor store, and a non-functional floor.		Ground floor height: 4.56 meters 1st story height: 9.1 meters Roof height: 11.96 meters
Block 2	Represents two classrooms and the restrooms. The courtyard is represented by the unbuilt portion.	Ground floor height: 5.1 meters
Block 3	Represents three separate classrooms.	Ground floor height: 4.26 meters Roof height: 6.2 7.x37 meters

III.2.3.2.2Dimension in plan

- Total length along the axis (y -y): 36.70 m.
- Total width along the axis (x -x): 42.8 m.

III.2.3.2.3Typology and plan

Dominant form: rectangular building (1 form)

Table III 2 . Divisions dimensions and openings

Space	Width (m)	Length (m)	Surface (m2)	Height (m)	Openings
Class1	7.015	5.815	40.79	5.1	(3.15*2) ;(1.45*3.41)
Class2	6.17	6.97	43	5.1	(1.38*2.75) ;(0.82*2) ;(0.82*2)
Class3	8.38	7.57	63.43	4.26	(1*1.85);(1*1.85);(0.65*2);(1*1.85);(2.8*2);(2.8*2)
Class4	7.85	7.335	57.579	4.26	(2.8*2);(0.97*2) ;(2.14*2)
Class5	7.85	7.335	57.579	4.26	(2.80*2);(0.97*2) ;(2.16*2)
1st floor	17.485	9.455	165.32	4.18	5 openings on each side (147*275)
Director's office	5.89	7.355	43.32	4.56	(1.5*2.5)
Director's office ancient	7.345	6.117	44.92	4.56	(1.5*2.5)
Store	4.42	2.35	10.387	4.56	(1*2.35)
Canteen	2.49	2.35	5.85	4.56	
Toilet	1.18006d	0.89	1.05	5.1	(4*2.84)
Courtyard	13.83	7.56	104.55		
Galleries	19.38	10.345	200.486		
Entrance hall	5.96	2.44	14.54	4.56	

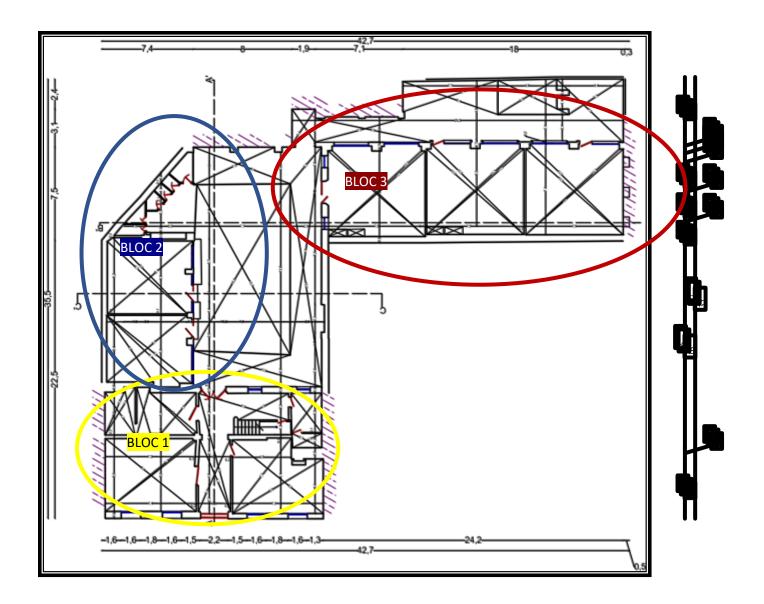


Figure III 4. ground floor plan and blocks divisions

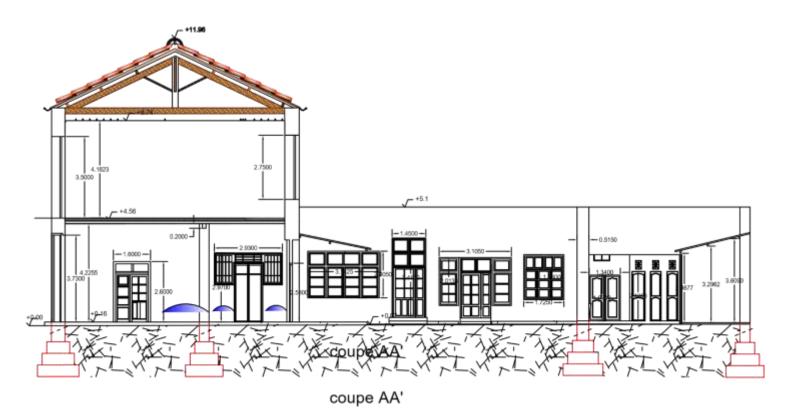
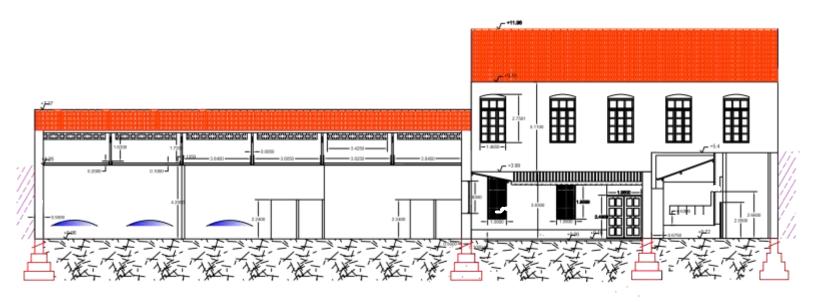


Figure III 5. architectural plan cut AA'



coupe BB'

Figure III 6. architectural plan Cut BB'

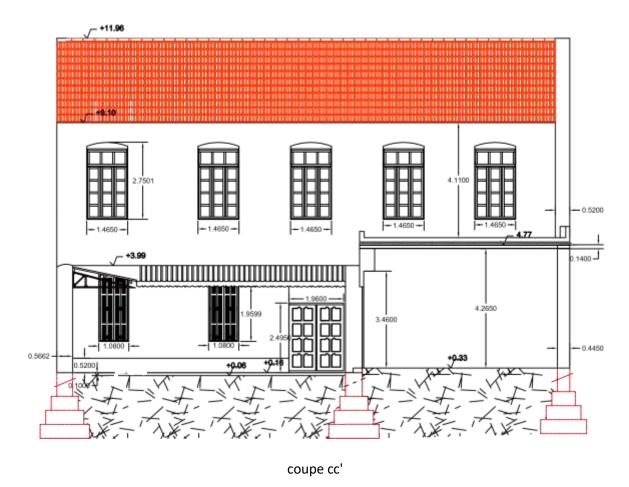


Figure III 7. architectural plan Cut CC'

III.3 STUDY CASE AND DIAGNOSIS

III.3.1 Constructive and structural analysis

A detailed comprehension of the structure of the building materials and building processes is required in order to evaluate its degree of conservation and offer an idea of its resistance to the various loads that this is of prior usage in the future.

The design of a civil engineering project is developed taking into account the functional aspects; structural and formal, which obliges the engineer to take into account the following data:

- the use of the building.
- resistance and stability.
- architectural, functional and aesthetic requirements.
- economic conditions.

III.3.1.1 Infrastructure

Access to infrastructure is an impossibility. We cannot recognise the sort of infrastructure; however, it is thought to have a continuous masonry foundation under walls.

III.3.1.2 Structure of the superstructure

The structure is made up of two major vertical and horizontal construction systems:

Table III 3. The structure elements

Element	Materials	Dimensions	
Vertical elements	- load-bearing wall: -rubble masonry wallsstones walls	-thicKNess ranging between 40 to 60 cm thicKNess of 40 cm.	
Horizontal elements	Brick floor + ipe metal	- thicKNess of 24.5 cm. (ipe 140)	
Roof	The roof is slanted (wood frame + tile) at the floor level	-frame wood dimensions and joists of (7*17cm) ;(7*25cm)	
Secondary system	Represent walls that do not contribute to load transmission but have the function of separating spaces, which made of bricks.	-thicKNess ranging between 10 to 23 cm.	



Figure III 8 . materials and architecture plan first floor

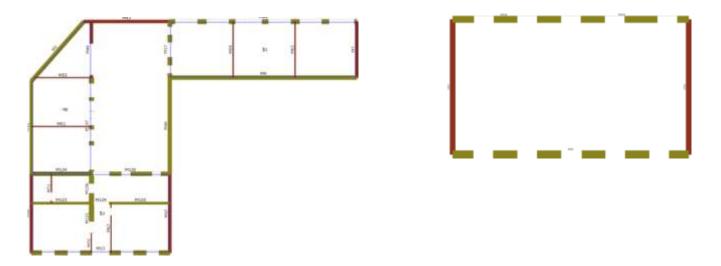
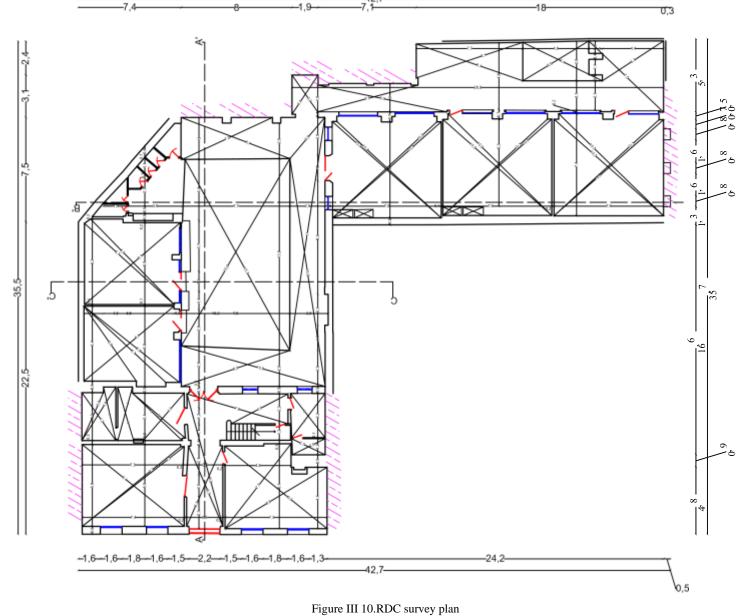


Figure III 9 material plan 1st floor and 2nd floor

Table III 4. The used material tables

Name	Туре	Colour	
C24 - en 338	Timber		En 338
Rubble	Masonry		
Stone	Masonry		
Bricks	Masonry		



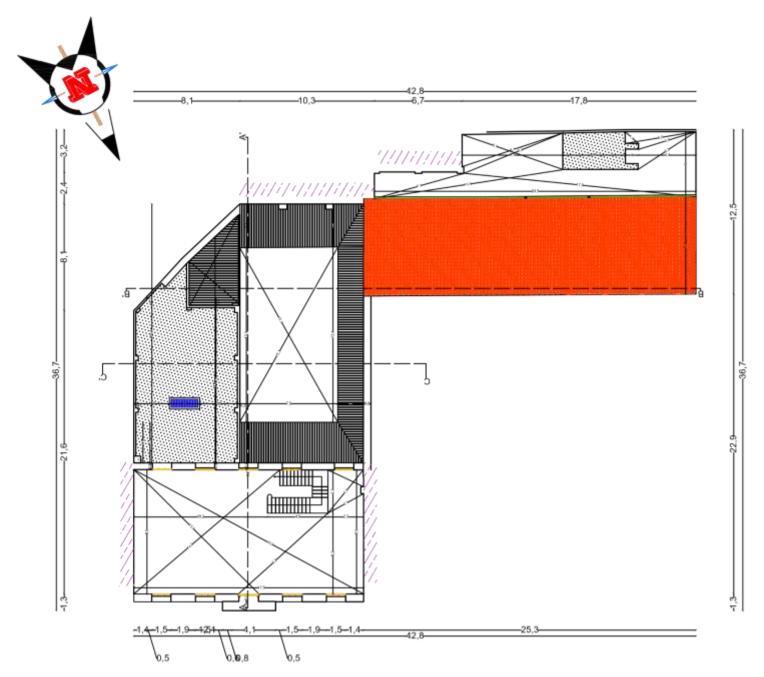


Figure III 11. 1st floor plan view

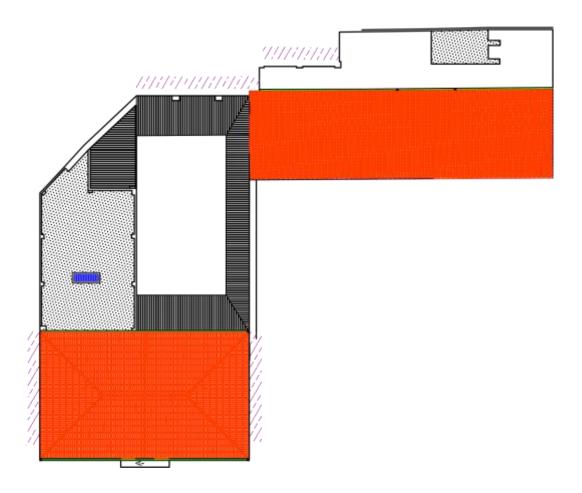


Figure III 12. Roof plan view

III.4 REFERENCE CODES

- Ntc 2018
- The algerian earthquake regulation "rpa" version 2003.
- Atc40
- Eurocode 8
- Eurocode 1
- Eurocode 6
- Fema 273, Fema 356

III.5 ACTIONS

III.5.1 Description of actions

The destination of the actions that will have to support the different floors of the building has been realistically designed in accordance with the writings of ntc 18 basis for structural calculation and eurocode 1: nf en 1991.1. Actions (2003-2008)

Loads classified by its nature can be distinguished between the direct actions include the self-weight of the structure, the rest of the dead loads, the operating overloads, etc.

The indirect actions consist of deformations or imposed accelerations capable of producing forces of indirect form. In this group there are the effects of settlement of foundations, rheological actions, seismic actions, etc.

According to the calculation rules, actions on structures can be classified into 3 different groups:

Permanent loads, operating loads and accidental loads (earthquake)

The characteristic value of an action is its main representative value. In general, for the proper weight of the structure, a unique value deduced from the nominal dimensions and the average specific weights will be adopted as characteristic action.

III.5.2 Permanent and variable loads

With regard to permanent and variable loads, the specific values of the Eurocode have been taken.

From the previous statements we go on to define the different actions that gravitate on the floors of each floor:

• The dead weight of the floors. The characteristic value of the self-weight of the elements constituting a building was determined on the basis of the average value obtained with the nominal dimensions and the average specific weights (an analytical method accepted by aeor-93).

Obtaining its value from these recommendations of various standards and instructions it should be mentioned that in some cases does not exist a single coating but more than one on top of the other) in these cases, the resulting wight have been taken into account.

Operating overload: the value recommended by the Eurocode has been taken.

Overload of small brick partitions: to calculate their weight, different thicknesses measured on each dwelling have been taken into account. Also, and on the safety side, the empty by full criterion was followed.

III.5.3 General evaluation of the actions

In the first place, the presentations in the italian ntc 18 and eurocodes instruction was taken as reference values for the permanent charges and operating charges.

The weights of the constituent elements of a construction were calculated analytically by using the integrated codes, wich are from national regulations.

In particular, we used the values provided by italian regulations (and european regulations in general) through known eurocodes and not the algerians dtr's.

Then we present in the table below some constructive elements that have been taken into account.

Table III 5 . Some materials propre weights

Materials	Proper weight
Steels	7850 kg/m3
Cast iron	7250 kg/m3
Aluminium	2750 kg/m3
Bronze	8600 kg/m3
Zinc	7200 kg/m3
Concrete flows	2200 kg/m3
Reinforced concrete	2500 kg/m3
Cedar wood	800kg/m3
Pine bowls	600 kg/m3
Colonial wood	1000 kg/m3
Wooden joists.	25/45 kg/m2
Hollow brick wall (perforated)	1500 kg/m3
Solid brick wall	1900 kg/m3
Rubble stone masonry	2100/2600 kg/m3
Solid brick partitions	120kg/m2
Hollow brick partitions	100kg/m2
Coatings	50/80 kg/m2

Large flat tile mold	80/85 kg/m2
Flat tile small mold	60/70 kg/m2
Flemish tile	80/100 kg/m2
Large mold flat tile	80/85 kg/m2
Corrugated asbestos cement tile	15/20 kg/m2
False ceiling	5/10 kg/m²

III.6 THE LOADS

Table III 6. Floor loads

No. Floor	Position	Gk1 [KN/m2]	Gk2 [KN/m2]	Qk [KN/m2]	Leading variable action 1	Ψ0	Ψ2
1	Level 1 (+4.630 [m])	1.85	1.34	1.00	No	1.00	0.70
2	Level 1 (+4.630 [m])	1.85	1.34	1.00	No	1.00	0.70
3	Level 1 (+4.630 [m])	1.85	1.34	2.50	No	1.00	0.70

Table III 7 . Balcony loads

No. Balconies	Position	Gk1 [KN/m2]	Gk2 [KN/m2]	Qk [KN/m2]	Leading variable action 1	Ψ0	Ψ2
1	Level (+9.100 [m])	2.67	1.34	1.50	No	1.00	0.70

Table III 8. Roof slope loads

Roof slope	Position	Gk1 [KN/m2]	Gk2 [KN/m2]	Qk [KN/m2]	Leading variable action 1	Ψ0	Ψ2
1	Level 1 (+4.630 [m])	0.70	0.00	1.00	No	1.00	0.70
2	Level 1 (+4.630 [m])	0.70	0.00	1.00	No	1.00	0.70
3	Level (+9.100 [m])	0.70	0.00	1.00	No	1.00	0.70
4	Level (+9.100 [m])	0.70	0.00	1.00	No	1.00	0.70

III.7 THE MECHANICAL CHARACTERISTICS

III.7.1 Masonry

Table III 9. Masonry element mechanical characteristics

Name	The material's condition	Constitutive law	E [KN/m2]	Eh [KN/m2]	G [KN/m2]	Specific weight [kg/m3]	Fm [KN/m2]
Bricks	Existing	Irregular masonry (turnsek/cacovic)	1,500,000.00	1,500,000.00	500,000.00	1,835	2,600.00
Rubble	Existing	Irregular masonry (turnsek/cacovic)	1,230,000.00	1,230,000.00	410,000.00	2,039	2,000.00
Stone	Existing	Irregular masonry (turnsek/cacovic)	870,000.00	870,000.00	290,000.00	1,937	1,000.00

The material's condition: existing

Constitutive law: irregular masonry (turnsek/cacovic)

Table III 10. Materials coefficients

Name	Fk [KN/m2]	T [KN/m2]	Cf	Гт
Bricks	1348.10	50.00	1.35	3.00
Rubble	1037.00	35.00	1.35	3.00
Stone	518.50	18.00	1.35	3.00

III.7.2 Timber

Table III 11. Timber mechanical characteristics

Name	E [KN/m2]	G [KN/m2]	Specific weight [kg/m3]	Fwm [KN/m2]	Fwk [KN/m2]	Γw
C24 - en 338	11,000,000.00	690,000.00	428	34,000.00	24,000.00	1.30

III.7.3 Steel

Table III 12 structural steel mechanical characteristics

Name	E [n/m2]	G [n/m2]	Specific weight [kg/m3]	Fym [n/m2]	Fyk [n/m2]	Гѕ
S 235 (t <= 40mm)	2.10e+11	8.08e+10	8.00e+03	2.53e+08	2.35e+08	1.05

III.7.4 Floors

Steel-beam and vault

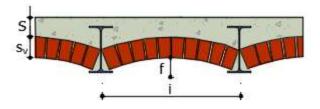


Figure III 13. Floor concept

Table III 13 . Floor dimensions

Name	Materials	Description
Vault	Steel: s 235 (t <= 40mm) Concrete: c8/10 Vaulted: brick	Steel-beam and vault Profile: ipe 140 I [mm] = 500; f [mm] = 100; sv [mm] = 70; a flat/m [mm2] = 0.00; s [mm] = 100

Table III 14. Floor mechanical characteristics

Archive	Elevation [m]	ThicKNess [mm]	G [KN/m2]	Ex [KN/m2]	Ey [KN/m2]	Mass loading	Туре
Vault	4.630	40	13,593,229.49	17,251,501.95	0.00	Unidirectional	Steel- beam and vault

III.7.5 Roof elements

NOTE:

we considered the roof as a rigid element because it's so rotten and old and it will affect the analysis

1) Wooden beam

Table III 15. Roof materials

Material	Area [mm2]	J [mm4]	W [mm3]
C24 - en 338	17,500.00	91,145,800.8	729,170.0

2) Roof slope

Table III 16 the resistance direction of the floor

Mass loading	Туре
Unidirectional	Rigid floor

III.8 CONCLUSION

In conclusion, Chapter III focuses on the study case of the Asla Hocine Primary School. Includes a presentation of the school, an urban study, and an architectural study. It also covers a constructive and structural analysis, reference codes, actions, loads, and the mechanical characteristics of the building's elements.

This comprehensive study provides valuable insights into the condition, performance, and design of the school building. It serves as a practical example for assessing and diagnosing masonry structures.

IV.1 INTRODUCTION

Static analysis of a building refers to the process of evaluating the structural stability and strength of a building using engineering principles and mathematical calculations. It involves assessing the building's ability to withstand various loads, such as dead loads (weight of the building itself), live loads (occupant loads, furniture, equipment), wind loads, seismic loads, and other external forces.

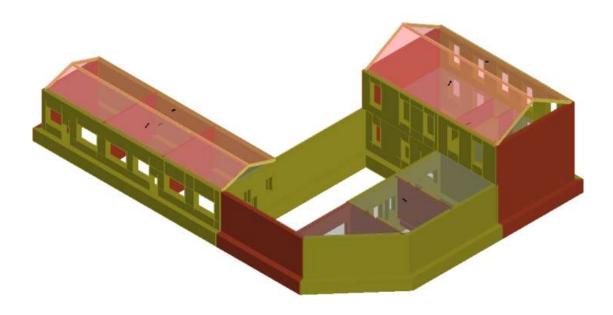


Figure IV 1. 3D view of the structure model

IV.2 REFERENCE CODE

For the analyzes described below, the principles and rules set out in the following regulations have been implemented:

Ministerial Decree of 17 January 2018 - "Technical standards for construction" (italy)
Application Circular No. 7 of 21 January 2019

IV.3 ANALYSIS METHOD

The modelling of the building is achieved by inserting walls that are discretized into macro-elements, representative of masonry piers and deformable floor strips; the rigid nodes are indicated in the portions of masonry which are typically less subject to seismic damage. Usually, the piers and spandrels are contiguous to the openings, the rigid nodes represent connecting elements between piers and spandrels. The mathematical conception that is hidden in the use of this element, allows to recognize the damage mechanism, by shear in its central part or by bending on the edges of the element in order to perceive the dynamics of the damage as it actually occurs in reality.

The nodes of the model are three-dimensional nodes with 5 degrees of freedom (the three components of displacement in the global reference system and the rotations around the X and Y axes) or two-dimensional nodes with 3 degrees of freedom (two translations and the rotation in the plane of the wall). The three-dimensional ones are used to allow the transfer of actions, from a first wall to a second one arranged transversally with respect to the first. The two-dimensional type nodes have degrees of freedom only in the plane of the wall allowing the transfer of stress states between the various points of the wall.

The horizontal elements, are modeled with three-node floor elements connected to the three-dimensional nodes, and can be loaded perpendicularly to their plane by accidental and permanent loads; seismic actions load the floor along the mid-story direction. For this reason, the floor finite element is defined with an axial stiffness, but no flexural stiffness, since the main mechanical behavior to be investigated is that under horizontal load due to the earthquake.

IV.3.1 Type of analysis performed

In order to carry out the necessary checks on the building in question, it was decided to proceed with the execution of a static analysis.

The required verifications take the form of a comparison between the value of the acting vertical load and the resistant vertical load. This evaluation is carried out by examining the slenderness and eccentricity values [2018 Technical Standards §4.5.6].

IV.4 MODEL DESCRIPTION

IV.4.1 materials

IV.4.1.1 Mechanical behaviour of the masonry

The mechanical properties of the masonry material are defined in order to best identify its behaviour in the non-linear field.

The main features are:

- Initial stiffness according to the elastic characteristics (cracked) of the material;
- Redistribution of the internal stresses of the element such as to guarantee equilibrium;
- Setting of the damage state according to the global and local parameters;
- Stiffness degradation in the plastic branch;
- Ductility control by defining the maximum drift (δu) differentiated according to the provisions of the regulations in force according to the damage mechanism acting on the panel;
- Elimination of the element, when the limit conditions are reached without interrupting the analysis.

The non-linear behaviour is activated when a force value reaches its maximum value defined as the minimum between the bending and shear resistance criteria.

The behaviour of the masonry piers associated with the shear and bending mechanisms can be described through different traits that represent the progressive levels of damage.

IV.4.1.2 Wall with shear mechanism

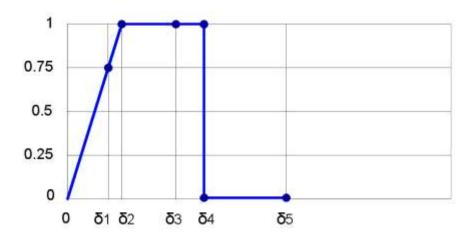


Figure IV 2 Wall behaviour curve with shear mechanism

The behavior of the masonry in shear can be described through the following sections, representative of the progressive levels of damage relative to the previous diagram:

Table IV 1 The behaviour of the masonry in shear and the related level of damage

$0-\delta 1$	elasticity
$\delta 1 - \delta 2$	incipient plasticity
$\delta 2 - \delta 3$	plastic for cutting
$\delta 3 - \delta 4$	incipient shear failure
$\delta 4 - \delta 5$	shear breakage
$\delta 5 - \infty$	severe crisis

IV.4.1.3 Wall with bending mechanism

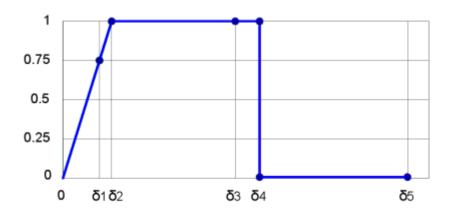


Figure IV 3 Wall behaviour curve with bending mechanism

On the other hand, the behavior of the bending wall masonry can be described by the following features:

Table IV 2 The behaviour of the masonry in bending mechanism and the related level of damage

$0-\delta 1$	elasticity	
$\delta 1 - \delta 2$	incipient plasticity	
$\delta 2 - \delta 3$	plastic for bending	
$\delta 3 - \delta 4$	incipient rupture due to bending	
$\delta 4 - \delta 5$	bending failure	
$\delta 5 - \infty$ severe crisis		

Some of these failure levels are necessary to describe the progress of the crisis more accurately, allowing a more accurate prediction of the interventions and the level of deterioration of the masonry:

- Incipient plasticity: When an element is still in the elastic range but is close to plasticity
- Incipient failure: When an element is in the plastic range but is close to failure
- Serious crisis: When, following the failure of the element, the deformations become so significant as to be able to generate a local collapse.
- The software provides three bond categories:
- With Strength Degradation to a Residual Value (Multiline Link)

- With resistance equal to the residual value (Bilinear bond)
- No residual strength
- Among these, the bond categories used within the project in question are:
- In the absence of residual resistance

IV.4.1.4 In the absence of residual resistance

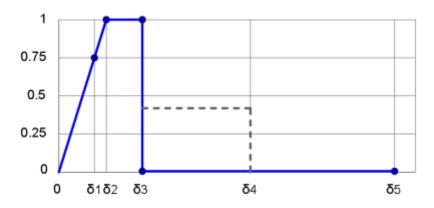


Figure IV 4 Wall behaviour curve in case of absence of residential resistance

This type of link represents a variant logic of the previous links starting from the multilinear link but is not currently contemplated in the current regulations. For the identifications and Explanations of details look in the **Appendix I**

IV.5 LOADS

IV.5.1 Seismic load:

Checks at the ultimate limit state (SLV) and at the serviceability limit state (SLD; SLO); must be carried out for the following combination [Technical Standards 2018 §2.5.3].

$$E + G_{k1} + G_{k2} + \sum_{i} \Psi_{2i} Q_{Ki}$$

The effects of the seismic action will be evaluated taking into account the masses associated with the following gravitational loads:

$$G_{k1} + G_{k2} + \sum_{i} \Psi_{2i} Q_{Ki}$$

IV.5.2 Static Load:

The ultimate limit state verification for static loads is conducted with the following combination of loads.

$$\gamma_{G1} G_{k1} + \gamma_{G2} G_{k2} + \gamma_{Q} \Psi_{0} Q_{k}$$

Where:

E seismic action for the limit state in question;

G_{k1} self-weight of all structural elements;

G_{k2} self-weight of all non-structural elements;

 Q_{Ki} characteristic value of the variable action;

Y₂ combination coefficient;

Y₀ combination factor for variable loads

y_{G1}; y_{G2}; y_{Q:} partial safety factors

The values of the various coefficients are chosen on the basis of the intended use of the various floors as indicated in the standard. [2018 Technical Standards Table 2.5.1].

IV.6 GLOBAL STATIC VERIFICATION

The static checks performed on the structure in question are as follows:

IV.6.1 Slenderness of the masonry

The slenderness check is performed in accordance with what is reported in point 4.5.4. of the DM2018.

The slenderness of a masonry is defined as the ratio h0/t in which:

h0: free buckling length of the wall equal to ar h;

t: wall thickness.

h: the internal height of the floor;

r: the lateral constraint factor.

The slenderness check is satisfied if the following is true:

h0/t < 20

CHAPTER IV STATIC VERIFICATION

IV.6.2 Load eccentricity

The slenderness check is performed in accordance with what is reported in point 4.5.6.2. of the DM2018.

This verification is satisfied if the following conditions are verified:

$$e1/t \le 0.33$$

$$e2/t \le 0.33$$

in which:

t: wall thickness

$$e_1 = |e_s| + |e_a|$$
 ; $e_2 = \frac{e_1}{2} + |e_v|$

es: total eccentricity of vertical loads

ea: h/200

ev: eccentricity due to wind ev = Mv / N

IV.6.3 Verification at vertical loads

The slenderness check is performed in accordance with what is reported in point 4.5.6.2. of the DM2018.

This verification is satisfied if the following is verified:

 $Nd \le Nr$

in which:

Nd: acting vertical load

Nr: resistant vertical load; Nr = f fd A

A: area of the horizontal section of the wall net of openings;

fd: design resistance of the masonry;

f: coefficient of reduction of the resistance of the wall

These checks were carried out in each masonry of the structure, in the three main sections (lower, central, upper).

The values of the normal resistant stress will be calculable only if the checks of slenderness and eccentricity of the loads are satisfied. We report below the verification details for the individual walls.

CHAPTER IV STATIC VERIFICATION

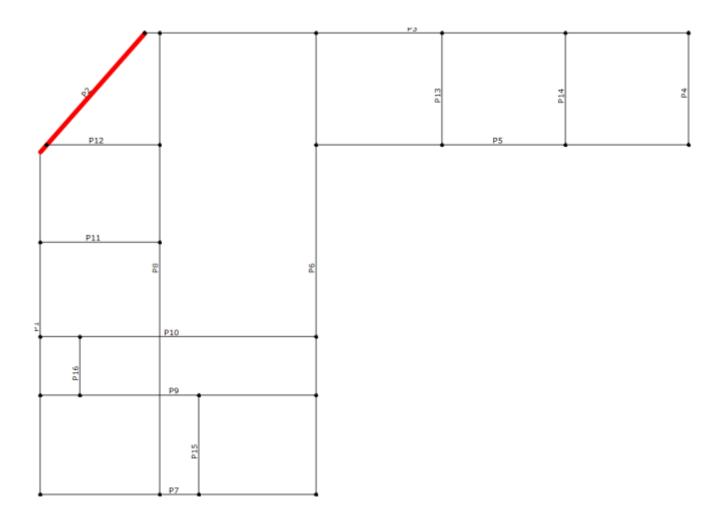


Figure IV 5. the structure walls numbers

IV.6.4 the results

a static verification process is conducted to assess the structural integrity of the building's elements. The non-vitrified (red) elements are scrutinized for potential vulnerabilities, while the verified (green) elements have been thoroughly examined and deemed structurally sound. This differentiation helps identify areas that require further analysis or reinforcement to ensure the overall safety and stability of the building.

Table IV 3 the legend table for verification of element status

Legend						
Verified element						
Not verified element						

IV.6.4.1 Wall: 1

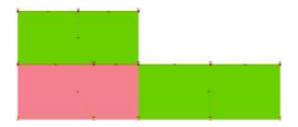


Figure IV 6 wall 1 element verification

Table IV 4 slenderness and eccentricity verification for wall 1

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
1	4.510	0.400	11.275	0.056	0.056	0.056	Yes
2	4.510	0.400	11.275	0.122	0.077	0.245	Yes
3	4.350	0.400	10.875	0.054	0.054	0.054	Yes

Table IV 5 vertical load bearing resistance verification for wall 1

		Тор	ı				Middle	e				Bottom			
Pier	Nd	F	Nr	Nd/N	٧r	Nd	F	Nr	Nd	/Nr	Nd	F	Nr	Nd/Nr	Satisfied
1	426	0.654	659	0.64	6	659	0.654	659	1.0	000	893	0.654	659	1.354	No
2	308	0.255	604	0.51	1	597	0.595	1,408	0.4	124	885	0.503	1,188	0.745	Yes
3	155	0.672	677	0.22	9	356	0.672	677	0.5	527	582	0.672	677	0.859	Yes

IV.6.4.2 Wall: 3

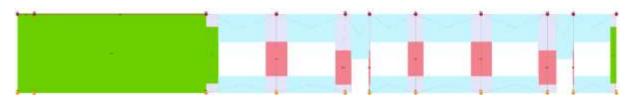


Figure IV 7 wall 3 element verification

Table IV 6 slenderness and eccentricity verification for wall 3

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
19	4.630	0.400	11.575	0.058	0.058	0.058	Yes
20	4.510	0.600	7.517	0.087	0.049	0.116	Yes
21	4.510	0.600	7.517	0.179	0.096	0.207	Yes
22	4.510	0.600	7.517	0.174	0.092	0.196	Yes
23	4.510	0.600	7.517	0.174	0.091	0.191	Yes
24	4.510	0.600	7.517	0.178	0.094	0.201	Yes
25	4.510	0.600	7.517	0.183	0.098	0.214	Yes
26	4.510	0.600	7.517	0.171	0.090	0.191	Yes
27	4.510	0.600	7.517	0.182	0.094	0.196	Yes
28	4.510	0.600	7.517	0.074	0.040	0.089	Yes

Table IV 7 vertical load bearing resistance verification for wall $\boldsymbol{3}$

		Top)				Middle]	Bottom			
Pier	Nd	F	Nr	Nd/N	Jr .	Nd	F	Nr	Nd	/Nr	Nd	F	Nr	Nd/Nr	Satisfied
19	58	0.642	703	0.083	3	302	0.642	703	0.4	-29	555	0.642	703	0.790	Yes
20	65	0.597	128	0.50	6	84	0.764	164	0.5	609	102	0.652	140	0.730	Yes
21	197	0.418	156	1.26	3	217	0.636	237	0.9	13	237	0.475	178	1.332	No
22	177	0.440	120	1.47	5	192	0.643	176	1.0	91	206	0.485	133	1.555	No
23	22	0.450	12	1.91	1	24	0.645	17	1.4	16	25	0.484	13	1.994	No
24	175	0.431	117	1.49	1	189	0.639	174	1.0	87	204	0.477	130	1.566	No
25	182	0.404	146	1.24	9	201	0.631	228	0.8	884	220	0.466	168	1.309	No
26	212	0.450	139	1.529	9	228	0.647	199	1.1	45	245	0.491	152	1.613	No
27	15	0.439	6	2.35	1	16	0.639	9	1.7	00	17	0.469	7	2.425	No
28	45	0.650	67	0.669	9	54	0.792	82	0.6	558	63	0.688	71	0.885	Yes

IV.6.4.3 Wall: 6



Figure IV 8 wall 6 element verification

Table IV 8 slenderness and eccentricity verification for wall 6

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
38	4.510	0.400	11.275	0.056	0.056	0.056	Yes
39	4.630	0.500	9.260	0.046	0.046	0.046	Yes
40	4.350	0.400	10.875	0.054	0.054	0.054	Yes
41	4.510	0.550	8.200	0.041	0.041	0.041	Yes
42	4.510	0.550	8.200	0.041	0.041	0.041	Yes
43	4.510	0.550	8.200	0.041	0.041	0.041	Yes
44	4.510	0.550	8.200	0.041	0.041	0.041	Yes
45	4.510	0.550	8.200	0.041	0.041	0.041	Yes

Table IV 9 vertical load bearing resistance verification for wall 6

		Тор	p			Middl	e			В	ottom			
Pier	Nd	F	Nr	Nd/N	Ir Nd	F	Nr	Nd	/Nr	Nd	F	Nr	Nd/Nr	Satisfied
38	390	0.654	659	0.592	2 624	0.654	659	0.9	946	857	0.654	659	1.300	No
39	296	0.737	2,257	0.13	1 669	0.737	2,257	0.2	297	1,043	0.737	2,257	0.462	Yes
40	163	0.672	677	0.240	0 369	0.672	677	0.5	645	594	0.672	677	0.877	Yes
41	29	0.775	124	0.236	6 43	0.775	124	0.3	346	56	0.775	124	0.456	Yes
42	85	0.775	235	0.362	2 100	0.775	235	0.4	28	116	0.775	235	0.493	Yes

43	5	0.775	15	0.357	6	0.775	15	0.422	7	0.775	15	0.488	Yes
44	73	0.775	219	0.333	87	0.775	219	0.396	101	0.775	219	0.459	Yes
45	51	0.775	146	0.349	67	0.775	146	0.459	83	0.775	146	0.569	Yes

IV.6.4.4 Wall: 7

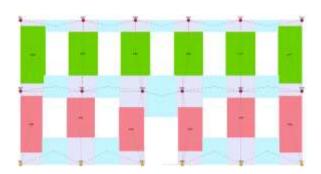


Figure IV 9 wall 7 element verification

Table IV 10 slenderness and eccentricity verification for wall 7

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
60	4.510	0.600	7.517	0.087	0.047	0.102	Yes
61	4.510	0.600	7.517	0.123	0.066	0.141	Yes
62	4.510	0.600	7.517	0.125	0.067	0.146	Yes
63	4.510	0.600	7.517	0.122	0.066	0.144	Yes
64	4.510	0.600	7.517	0.122	0.065	0.141	Yes
65	4.510	0.600	7.517	0.082	0.044	0.097	Yes
66	4.350	0.600	7.250	0.036	0.036	0.036	Yes
67	4.350	0.600	7.250	0.036	0.036	0.036	Yes
68	4.350	0.600	7.250	0.036	0.036	0.036	Yes
69	4.350	0.600	7.250	0.036	0.036	0.036	Yes
70	4.350	0.600	7.250	0.036	0.036	0.036	Yes
71	4.350	0.600	7.250	0.036	0.036	0.036	Yes

Table IV 11 vertical load bearing resistance verification for

		To	p				Middle				I	Bottom			
Pier	Nd	F	Nr	Nd/N	١r	Nd	F	Nr	Nd	/Nr	Nd	F	Nr	Nd/Nr	Satisfied
60	247	0.624	255	0.97	0	285	0.772	315	0.9	906	324	0.653	267	1.214	No
61	323	0.549	285	1.13	3	357	0.714	371	0.9	963	392	0.583	303	1.291	No
62	272	0.539	252	1.07	7	306	0.709	332	0.9	920	339	0.580	272	1.250	No
63	265	0.544	249	1.06	1	298	0.713	327	0.9	911	331	0.585	268	1.235	No
64	319	0.550	286	1.11	6	354	0.715	372	0.9	950	388	0.585	304	1.274	No
65	248	0.634	269	0.92	0	288	0.779	331	0.8	368	327	0.662	282	1.163	No
66	60	0.809	379	0.15	9	105	0.809	379	0.2	277	149	0.809	379	0.394	Yes
67	39	0.809	445	0.08	7	78	0.809	445	0.1	176	118	0.809	445	0.265	Yes
68	40	0.809	445	0.09	1	80	0.809	445	0.1	180	120	0.809	445	0.270	Yes
69	39	0.809	434	0.08	9	78	0.809	434	0.1	179	116	0.809	434	0.268	Yes
70	39	0.809	445	0.08	7	78	0.809	445	0.1	176	118	0.809	445	0.266	Yes
71	58	0.809	361	0.16	0	100	0.809	361	0.2	278	143	0.809	361	0.395	Yes

IV.6.4.5 Wall: 8

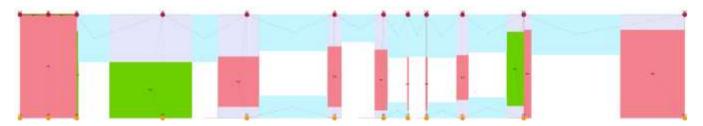


Figure IV 10 wall 8 element verification

Table IV 12 slenderness and eccentricity verification for wall 8

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
85	4.510	0.100	45.100	0.226	0.226	0.226	Yes
86	4.510	0.600	7.517	0.038	0.038	0.038	Yes
87	4.510	0.600	7.517	0.038	0.038	0.038	Yes

88	4.510	0.600	7.517	0.113	0.060	0.130	Yes
89	4.510	0.600	7.517	0.172	0.093	0.203	Yes
90	4.510	0.600	7.517	0.167	0.091	0.202	Yes
91	4.510	0.600	7.517	0.174	0.092	0.195	Yes
92	4.510	0.600	7.517	0.175	0.092	0.196	Yes
93	4.510	0.600	7.517	0.174	0.091	0.192	Yes
94	4.510	0.600	7.517	0.123	0.069	0.160	Yes
95	4.510	0.400	11.275	0.171	0.105	0.286	Yes
96	4.510	0.400	11.275	0.112	0.068	0.189	Yes

Table IV 13vertical load bearing resistance verification for wall 8

		Top)				Middle]	Bottom			
Pier	Nd	F	Nr	Nd/N	٧r	Nd	F	Nr	Nd	/Nr	Nd	F	Nr	Nd/Nr	Satisfied
85	39	0.000	n/d	n / c	d	53	0.000	n/d	n /	/ d	67	0.000	n / d	n / d	No
86	5	0.800	17	0.31	2	7	0.800	17	0.4	40	10	0.800	17	0.568	Yes
87	368	0.800	879	0.41	9	441	0.800	879	0.5	501	513	0.800	879	0.584	Yes
88	286	0.570	312	0.91	5	318	0.730	400	0.7	95	350	0.603	330	1.061	No
89	113	0.425	79	1.42	4	126	0.641	120	1.0)55	140	0.489	91	1.528	No
90	90	0.428	73	1.23	3	103	0.645	110	0.9	930	115	0.500	85	1.343	No
91	12	0.441	7	1.77	9	13	0.643	10	1.3	316	14	0.485	8	1.874	No
92	20	0.440	10	1.88	0	21	0.642	15	1.3	885	23	0.482	11	1.973	No
93	128	0.447	71	1.80	7	136	0.644	102	1.3	37	144	0.484	76	1.889	No
94	91	0.512	117	0.77	8	111	0.703	160	0.6	591	131	0.584	133	0.982	Yes
95	13	0.000	n /d	n / c	d	20	0.536	18	1.1	.08	27	0.408	14	1.941	No
96	82	0.370	106	0.77	9	139	0.622	178	0.7	81	196	0.521	149	1.311	No

IV.6.4.6 Wall: 9

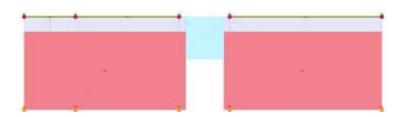


Figure IV 11 wall 9 element verification

Table IV 14 slenderness and eccentricity verification for wall 9

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
98	4.510	0.300	15.033	0.092	0.075	0.105	Yes
99	4.510	0.300	15.033	0.104	0.075	0.123	Yes

Table IV 15 vertical load bearing resistance verification for wall 9

	Тор				Middle				Bottom					
Pier	Nd	F	Nr	Nd/Nı	r Nd	F	Nr	Nd/	Nr	Nd	F	Nr	Nd/Nr	Satisfied
98	332	0.437	523	0.635	454	0.500	597	0.76	60	576	0.462	552	1.044	No
99	383	0.404	472	0.812	502	0.500	584	0.86	51	622	0.439	513	1.213	No

IV.6.4.7 Wall: 10

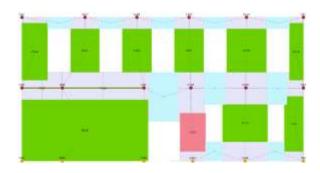


Figure IV 12 wall 10 element ferification

Table IV 16 slenderness and eccentricity verification for wall 10

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
110	4.510	0.500	9.020	0.104	0.060	0.147	Yes
111	4.510	0.500	9.020	0.105	0.056	0.119	Yes
112	4.510	0.500	9.020	0.099	0.053	0.113	Yes
113	4.510	0.500	9.020	0.083	0.045	0.103	Yes
114	4.350	0.500	8.700	0.043	0.043	0.043	Yes
115	4.350	0.500	8.700	0.043	0.043	0.043	Yes
116	4.350	0.500	8.700	0.043	0.043	0.043	Yes
117	4.350	0.500	8.700	0.043	0.043	0.043	Yes
118	4.350	0.500	8.700	0.043	0.043	0.043	Yes
119	4.350	0.500	8.700	0.043	0.043	0.043	Yes

Table IV 17 vertical load bearing resistance verification for wall 10

		Тој	p			Middle	9				Bottom			
Pier	Nd	F	Nr	Nd/Nr	Nd	F	Nr	Nd/	/Nr	Nd	F	Nr	Nd/Nr	Satisfied
110	553	0.507	1,001	0.552	755	0.700	1,383	0.5	46	956	0.590	1,165	0.821	Yes
111	215	0.561	222	0.968	241	0.714	283	0.8	51	266	0.588	233	1.141	No
112	333	0.572	402	0.829	377	0.722	507	0.7	42	420	0.599	421	0.998	Yes
113	101	0.591	176	0.575	128	0.744	221	0.5	80	156	0.631	188	0.830	Yes
114	59	0.757	304	0.193	97	0.757	304	0.3	19	135	0.757	304	0.444	Yes
115	31	0.757	337	0.093	63	0.757	337	0.1	88	96	0.757	337	0.284	Yes
116	33	0.757	344	0.095	65	0.757	344	0.1	90	98	0.757	344	0.286	Yes
117	30	0.757	344	0.087	63	0.757	344	0.1	83	96	0.757	344	0.278	Yes
118	40	0.757	469	0.085	85	0.757	469	0.1	81	130	0.757	469	0.277	Yes
119	42	0.757	165	0.253	62	0.757	165	0.3	79	83	0.757	165	0.505	Yes

IV.7 FINDS

The results of the static verification process have revealed that a significant number of masonry elements are represented in red, indicating potential concerns. Specifically, these elements have been verified for slenderness and eccentricity but have not been verified for their ability to bear vertical loads effectively.

The identification of these red-colored masonry elements raises concerns about their structural integrity and their capacity to handle the vertical loads imposed upon them. It suggests that further investigation and analysis are required to ensure their ability to safely support vertical loads.

Addressing the issues related to the vertical load-bearing capacity of these masonry elements is crucial to maintain the overall stability and safety of the building. Measures such as additional reinforcement, modifications, or design alterations might be necessary to enhance their load-bearing capacity and minimize the risk of structural failure.

. The slenderness ratio of a masonry structure provides insights into its stability and vulnerability to excessive deflection or failure under vertical loads.

Excessive eccentricity can result in uneven stress distribution, compromising the overall stability and load-carrying capacity of the structure.

Without the required verifications, comparing the acting vertical load to the resistant vertical load, considering slenderness and eccentricity values, offers a preliminary understanding of the potential structural adequacy or vulnerability of the masonry building, wish mean that the faluire is about the wall resistance.

By giving proper attention to these red-colored masonry elements, the building's structural performance can be improved, providing a secure environment for occupants and ensuring the long-term integrity of the structure.

Therefore, it is essential to prioritize the verification of the vertical load-bearing capacity of these masonry elements to address any potential weaknesses and ensure their ability to effectively carry the required loads within the building.

IV.8 CONCLUSION

The study delves into the static verification of the masonry structure. The analysis method used and the type of analysis performed are described, providing a framework for the evaluation process. A comprehensive model description, including the materials behaviour hypothisis utilized, is provided to establish the context for the verification. The loads considered, such as seismic and static loads, are discussed in relation to their influence on the structural behavior.

The global static verification process focuses on three key aspects: the slenderness of the masonry, load eccentricity, and the verification of vertical loads. These factors are crucial in assessing the structural stability and load-bearing capacity of the masonry elements. The chapter presents the results of the verification, highlighting the findings of the analysis. These findings offer valuable insights into the behavior and performance of the masonry structure, enabling a comprehensive assessment of its structural integrity and its ability to withstand various loads and external forces.

CHAPTE V SEISMIC PERFORMANCE ANALYSIS

V.1 Introduction

A building prototype's seismic vulnerability is determined by the probability that it will encounter some sort of financial loss at a specific level of seismic activity. It is generated by combining the fragility model, the probability of experiencing each state of damage for a specific degree of seismic intensity, and the resulting economic losses for each condition of damage.

Analysing the seismic reaction of a building prototype is necessary for the fragility model. The capacity model or pushover curve is a representation of a building's physical response to seismic pressures. The performance point of the prototype can be obtained by combining the capacity curve with the seismic demand, which is represented by the seismic response spectrum. There are various ways to determine the performance point. The degree of damage established according to quantitative parameters (such as displacement) or qualitative ones (such as state of cracking) is compared to the performance point to identify the state of damage obtained by the prototype (light, moderate, extensive, and complete).

It is possible to identify the distinctive characteristics of the fragility curves and derive the probability for each state of damage (light, moderate, extensive, and complete) thanks to the variability of the capacity model, seismic demand, and specification of the degrees of damage. Finally, the creation of vulnerability curves allows for the economic losses caused by physical damage indicated by the risk ratio to be translated.

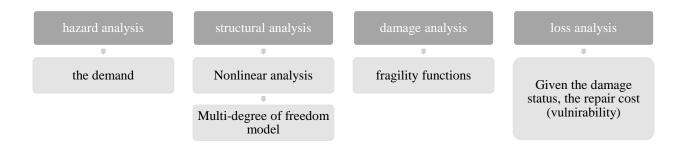


Figure V 1. risk assessment formwork

V.2 SEISMIC SPECTRUM ASSESSMENT

According to the (ATC40), the maximum reaction of any simple linear oscillator exposed to a given stress is summarized by the elastic response spectrum. The response spectrum is created by classifying the maximal elastic response values for each oscillator by vibration period. For a fixed value

of the damping coefficient, the response values are calculated. The graphs used to show the spectral acceleration (Sa) as a function of the period (T) are called spectra.

The elastic Response spectrum: Curves used to assess the maximum response of a building to a past or future earthquake, and according to the **Algerian seismic regulation (RPA 99 2003)** we can determine the demand spectrum as follows:

V.2.1 SITE SELECTION

Site selection should take into account adverse conditions such as active faults, unstable ground, compacts, waterlogged, poorly drained or flood-prone land, underground cavities, uncompacted backfill, uneven surface topography, alluvium, different geological formations, and seismic microzoning studies. The final choice of the site will be decided on the basis of the results of investigations, the importance of which will be related to that of the planned work.

V.2.2 Reconnaissance and soil studies

Soil reconnaissance and studies are essential for structures of medium or greater importance located in areas of medium to high seismicity. These studies must be able to classify the site and detect liquefiable and/or unstable zones, as well as consider the dynamic properties of the soils in calculations.

V.2.3 Modelling and calculation methods

The choice of calculation methods and modelling of the structure must aim to reproduce the real behaviour of the structure as well as possible. It is accepted that structures subjected to seismic action may undergo deformations in the post-elastic range, so linear calculation methods are used. A unique behaviour coefficient is used to determine the design forces of the structure and estimate the inelastic deformations. More elaborate calculation methods may be used, subject to scientific justification.

V.2.4 Seismic zone classification

The national territory is divided into four zones of increasing seismicity, defined on the map of seismicity zones and the associated table.

- Zone O is negligible
- Zone L is low
- Zone IIa is average

• Zone IIb and III is high.

The seismic classification by wilaya and municipality is different when the wilaya is shared between two different seismic zones.

V.2.5 Classification Of Works According to Their Importance

The minimum level of seismic protection granted to a structure depends on its destination and importance to the community. This classification recommends minimum protection thresholds that a client can modify only by upgrading the structure for increased protection, taking into account the nature and destination of the structure with regard to the objectives targeted. Structures must be classified in one of the four (04) groups defined below:

- Group 1A includes works of vital importance that must remain operational after a major
 earthquake. These include strategic decision-making centres, emergency and/or national
 defense personnel and equipment, public health establishments, public communication
 establishments, public works of a cultural or historical nature, energy production or
 distribution centers, and administrative or other buildings that must remain functional in
 the event of an earthquake.
- **Group 1B** includes works of great importance such as mosques, office buildings, industrial and commercial buildings, schools, universities, sports and cultural buildings, penitentiaries, large hotels, collective housing or office use, public works of national interest or socio-cultural and economic importance, libraries or archive buildings of regional importance, health establishments other than those of group 1A, energy production or distribution centers, and large to medium size water towers and reservoirs.
- **Group 2** is composed of structures that can accommodate up to 300 people simultaneously, such as collective housing, office buildings, industrial buildings, and public car parks.
- **Group 3**: Structures of minor importance, Industrial, agricultural, and temporary buildings are suitable for low-value goods, with limited risk for people.

V.2.6 Site classification

The sites are classified into four categories based on the mechanical properties of the soils.

Table '	V	1	the	sites	classifica	tions

Category	Description	qc(MPA)	N(d)	pl(MPA) (Ep(MPA)	qu (MPA)	Vs (m/s) (g)
S1	Rocky (a)	-	-	>5	>100-	>10	≥800
S2	Firm	>15	>50	>2	>20	>0.4	≥400 - <800
S 3	loose soil	1.5 ~ 15	10 ~ 50	1 ~ 2	5 ~ 20	01 ~ 0.4	≥200 - <400
S4	Very Loose or Presence of at least 3m of soft clay (b)	<1.5	<10	<1	<5	< 0.1	≥100 <200

V.2.7 Calculation response Spectrum

The seismic action is represented by the following calculation spectrum.

$$\frac{S_a}{g} = \begin{cases} 1.25A \left(1 + \frac{T}{T_1} \left(2.5\eta \frac{Q}{R} - 1\right)\right) & 0 \le T \le T_1 \\ 2.5\eta \left(1.25A\right) \left(\frac{Q}{R}\right) & T_1 \le T \le T_2 \\ 2.5\eta \left(1.25A\right) \left(\frac{Q}{R}\right) \left(\frac{T_2}{T}\right)^{2/3} & T_2 \le T \le 3.0s \\ 2.5\eta \left(1.25A\right) \left(\frac{T_2}{3}\right)^{2/3} \left(\frac{3}{T}\right)^{5/3} \left(\frac{Q}{R}\right) & T > 3.0s \end{cases}$$

A: zone acceleration coefficient

Table V 2. The zones acceleration

	Zone		
Group	I	II	III
1A	0,12	0,25	0,35
1B	0,10	0,20	0,30

2	0,08	0,15	0,25
3	0,05	0,10	0,15

 η : damping correction factor for the elastic spectrum ξ =5%

$$\eta = \sqrt{7/(2+\xi)} \ge 0.7$$

T1, T2: characteristic periods associated with the category of site

Table V 3. sites periods

Site	S_1	S_2	S ₃	S ₄
$T_{1(sec)}$	0,15	0,15	0,15	0,15
T _{2(sec)}	0,30	0,40	0,50	0,70

Q: quality factor $Q = 1 + \sum_{1}^{5} P_q$

Table V 4. quality factors index

		Pq
Criteria q »	Observed	N/observed
1. Minimum conditions on bracing rows	0	0,05
2. In-plane redundancy	0	0,05
3. Regularity in plan	0	0,05
4. Regularity in elevation	0	0,05
5. Material quality control	0	0,05
6. Execution quality control	0	0,10

W: total weight of the structure,

 \mathbf{W} is equal to the sum of the weights

W_i, calculated at each level (i):

$$W = \sum_{i=1}^n \ W_i \qquad \qquad with \qquad W_{i=} \ W_{Gi} + \beta \ W_{Qi}$$

 W_{Gi} : weight due to permanent loads and those of fixed equipment possible, integral to the structure

W_{Qi}: charges exploitation

 $\beta\,$: weighting coefficient, depending on the nature and duration of the operating load

Table V 5. weighting coefficient

Case	Type of work	β
1 2	Residential buildings, offices or similar Buildings open to the public temporarily:	0,20
	 Exhibition halls, sports halls, places of worship, meeting rooms with standing room. classrooms, restaurants, dormitories, meeting rooms with 	0,30
	Seating places	0,40
3	Warehouses, sheds	0,50
4	Archives, libraries, repositories and similar works	1,00
5	Other premises not referred to above	0,60

R: global behaviour coefficient of the structure

For the elastic spectrum the value of the coefficient ${\bf R}={\bf 1}$ and ${\bf \xi}={\bf 5}$

V.2.8 Observance of Algerian seismic regulations

Because rules change and develop with time, the regulatory review is a critical stage in bringing the building up to code in order to:

- To avoid the technical and legal risks involved with rehabilitation operations.
- Ensure the implementation and follow-up of rehabilitation projects in accordance with continually changing requirements.

The school will be made comply with the current building rules, which concern:

- The Algerian earthquake regulation "RPA" version 2003.
- Fire and panic restrictions.

The classification is required for the definition of the seismic setting investigated which will aid in the selection of the technique of calculation and the identification of the seismic force calculation parameters in order to simulate the building to the earthquake once it has been modelled.

• Seismic Zone:

This entails categorizing the structure based on the following criteria:

The school is located in the town of **Annaba**, the latter is in the seismic zone

"Zone II a" which is characterized by an average seismicity.

• Importance of the building: classified in the group "medium-sized work in ''the category 1A''.

site soil classification: Category S2 (firm site): Deposits of very dense sand and gravel and/or over consolidated clay 10 to 20 m thick with $VS \ge 400$ m/s from a depth of 10 m.

Values of ξ (%): where ξ (%) is percentage of critical damping function of the constituent material, type of structure and the importance of the fillings adopted: for elastic spectrum " $\xi = 5\%$ "

- '' $\eta = 1$ '': damping factor
- R: global behaviour coefficient of the structure: Value of "R = 1".
- **Q:** quality factor: "Q = 1"
- "CT = 0.5": coefficient, depending on the bracing system, the type of filling
- Value of "T1=0.15 et T2=0.40"

The response spectrum for the city of Annaba for a category S2 site is shown in the accompanying figure 2.

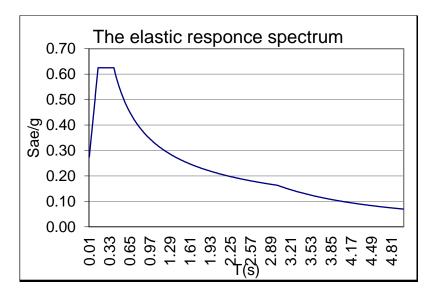


Figure V 2. The elastic response spectrum for A=0.2

V.3 PUSHOVER ANALYSIS DESCRIPTION

In order to carry out the necessary checks on the building in question, it was decided to proceed with the execution of a non-linear static analysis.

The required verifications take the form of a comparison between the capacity curve for the various conditions envisaged and the travel demand envisaged by the legislation.

The capacity curve is identified by means of a maximum displacement-shear diagram at the base.

According to the provisions of the legislation, the load conditions to be examined must consider at least two distributions of inertia forces, one falling into the main distributions (Group 1) and the other into the secondary distributions (Group 2) illustrated below.

- distribution proportional to static forces (Group 1)
- uniform distribution of forces, to be understood as derived from a uniform distribution of accelerations along the height of the building (Group 2);

The analysis, performed in displacement control, proceeds with the calculation of the distribution of forces which generates the value of the required displacement. The analysis is continued until the shear decays to 80% of its peak value. Thus, the value of the maximum displacement at the base of the building generated by that distribution of forces is calculated. This displacement value forms the ultimate value of the building.

The displacement taken into consideration for drawing the capacity curve is that of a point of the building called the control node.

The legislation requires the drawing of a bi-linear capacity curve of an equivalent system (SDOF). The tracing of this curve must take place with a straight line which, passing through the origin, intersects the curve of the real system in correspondence with 70% of the peak value; the second straight line will be parallel to the displacement axis such as to generate the equivalence of the areas between the diagrams of the real system and the equivalent one.

The determination of the curve relating to the equivalent system makes it possible to determine the period with which to obtain the maximum displacement required by the earthquake, according to the spectra reported in the regulations.

The legislation defines an accidental eccentricity of the center of the masses equal to 5% of the maximum dimension of the building in a direction perpendicular to the earthquake.

Based on the type of building and the design choices that are deemed most suitable, the seismic load condition to be taken into consideration can be decided.

- Seismic load: Identify which of the two types of distributions (proportional to the masses or the first way) to take into consideration.
- Direction: Identifies the direction along which the structure is loaded (X or Y of the global system) by the seismic load.

In order to identify the most severe seismic load condition, it was decided to carry out separate analyses by type of load, direction of the earthquake and any accidental eccentricities.

Table V 6 direction of the earthquake

No.	Seism dir.	Uniform pattern of lateral loads	Eccentricity [mm]	Level	node
1	+X	Uniform	0	2	3
2	+X	Static forces	0	2	3
3	-X	Uniform	0	2	3
4	-X	Static forces	0	2	3
5	+Y	Uniform	0	2	3
6	+Y	Static forces	0	2	3
7	-Y	Uniform	0	2	3
8	-Y	Static forces	0	2	3

V.4 DATA VALIDATION

V.4.1 Domain resistance calculation

V.4.1.1 Ordinary masonry

As indicated in paragraph C8.7.1.3.1.1 of the Circular n. 7 on 21st January 2019, three main methods of failure can be distinguished:

- by compression bending
- by sliding shear
- by diagonal cracking, dominated by diagonal traction in irregular masonry and in the form of "ladder" through the mortar joints.

The resistant shear is equal to the minimum of the values obtained by using, as appropriate, the verification criteria described below. Look ''data validation'' in **APPENDIX II.**

V.4.1.1.1 Compression bending

The resistant moment of the section is equal to:

$$M_u = \frac{\sigma_0 l^2 t}{2} \left(1 - \frac{\sigma_0}{k f_d} \right) \tag{1}$$

where:

 $\sigma_o = \frac{N}{lt}$ is the average compression normal stress,

N is the normal force acting on the section,

1 is the length of the panel,

t is the thickness of the panel,

f_d is the compressive resistance of the masonry,

 κ defines the amplitude of the stress-block (usually $\kappa = 0.85 \div 1$),

The value of k used in the present work is 0.85

Once the value of the resisting moment in the plane is known, the resistive shear of the panel can be calculated as:

$$V_f = \frac{M_u}{\alpha H} \tag{2}$$

where H is the height of the panel and a is a parameter that depends on the static diagram of the panel and is defined as:

$$\alpha = \left| \frac{M_{max}}{M_{max} + M_{min}} \right|$$

 M_{max} and M_{min} are respectively the bending moments acting at the upper and lower extremities of the pier. Consequently, in the case in which the panel is comparable to a cantilever a=1 while in the case it is comparable to a beam fixed at both ends a=0.5.

V.4.1.1.2 Sliding shear (new masonry)

The ultimate sliding shear resistance for new masonry can be obtained as described in paragraph 7.8.2.2.2 of Circular no. 7 of 21 January 2019:

$$V_{s} = f_{v}l't \tag{3}$$

where:

f_v is the shear resistance of the masonry,

1' is the length of the compressed area of the section,

t is the thickness of the panel.

The shear resistance fv is calculated using the Mohr-Coulomb resistance criterion by adding the contribution due to cohesion and the one due to friction:

$$f_v = f_{v0} + \mu \sigma_0 \le f_{v,lim} \tag{4}$$

 $\sigma_o = \frac{N}{l't}$ is the normal stress acting on the compressed part of the section (partialized section),

 μ is the coefficient of friction (usually assumed to be 0.4),

 f_{v0} is the initial shear resistance in the absence of compression,

f_{v,lim} is the upper limit value of the shear resistance (cracking of the elements).

Considering the section partialization condition, the length of the compressed portion can be determined (GUIDO MAGENES, 2002).

V.4.1.1.3 Sliding shear (existing regular masonry)

The ultimate sliding shear resistance for regular existing masonry can be obtained using the equation C8.7.1.17 of the Circular which takes into account the equivalent shear resistance of the masonry \tilde{f}_{v0} and an equivalent coefficient of friction \tilde{m} as a function of the local friction parameters of the joint:

$$V_s = \frac{l t}{b} \left(\tilde{f}_{v0} + \tilde{\mu} \sigma_0 \right) = \frac{l t}{b} \left(\frac{f_{v0d}}{1 + \mu \phi} + \frac{\mu}{1 + \mu \phi} \sigma_0 \right)$$
 (5)

where:

b varies with the h / l aspect ratio of the masonry panel (usually $1 \le b \le 1.5$),

m in the absence of more accurate assessments it can be assumed equal to 0.577,

F masonry meshing coefficient (in the absence of more accurate assessments it can be assumed equal to 0.5),

$$\sigma_o = \frac{N}{lt}$$
 is the average normal stress acting on the section

 f_{v0} is the initial shear strength in the absence of compression

Furthermore, it is necessary that the shear strength thus calculated does not exceed the value evaluated using the same formulas valid for the new masonry and illustrated in the previous paragraph.

V.4.1.1.4 Shear by diagonal cracking (existing irregular masonry)

The ultimate shear-traction resistance can be obtained using the Turnšek - Cacovic resistance criterion (equation C8.7.1.16 of the Circular):

$$V_{t} = lt \frac{f_{tu}}{b} \sqrt{1 + \frac{\sigma_{0}}{F_{tu}}} = lt \frac{1.5\tau_{0d}}{b} \sqrt{1 + \frac{\sigma_{0}}{1.5\tau_{0d}}}$$
 (6)

where: $\sigma_{o} = \frac{N}{lt}$ is normal stress of average compression,

b varies with the aspect ratio h / 1 (usually $1 \le b \le 1.5$),

 $f_{tu} = 1.5\tau_o$ is the conventional tensile strength of masonry,

t_o reference shear resistance of the masonry.

V.4.1.1.5 Shear by diagonal cracking (existing regular masonry)

In the case of existing regular masonry, the shear resistance for diagonal cracking is equal to the upper limit of the equation C8.7.1.17 of the Circular, i.e. the value $V_{t,lim}$ which can be estimated, approximately, as a function of the tensile failure of the f_{bt} blocks, and taking into account the geometry of the panel. This value can be deduced using the Mann-Muller Resistance Criterion defined in equation C8.7.1.18 of the Circular:

$$V_{t,lim} = \frac{lt}{b} \frac{f_{btd}}{2.3} \sqrt{1 + \frac{\sigma_0}{f_{btd}}}$$
 (7)

where f_{btd} can be obtained from literature data or through direct characterization tests in the laboratory of samples taken on site, eventually estimating it from the compressive strength of the f_b block, as f_{btd} =0.1 f_b .

V.4.1.1.6 Summarizing table of the verification criteria

In summary, the verification of an ordinary masonry wall panel can be summarized using the following table:

	Type of masonry		
	New	Existing regular	Existing irregular
Shear resistance	Minimum between: Equation (2) Equation (3)	Minimum between: Equation (2) Equation (3) Equation (5) Equation (7)	Minimum between: Equation (2) Equation (6)
Input parameters	l, t, H, a, fd, N, fv0, fv,lim	l, t, H, a, fd, N, fv0, fv,lim, m, F, fbtd	l, t, H, a, fd, N, t0

Table V 7 summary of verification equations for masonry wall

V.5 RESULTS

According to the indications of the law, the following checks must be carried out:

Limit State Collapse (SLC):

 D_u^{SLC} : Maximum displacement offered by the structure corresponding to the lesser of:

- the value of the residual basic cut equal to 80% of the maximum one
- the value corresponding to the achievement of the limit threshold of the angular deformation at SLC in all vertical piers of any level in any wall considered significant for safety purposes.

Limit State Life (SLV):

$$D_{max}^{SLV} \leq D_{u}^{SLV}$$

 D_{max}^{SLV} : Maximum displacement required by the standard identified by the elastic spectrum.

 D_u^{SLV} : Maximum displacement offered by the structure identified at 0.75 D_u^{SLC} .

$$q* < 3.0$$

q*: ratio between the elastic response force and the yield strength of the equivalent system

V.5.1 Result details

Table V 8 verification of the critical direction of the earthquake

No.	Seism dir.	Seismic load	Ecc.	Dmax ULS [mm]	Du ULS [mm]	q* ULS	ULS Ver.
1	+X	Uniform	0	22.32	40.21	2.02	Yes
2	+X	Static forces	0	08.33	35.07	2.63	Yes
3	-X	Uniform	0	23.75	51.30	2.18	Yes
4	-X	Static forces	0	29.47	38.80	3.61	No
5	+Y	Uniform	0	09.15	10.50	2.55	No
6	+Y	Static forces	0	18.62	17.39	3.17	No
7	-Y	Uniform	0	15.21	12.88	2.58	No
8	-Y	Static forces	0	18.70	18.21	3.20	No

Table V 9 pushover critical direction of the earthquake

No.	Seism dir.	Seismic load	Ecc.	α ULS
1	+X	Uniform	0	1,485
2	+X	Static forces	0	1.056
3	-X	Uniform	0	1,378
4	-X	Static forces	0	0.830
5	+Y	Uniform	0	0.760
6	+Y	Static forces	0	0.944
7	-Y	Uniform	0	0.878
8	-Y	Static forces	0	0.938

V.5.2 Results legend

Table V 10 colours legend RC

RC
undamaged
Shear failure
Bending damage
Bending failure
Compression failure
Tension failure
Shear failure

Tension failure		
Shear failure		
 timber		
undamaged		
Bending failure		
Compression failure		
Tension failure		
Steel		
undamaged		
Bending damage		
Compressive damage		
tensile damage		
Ineffective element		
Back to elastic condition		

 masonry		
undamaged		
Incipient plasticity		
Shear damage		
Incipient shear failure		
Shear failure		
Bending damage		
Incipient bending failure		
Bending failure		
Serious crisis		
Compression failure		
Tension failure		
Failure during elastic phase		
Ineffective element		

V.5.3 Seismic analysis no. 4 Direction X

We will only show the walls that are most vulnerable.

V.5.3.1 Seismic analysis no. 4 Wall 10

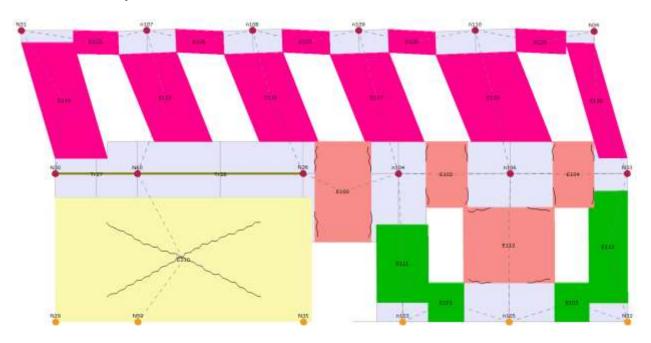


Figure V 3 wall 10 deformations result for X direction

V.5.3.1.1 General data

Table V 11 wall 10 analysis damage results X direction

Code	Technical standards 2018
Wall	10
Piers	110
Analysis	4
Substep	47/50
Limit Drift	0.005
Drift in Step	0.001
Damage condition	Shear damage

V.5.3.1.2 Input data from Model

Table V 12 wall 10 input conditions

Typology	Common masonry
The material's condition	Existing
Constitutive law	Irregular masonry (Turnsek/Cacovic)

V.5.3.1.2.1 Geometry

Table V 13 wall 10 geometry

Name	Value	Description
h [m]	3.883	Height (deformable portion)
1 [m]	7.999	Length
t [m]	0.500	Thickness

V.5.3.1.2.2 Masonry: rubble

Table V 14 wall 10 mechanical characteristics

Name	Value	Description
fm [kN/m2]	2,000.00	Average compressive strength of masonry
τ [kN/m2]	35.00	Average shear strength in the absence of normal stresses
CF	1.35	Confidence factor

V.5.3.1.3 Applied forces (from pushover analysis)

Table V 15 wall 10 applied forces for X direction

Name	Value	Description
Name	v alue	Description
N [kN]	527	Axial force
Vd [kN]	263	Shear
M top [kNm]	-225	Upper section bending moment
M bottom [kNm]	-794	Lower section bending moment

V.5.3.1.4 Resistance forces and verification

Table V 16 wall 10 resistance forces verifications for X direction

Name	Value	Description
N [kN]	527	Axial force (coincident with applied)
Vf [kN]	624	Shear (principle bending) calculated by interpolation on the resistance domain
Vs [kN]	326	Shear (principal shear) calculated by interpolation on the resistance domain
Vr [kN]	326	Shear (minimum between Vf and Vs)
Vd/Vr	0.806	Safety factor

V.5.3.1.5 Resistance domain diagram

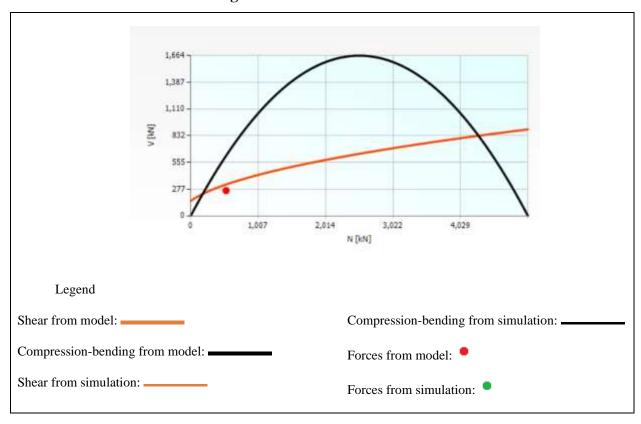
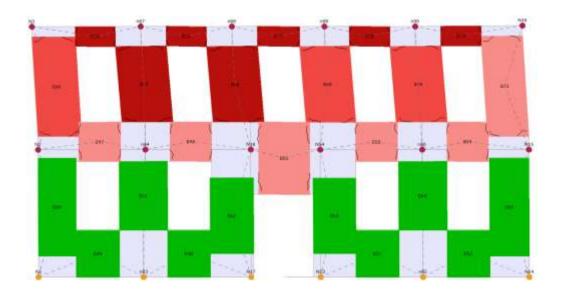


Figure V 4 wall 10 Resistance domain diagram

For the calculation domain look table 1 and 2 on the APPENDIX II



V.5.3.2 Seismic analysis no. 4 Wall 7

V.5.3.2.1 General data

Table V 17 wall 7 analysis damage results X direction

Code	Technical standards 2018
Wall	7
Piers	66
Analysis	4
Substep	45/50
Limit Drift	0.010
Drift in Step	0.008
Damage condition	Incipient bending failure

V.5.3.2.2 Input data from Model

Table V 18 wall 7 input conditions

Typology	Common masonry
The material's condition	Existing
Constitutive law	Irregular masonry (Turnsek/Cacovic)

V.5.3.2.2.1 Geometry

Table V 19 wall 7 geometry

Name	Value	Description
h [m]	3.610	Height (deformable portion)
l [m]	1.580	Length
t [m]	0.600	Thickness

V.5.3.2.2.2 Masonry "rubble"

Table V 20 wall 7 mechanical characteristics

	Tuest 1 20 Hall 1 Meetinited Characteristics		
Name	Value	Description	
fm [kN/m2]	2,000.00	Average compressive strength of masonry	
τ [kN/m2]	35.00	Average shear strength in the absence of normal stresses	
CF	1.35	Confidence factor	

V.5.3.2.3 Applied forces (from pushover analysis)

Table V 21 wall 7 applied forces for X direction

Name	Value	Description
N [kN]	17	Axial force
Vd [kN]	7	Shear
M top [kNm]	-13	Upper section bending moment
M bottom [kNm]	-13	Lower section bending moment

V.5.3.2.4 Resistance forces and verification

Table V 22 wall 7 resistance forces verifications for X direction

-	racio + 22 wan + repistance for	ces verifications for 11 direction	
	Name	Value	Description
	N [kN]	17	Axial force (coincident with applied)
	Vf [kN]	7	Shear (principle bending) calculated by interpolation on the resistance domain

Vs [kN]	30	Shear (principal shear) calculated by interpolation on the resistance domain
Vr [kN]	7	Shear (minimum between Vf and Vs)
Vd/Vr	1.002	Safety factor

V.5.3.2.5 Resistance domain diagram

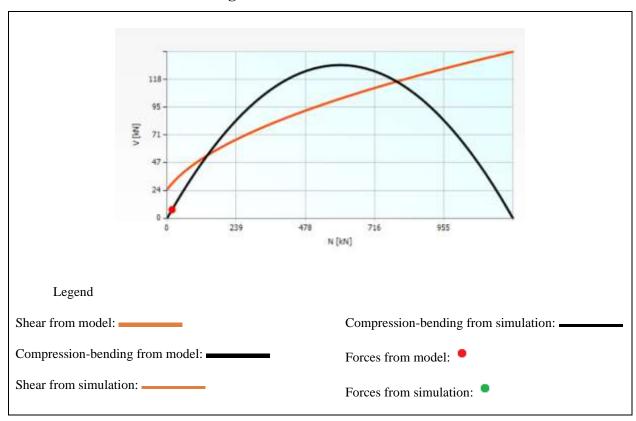


Figure V 6 wall 7 Resistance domain diagram

For the calculation domain look table 3 and 4 on the APPENDIX II

V.5.3.3 Plan deformed shape

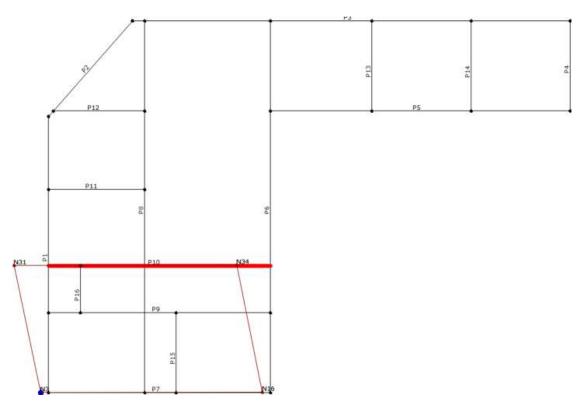


Figure V 7 Plan deformed shape for X direction

V.5.3.4 Pushover curves (analysis n. 4)

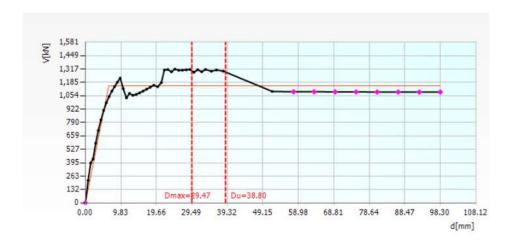


Figure V 8 Pushover curves for X direction

V.5.4 Seismic analysis no. 5 Direction Y

Wi will only show the walls that are most vulnerable.

V.5.4.1 Seismic analysis no. 5 Wall 8

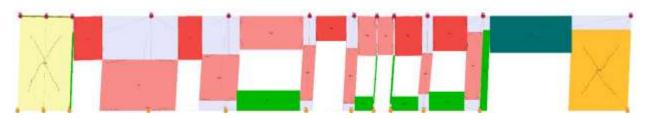


Figure V 9 wall 8 Resistance domain diagram

V.5.4.1.1 General data

Table V 23 wall 8 deformations result for Y direction

Code	Technical standards 2018
Wall	8
Piers	88
Analysis	5
Substep	14/15
Limit Drift	0.005
Drift in Step	0.003
Damage condition	Shear damage

V.5.4.1.2 Input data from Model

Table V 24 wall 8 input conditions

- 10-11 / - 1 / 10-11		
Typology	Common masonry	
The material's condition	Existing	
Constitutive law	Irregular masonry (Turnsek/Cacovic)	

V.5.4.1.2.1 Geometry

Table V 25 wall 8 geometry

Name	Value	Description
h [m]	2.250	Height (deformable portion)
1 [m]	1.848	Length
t [m]	0.600	Thickness

V.5.4.1.2.2 Masonry: rubble

Table V 26 wall 8 mechanical characteristics

	table (20 mail o modification)				
Name	Value	Description			
fm [kN/m2]	2,000.00	Average compressive strength of masonry			
τ [kN/m2]	35.00	Average shear strength in the absence of normal stresses			
CF	1.35	Confidence factor			

V.5.4.1.3 Applied forces (from pushover analysis)

Table V 27 wall 8 applied forces for Y direction

Name	Value	Description	
N [kN]	94	Axial force	
Vd [kN]	63	Shear	
M top [kNm]	71	Upper section bending moment	
M bottom [kNm]	71	Lower section bending moment	

V.5.4.1.4 Resistance forces and verification

Table V 28 wall 8 resistance forces verifications for Y direction

Name	Value	Description
N [kN]	94	Axial force (coincident with applied)
Vf [kN]	72	Shear (principle bending) calculated by interpolation on the resistance domain
Vs [kN]	63	Shear (principal shear)

		calculated by interpolation on the resistance domain	
Vr [kN]	63	Shear (minimum between Vf and Vs)	
Vd/Vr	1.000	Safety factor	

V.5.4.1.5 Resistance domain diagram

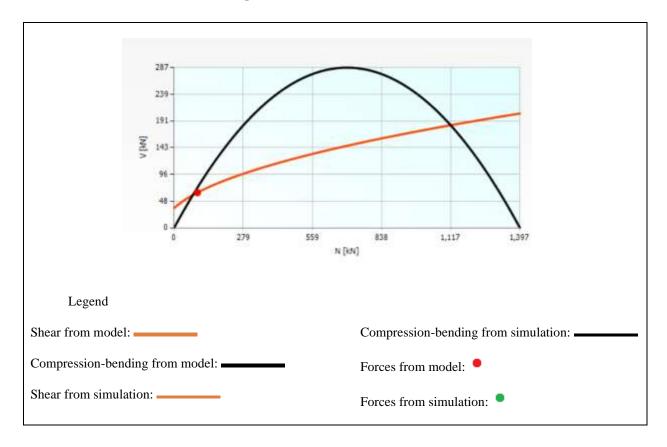


Figure V 10 wall 8 Resistance domain diagram

For the calculation domain look table 5 and 6 on the APPENDIX II

V.5.4.2 Plan deformed shape

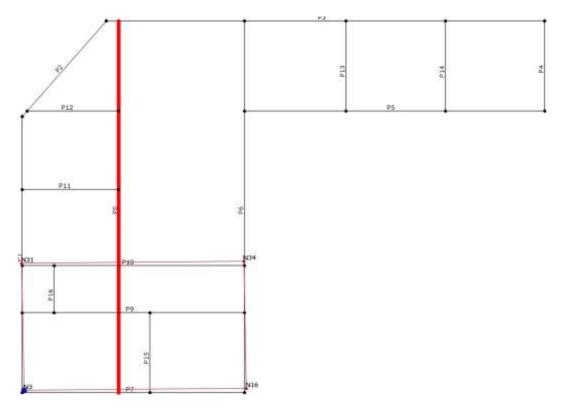


Figure V 11 Plan deformed shape Y direction

V.5.4.3 Pushover curves (analysis n. 4)

The mechanics-based approaches construct the strength, stiffness, and deformation parameters of single masonry walls using simplified structural mechanics concepts, and then combine those parameters to create the building's capacity curve.

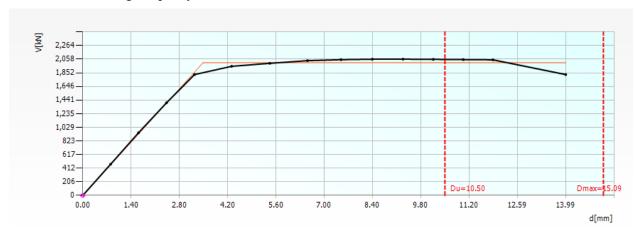


Figure V 12 Pushover curves Y direction

V.6 ASSESSMENT OF THE PERFORMANCE POINT (X DIRECTION)

The intersection of the demand spectrum and capacity curve is a critical point that determines the seismic performance of a structure. If the capacity curve lies above the demand spectrum, it indicates that the structure has sufficient strength to withstand the expected seismic forces. Conversely, if the capacity curve intersects or falls below the demand spectrum, it suggests that the structure may experience significant damage or failure during an earthquake.

To assess the performance point, we have seen choosing two different methods (graphical, and empirical).

All calculation details are in the table 7, 8, 9,10 Appendix II

V.6.1 Graphical "using excel table":

The method used is the (N2) approach as described in the seismic analysis part:

V.6.1.1 SDOF to MDOF

The capacity curve can be transformed into an equivalent capacity curve relating the (shear, displacement) of a structure to a single degree of freedom. For all calculation look table 8 **Appendix II**

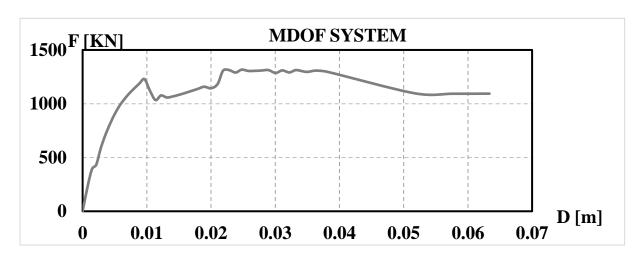


Figure V 13 MDOF capacity curve for X direction

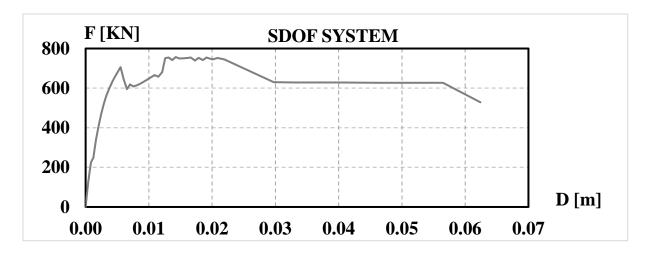


Figure V 14 SDOF capacity curve for X direction

V.6.1.2 The bi-linear equivalent capacity curve

The bi-linear equivalent capacity curve represents dual stiffness behaviour in a structure: elastic until yielding and post-yield with reduced stiffness. It indicates ultimate strength, ductility, and seismic performance. And characterized by the lateral resistance represented by a horizontal plateau bounded by the elastic displacement and the ultimate displacement at the top of the building. see table 7 **Appendix II.**

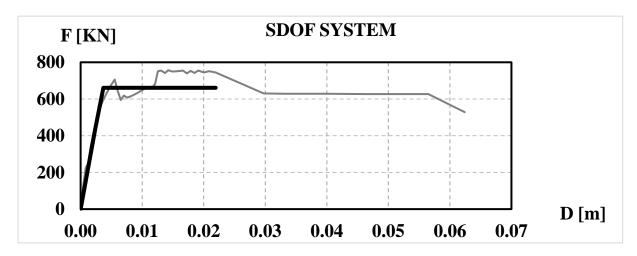


Figure V 15 bi-linear equivalent capacity curve X direction

V.6.1.3 The intersection

The intersection of the bi-linear equivalent capacity curve and the Acceleration-Displacement Response Spectrum (ADRS) demand is determined through a systematic analysis process. First, the bi-linear capacity curve is constructed, considering the structural properties such as stiffness, strength, and energy dissipation. Simultaneously, the ADRS demand curve is developed, representing the expected ground motion intensities. Plotting both curves on the same graph allows for the identification of the intersection point. By analysing the location of this point relative to the different segments of the bi-linear curve, the structure's ability to withstand the seismic demand can be assessed. If the intersection lies below the post-yield segment, it signifies that the structure can resist the seismic forces without exceeding its capacity, indicating a favorable (Transport, 2019) safety margin and reliable seismic performance.

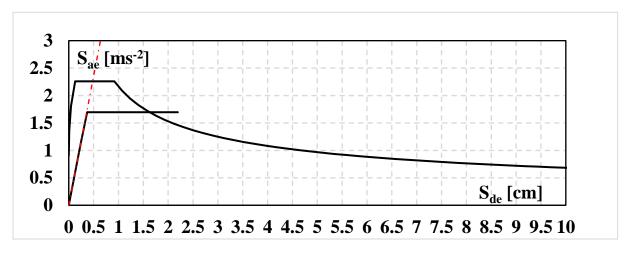


Figure V 16 intersection of the capacity curve and the demand X direction

V.6.2 Numerical:

According to (Sergio Lagomarsino, 2006)the performance point, Sd, in terms of displacement, is determined by a closed analytical function as a function of the demand and capacity curves:

$$Sd * = \begin{cases} \left[1 + \left(\frac{Sae(T)}{ay} - 1\right)\left(\frac{Tc}{T}\right)\right] dy &, & T < Tc \text{ and } \frac{Sae(T)}{ay} > 1, \\ \left(\frac{Sae(T)}{ay}\right) dy &, & Tc \le T < TD \text{ or } \frac{Sae(T)}{ay} < 1, \\ \left(\frac{Sae(TD)TD^2}{4\pi^2}\right) &, & T \ge TD \end{cases}$$

Or even by:

$$Sd * = \begin{cases} \left[1 + (q-1)\left(\frac{Tc}{T}\right)\right] dy &, & T < Tc \text{ and } q > 1 \text{ ,} \\ qdy &, & Tc \leq T < TD \text{ or } q < 1 \\ \left(\frac{Sae(TD)TD^2}{4\pi^2}\right) &, & T \geq TD \end{cases}$$

With: $q = \frac{du}{dy}$

Table V 29 performance point X direction numerical method data

T [sec]	TC [sec]	Sae [m/s ²]	ay [m/s ²]	Dy [m]	Sd*[m]
0.29	0.4	6.1	1.7	0.0037	0.01684

V.6.3 Finds

Using different methods to assess the performance point gave an approximate value which around "1.7cm"

V.7 ASSESSMENT OF THE PERFORMANCE POINT (Y DIRECTION)

V.7.1 Graphical "using excel table"

The method used is the (N2) approach as described in the seismic analysis part:

all calculation details are in the table 11, 12, 13,14 Appendix II

V.7.1.1 SDOF to MDOF

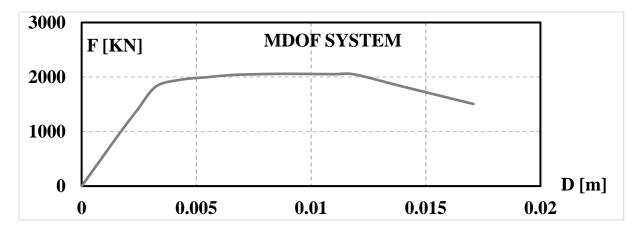


Figure V 17 MDOF capacity curve Y direction

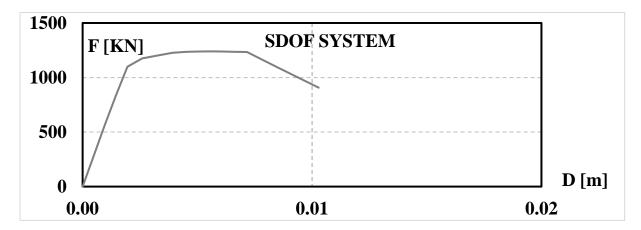


Figure V 18 SDOF capacity curve Y direction

V.7.1.2 The bi-linear equivalent capacity curve

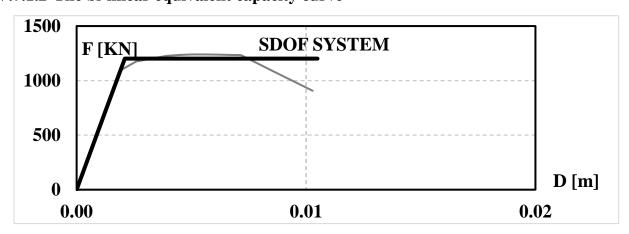


Figure V 19 bi-linear equivalent capacity curve Y direction

V.7.1.3 The intersection

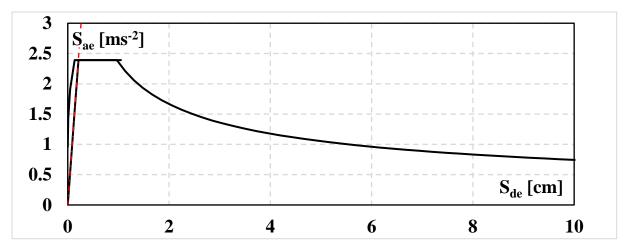


Figure V 20 intersection of the capacity curve and the demand Y direction

V.7.2 Numerical

According to (Sergio Lagomarsino, et al,2006), performance point, Sd, in terms of displacement, is determined by a closed analytical function as a function of the demand and capacity curves:

$$Sd * = \begin{cases} \left[1 + \left(\frac{Sae(T)}{ay} - 1\right)\left(\frac{Tc}{T}\right)\right] dy &, & T < Tc \text{ and } \frac{Sae(T)}{ay} > 1 \text{ ,} \\ \left(\frac{Sae(T)}{ay}\right) dy &, & Tc \leq T < TD \text{ or } \frac{Sae(T)}{ay} < 1 \\ \left(\frac{Sae(TD)TD^2}{4\pi^2}\right) &, & T \geq TD \end{cases}$$

Or even by:

$$Sd * = \begin{cases} \left[1 + (q-1)\left(\frac{Tc}{T}\right)\right]dy & , & T < Tc \text{ and } q > 1 \text{ ,} \\ qdy & , & Tc \leq T < TD \text{ or } q < 1 \\ \left(\frac{Sae(TD)TD^2}{4\pi^2}\right) & , & T \geq TD \end{cases}$$

With:
$$q = \frac{du}{dv}$$

Table V 30	performance	point Y	direction	numerical	method data

T [sec]	TC [sec]	Sae [m/s ²]	ay [m/s ²]	Dy [m]	Sd*[m]
0.186	0.4	6.1	2.39	0.0021	0.0093

V.7.3 Finds:

Using different methods to assess the performance point gave an approximate value which around "1cm"

V.8 VULNERABILITY ANALYSIS:

Since vulnerability modelling is typically confined by a lack of knowledge and information, there may be an important amount of uncertainty throughout the assessment process. The exposure and vulnerability models are mostly affected by epistemic uncertainties, whereas the definition of the seismic hazard is affected by both epistemic and aleatory uncertainty. A risk assessment study's overall findings and conclusions may be significantly impacted by the use of various input models, such as ground motion models, structural capacity models, or repair cost data. Therefore, regardless of the methodology used, identifying, quantifying, and incorporating the uncertainties associated with each input parameter is one of the most crucial parts in the creation of a seismic vulnerability model.

V.8.1 Fragility and vulnerability functions

The terms fragility functions and vulnerability functions, which are both related to seismic damageability, must be distinguished in this context. An intensity measure, is used to define a seismic fragility function, which quantifies the probability that some unwanted event or physical damage will occur as a function of the intensity measure. As a function of a structure independent intensity measure, a seismic vulnerability function determines the economic loss, the damage factor defined as the repair to replacement cost ratio. For instance, a fragility function can indicate the probability that a structure will collapse given a certain amount of trembling. The damage factor (in terms of repair to replacement cost ratio) for the building given the intensity of the shaking would be provided by analogous vulnerability functions.

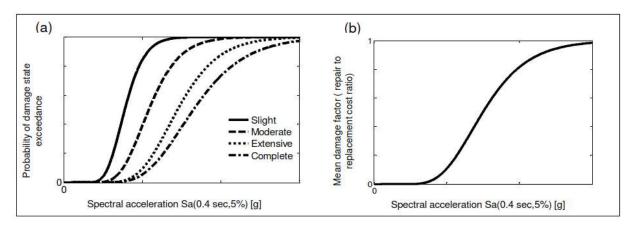


Figure V 21 fragility curves stages

The fragility functions may also depend on a structural response parameter, such as the inter-storey drift ratio or the roof displacement transformed to spectral displacement (Kircher et al. 1997a). They are described as a displacement fragility function in this instance. These fragility functions are a crucial part of the seismic vulnerability modelling, which uses displacements to gauge the severity of damage caused by earthquakes.

According to Rossetto and Elnashai (2005), fragility and vulnerability functions can be derived from empirical data, expert judgment, analytical models, or any combination of these approaches. There are uncertainties in the evaluation processes and data used regardless of the method employed to anticipate the seismic damageability. They consist of measurements with observational uncertainty:

- the analysis and database's quality are inconsistent.
- the ground's motion is variable.
- uncertainty over the experts' opinions.
- the strength and stiffness of structural materials and components are subject to ambiguity because of model simplification.
- Uncertainties in the definition of the damage states, variances in the geometry and material qualities of the structures, and their seismic demand and capability.

V.8.1.1 Analytical functions for fragility curve

according to (Giovinazzi, 2005), The probability of a particular damage state occurring or exceeding a given damage state for a structural response parameter (such as spectral inelastic displacement demand) is typically given in the form of a lognormal distribution in analytical displacement

fragility functions. The following equation describes the conditional possibility of achieving a specific damage state, DS, given the spectral displacement, Sd:

$$p [DS|Sd] = \Phi \left[\frac{1}{\beta_{dS}} ln \left(\frac{Sd}{\overline{S}_{d}.Ds} \right) \right]$$

$$Bds = \sqrt{CONV(\beta_c,\beta_d)^2 + \beta t^2}$$

Or even: $B_{ds} = B_k$ and $B_k = 0.4 \ln(q)$

Damage limit states \mathbf{Sd} , $\mathbf{k}(\mathbf{k} = 1/4)$ are identified directly on the capacity curve as a consequence of the yielding \mathbf{dy} and the ultimate displacements \mathbf{du} to determine the damage suffered by the structures.

$$\begin{cases}
DS1 = 0.7 \text{ dy} \\
DS2 = 1.5 \text{ dy}
\end{cases}$$

$$DS3 = 0.5(\text{du} + \text{dy})$$

$$DS4 = \text{du}$$

q: is the behaviour factor behaviour factor and du; du are the displacements

Recent vulnerability modelling has a heavy emphasis on analytical techniques. Analytical methods take into account all uncertainties. However, analytical techniques must require substantial computational effort.

Sd,DS is the median spectral displacement value at which the building enters the damage state DS.

 β_{dS} stand for the natural logarithm of spectral displacement standard deviation for damage state DS.

 Φ stands for the standard normal cumulative distribution function. Any given damage state's total variability comes from three main sources, including the variation in the **capacity** model βC .

the variability in the **demand** model βd . and the variability in the **damage** state threshold from the damage model βt .

By performing seismic demand studies on capacity curves and calculating the probability that certain damage states would be reached or exceeded, the convolution (CONV) is assessed.

Ps1 is the fragility curve for the probability of damage state 1 and so on ..etc

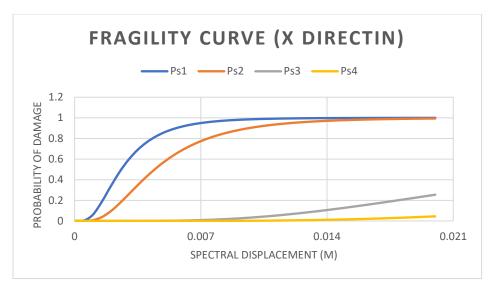


Figure V 22 fragility curve (X direction)

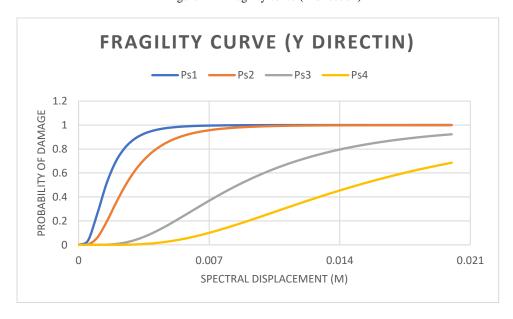


Figure V 23 fragility curve (Y direction)

V.8.1.2 Damage distribution of the studied structure

A vulnerability histogram for a structure and its damages due to seismic demand provides insights into the distribution of vulnerability levels and the resulting damages caused by earthquakes. This assessment involves evaluating various parameters such as construction materials, structural design, age, maintenance, and location to determine the vulnerability of the structure. By assigning vulnerability levels, such as low, medium, and high, or numerical values, a vulnerability profile can be created. Additionally, considering the seismic demand or the forces imposed on the structure during an earthquake, can be conducted to determine the expected damages.

Making reference to the EMS-98 scale wish is the macroseismic method and the mechanical method to best understanding of the damage level is summarised in the table 31 form (Sergio Lagomarsino, et al,2006).

Table V 31. Correspondence between damage level \mathbf{D}_{Sk} and damage grades \mathbf{D}_{k} related to structural and non-structural damage, (Sergio Lagomarsino, et al,2006).

D_{Sk}	D_k	Structural (SD) and non-structural (N-SD) damage
Slight (D _{S1}) Moderate (Ds2) Extensive (Ds3) Complete (Ds4)	Slight (D ₁) Moderate (D _{S2}) Heavy (D ₃) Very heavy (D ₄) Destruction (D ₅)	No SD slight N-SD Slight SD moderate N-SD Moderate SD heavy N-SD Heavy SD very heavy N-SD Very heavy SD

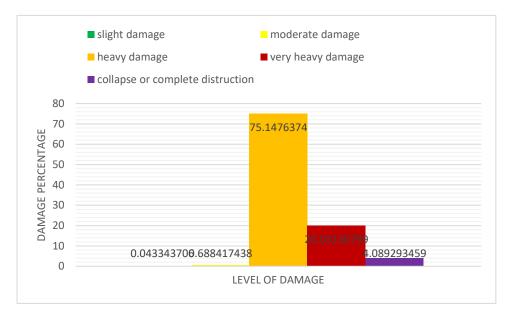


Figure V 24 damage histogram (X direction)

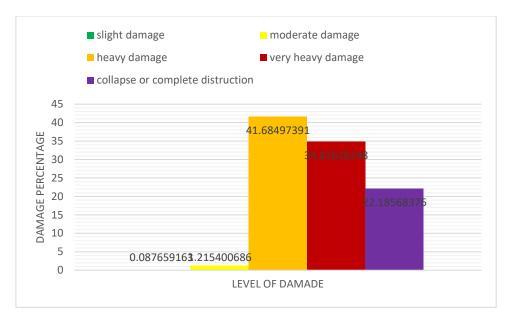


Figure V 25 Vulnerability histogram (Y direction)

V.8.1 Finds

Upon conducting an extensive seismic and vulnerability analysis of the masonry structure, it has become evident that the seismic behaviour and vulnerability of the structure exhibit notable variations across its different sides. The analysis has provided valuable insights, revealing that while the structure as a whole has not suffered from complete or irreparable damage, specific elements within it have experienced severe degradation. In light of these findings, it is imperative to implement targeted repair and rehabilitation measures to address the areas that have been adversely affected.

V.9 CONCLUSION

We have undertaken an extensive evaluation of the masonry structure's behaviour when subjected to seismic forces, while also investigating its susceptibility to damage. The chapter encompasses a comprehensive range of crucial aspects related to seismic spectrum assessment. It commences with a meticulous calculation of the response spectrum, ensuring strict adherence to the Algerian seismic regulations that govern the structural safety within the region.

Moreover, we delve into the methodology of pushover analysis, providing a meticulous and detailed description of the structure's response under the influence of seismic loads. Stringent data validation techniques, including domain resistance calculation, are employed to establish the utmost accuracy and reliability of the analysis outcomes.

The subsequent presentation of results showcases an in-depth examination of the seismic analysis, featuring comprehensive result details, an illustrative results legend, and detailed findings from the seismic analyses conducted for both the X and Y directions. These findings offer invaluable insights into the structure's behaviour, pinpointing areas of concern and potential vulnerability, thus empowering decision-makers with critical information.

In addition to the seismic analysis, the chapter encompasses a meticulous vulnerability analysis that entails the development of fragility and vulnerability functions. These functions are meticulously designed to assess the likelihood and severity of damage, allowing for a comprehensive understanding of the structure's vulnerability. The findings derived from this analysis not only enhance our comprehension of the structure's behaviour but also serve as a foundation for proposing effective mitigation measures.

Considering the outcomes and recommendations derived from the seismic and vulnerability analyses, it is crucial to propose targeted solutions to address the identified vulnerabilities. These solutions may encompass the implementation of retrofitting techniques, reinforcing critical structural elements, or considering architectural modifications to enhance the structure's resilience in the face of potential seismic events. By embracing and implementing these recommended measures, stakeholders can ensure the long-term safety, stability, and robustness of the masonry structure, thus safeguarding lives and preserving invaluable assets.

CHAPTER VI REINFORCEMEN ANALYSIS

VI.1 INTRODUCTION

Masonry structure reinforcement is the process of strengthening and enhancing the load-bearing capacity of existing masonry buildings or structures. It involves the application of various techniques such as steel reinforcement, fiber reinforcement, composite materials, and grouting or injection. These methods aim to improve the structural integrity, durability, and resistance of the masonry to external forces. The choice of reinforcement technique depends on factors such as the condition of the masonry, the desired level of reinforcement, and the specific load requirements of the structure.

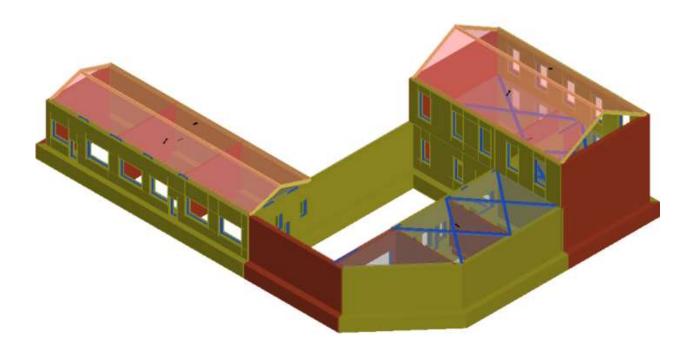


Figure VI 1 3d view after reinforcement

VI.2 Types of reinforcement used

Our masonry structures is often need to require reinforcement. Two common methods of masonry structure reinforcement are the use of wall frames and Fiber-Reinforced Cementitious Matrix (FRCM) systems.

VI.2.1 Wall frames

Wall frames are typically used as an external reinforcement system for masonry structures. They consist of steel or timber frames that are attached to the existing masonry walls. The frames are designed to bear a significant portion of the applied loads, such as wind or seismic forces, and transfer them to the foundation.

The installation of wall frames involves attaching horizontal and vertical members to the masonry wall, creating a framework that distributes the loads more evenly. These frames provide additional strength, stability, and ductility to the masonry structure, reducing the risk of failure under extreme conditions.

VI.2.2 Frcm systems

Fiber-Reinforced Cementitious Matrix (FRCM) systems are a relatively new technology used for the reinforcement of masonry structures. FRCM comprises high-strength fibers embedded in a cementitious matrix. The fibers can be made of materials like carbon, glass, or basalt, while the matrix is typically a cement-based mortar.

FRCM systems are applied directly to the masonry surface, providing both flexural and shear reinforcement. The fibers enhance the tensile strength and ductility of the masonry, while the cementitious matrix acts as a bonding agent between the fibers and the masonry substrate. This combination improves the overall structural performance and resists cracking, deformation, and delamination.

The installation of FRCM systems involves cleaning and preparing the masonry surface, applying a primer, and then applying multiple layers of the FRCM composite. Once cured, the FRCM becomes an integral part of the masonry structure, providing enhanced strength and durability.

VI.3 REINFORCEMENT TYPE CHARACTERISTICS

VI.3.1 Reinforcements frcm (walls)

Table VI 1 Block mechanical caracteristics

Name	Masonry	Masonry type	Exposure class	Fbm [n/m2]	Fbtm [n/m2]	Dist. Application [m]
Frcm (Rubble Masonry Wall)	Rubble	Limestone or leccese stone masonry	External	4.40e+06	4.00e+05	0.00e+00
Frcm (Stone Wall)	Stone	Brick masonry	Internal	2.20e+06	2.00e+05	0.00e+00

VI.3.1.1 Piers

Table VI 2 piers element type of reinforcement

Name	Effect typology	Application	Bending anchor
FRCM (Rubble Masonry Wall)	Shear	Double side	Efficacious
FRCM (Stone Wall)	Shear	Double side	Efficacious

Table VI 3 Piers FRCM geometrics

Name	tf [mm]	ηа	Ef [N/m2]
FRCM (Rubble Masonry Wall)	0.062	0.80	6.00E+10
FRCM (Stone Wall)	0.062	0.90	6.00E+10

Table VI 4 FRCM on piers mechanical characteristics

Name	ε (α) lim,conv	σ (α) lim,conv [N/mm2]	ε fd [%]	f fd /f fdd [N/m2]
FRCM (Rubble Masonry Wall)	2.80000	1,680.00000	1.49333	1.26E+20
FRCM (Stone Wall)	2.80000	1,680.00000	1.68000	1.01E+15

VI.3.1.2 Spandrel beam

Table VI 5 spandrel element type of reinforcement

Name	Effect typology	Application	Bending anchor	
FRCM (Rubble Masonry Wall)	Shear	Double side	Efficacious	
FRCM (Stone Wall)	Shear	Single side	Efficacious	

Table VI 6 spandrel FRCM geometrics

Name	tf [mm]	ηа	Ef [N/m2]	
FRCM (Rubble Masonry Wall)	0.062	0.80	6.00E+10	
FRCM (Stone Wall)	0.062	0.90	6.00E+10	

Table VI 7 FRCM on spandrel mechanical characteristics

Name	ε (α) lim,conv [%]	σ (α) lim,conv [N/mm2]	ε fd [%]	f fd /f fdd [N/m2]
FRCM (Rubble Masonry Wall)	2.80000	1,680.00000	1.49333	1.26E+20
FRCM (Stone Wall)	2.80000	1,680.00000	1.68000	1.01E+15

VI.3.2 Reinforcements wall (Steel frames)

Table VI 8 wall frame reinforcement characteristics for walls

Material	Profile	Area [m2]	J [m4]	W [m3]
S 235 (t <= 40mm)	IPE 180	2.40E-03	1.32E-05	1.46E-04
S 235 (t <= 40mm)	IPE 140	1.64E-03	5.41E-06	7.73E-05

VI.3.3 Reinforcements horizontal elements (Steel frame "tie rod ")

Table VI 9 tie rod reinforcement characteristics for horizontal elements

Category	Profile	Material	Area [m2]	J [m4]	W [m3]
Floor	HEA 180	S 235 (t <= 40mm)	3.88E-03	1.67E-05	2.20E-04
Floor	HEA 160	S 235 (t <= 40mm)	4.53E-03	2.51E-05	2.94E-04

VI.4 MASONRY WITH FRCM REINFORCEMENT

VI.4.1 Compression bending

For the calculation of the moment of bending resisting moment it is possible to carry out a simplified calculation (see APPENDIX 1 of the CNR-DT 215/2018), on which the resisting moment of calculation can be evaluated by assuming a stress diagram of constant compression stress equal to $a_m \, f_{md}$, extended to a portion of deep section βy_n , being y_n the distance of the neutral axis from the compressed end. a_m and b are two reduction coefficients, determined on empirical tests, described in the CNR -DT 215/2018.

In the case of crisis due to the achievement of the ϵ_{mu} deformation at the compressed end ($\epsilon_{m} = \epsilon_{mu}$) and of the neutral axis that cuts the section, the resistant moment of calculation is:

$$M_{Rd}(N_{sd}) = \frac{\alpha_m \beta f_{md} t y_n}{2} (H - \beta y_n) + \frac{\varepsilon_{mu}}{y_n} \frac{(d_f - y_n)^2}{12} E_f t_{2f} (2y_n + 4d_f - 3H)$$

being y_n the distance of the neutral axis from the compressed end, given by:

$$y_{n} = \frac{N_{sd} - E_{f}t_{2f}d_{f}\varepsilon_{mu} + \sqrt{{N_{sd}}^{2} + 2E_{f}t_{2f}d_{f}\varepsilon_{mu}\left(\alpha_{m}\beta f_{md}d_{f} - N_{sd}\right)}}{2\alpha_{m}\beta f_{md}t - E_{f}t_{2f}\varepsilon_{mu}}$$

Note the deformed configuration, it is necessary to verify that the maximum deformation of the reinforcement is less than the ultimate deformation.

In the case that the deformation of the reinforcement exceeds the maximum, it means that the hypothesis previously made (achievement of the ultimate deformation of the masonry) is not true, and therefore we proceed by assuming that the crisis occurs due to the achievement of the deformation ϵ_{fd} in the reinforcement ($\epsilon_{f} = \epsilon_{fd}$) and of neutral axis that cuts the section. In this case, the resistant moment of calculation is:

$$M_{Rd}(N_{sd}) = \frac{\alpha_m \beta f_{md} t y_n}{2} (H - \beta y_n) + \varepsilon_{fd} E_f t_{2f} \frac{d_f - y_n}{12} (2y_n + 4dy_f - 3H)$$

being y_n the distance of the neutral axis from the compressed end, given by:

$$y_n = \frac{\varepsilon_{fd} E_f t_{2f} d_f + 2N_{sd}}{2\alpha_m \beta f_{md} t + \varepsilon_{fd} E_f t_{2f}}$$

where:

H is the length of the wall (section height);

t is the wall thickness (section width);

t_{2f} is the total equivalent thickness of the fibers applied on the two sides;

d_f is the distance between the compressed end and the fiber of the reinforcement furthest away from it;

N_{sd} is the normal compressive stress applied (possibly zero in the case of the floor strips).

VI.4.2 Shear

With reference to paragraph 4.1.1 of CNR-DT 215/2018, the shear strength of the reinforced wall (V_s) is calculated as the sum of the contribution of the non-reinforced masonry (V_t) , evaluated in accordance with the Current legislation for non-reinforced walls that are in crisis due to traction shear, and that of the reinforcement (v_{tf}) .

The latter is evaluated with the following equation:

$$V_{t,f} = \frac{1}{\gamma_{Rd}} \, \eta_f t_{vf} l_f \alpha_t \varepsilon_{fd} E_f$$

where:

 γ _{Rd} it is a partial model factor to which value 2 is attributed, to the state of current knowledge;

n_f is the total number of reinforcement layers arranged on the sides of the wall;

 t_{vf} is the equivalent thickness of a layer of mesh with fibers arranged in a direction parallel to the shear force;

 l_f is the calculation dimension of the reinforcement measured orthogonally to the shear force, and in any case it cannot be assumed to be greater than the dimension H of the wall.

 ϵ_{fd} is the calculation deformation of the reinforcement;

E_f is the elastic modulus of the reinforcement.

The a_t coefficient takes into account the reduced extensional resistance of the fibers when in shear. In the absence of proven experimental results, it can be assigned the value 0.80.

In the presence of fibers orthogonal to the direction of the shear and effectively anchored, it must also be

verified that the effective shear does not exceed the following diagonal crushing value of the masonry:

$$V_{s,lim} = 0.25 f_{md} t d_f$$

where:

t is the thickness of the wall;

 f_{md} is the design compressive resistance of the masonry;

 d_f is the distance between the compressed end of the masonry and the extreme of the FRCM reinforcement subject to traction

VI.5 STATIC REINFORCEMENT VERIFICATIONS

Retrofitting the most affected element of a masonry structure is a critical step in reinforcing the overall stability and performance of the building. The identification of the most vulnerable element, such as a weakened wall, is crucial to ensure targeted reinforcement. Proper retrofitting not only addresses existing weaknesses but also improves the structure's ability to withstand external forces and extends its service life.

For this we have used steel frames for the weakened elements (Pierses) and for the openings, and so far, we have applied the FRCM for the rest of walls in wish we did not apply steel frames.

VI.5.1 Wall: 1

Table VI 10 wall 1 static state after reinforcement

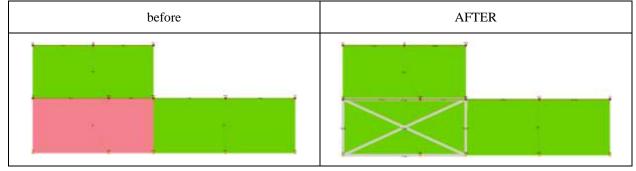


Table VI 11 wall 1slanderness and eccentrecity verification after reinforcement

Pier	ho	t	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
	[m]	[m]					
1	4.52E+00	4.00E-01	11.300	0.056	0.056	0.056	Yes
2	4.52E+00	4.00E-01	11.300	0.118	0.075	0.248	Yes
89	4.36E+00	4.00E-01	10.900	0.055	0.055	0.055	Yes

Table VI 12 wall 1 vertical load bearing verification after reinforcement

		Тор			Middle				Bottom				
Pie r	Nd	F	Nr	Nd/ Nr	Nd	F	Nr	Nd Nr		F	Nr	Nd/ Nr	Satisf ied
1	5.41E +04	0.6 53	6.58E +05	0.08	1.78E +05	0.6 53	6.58E +05	0.2	7 4.11E +05	0.6 53	6.58E +05	0.62 4	Yes
2	2.75E +05	0.2 47	5.85E +05	0.47	5.63E +05	0.6 00	1.42E +06	0.39	9 8.51E +05	0.5 09	1.20E +06	0.70 8	Yes
89	1.55E +05	0.6 71	6.76E +05	0.22 9	3.49E +05	0.6 71	6.76E +05	0.5 6	1 5.74E +05	0.6 71	6.76E +05	0.85	Yes

VI.5.2 Wall: 6

Table VI 13 wall 6 static state after reinforcement

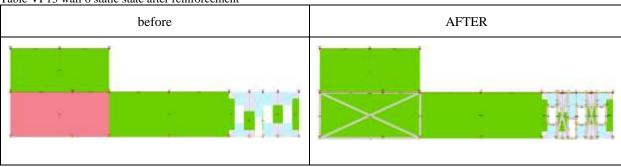


Table VI 14 wall 6 slanderness and eccentrecity verification after reinforcement

Pier	ho	t	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
	[m]	[m]					
33	4.52E+00	4.00E-01	11.300	0.056	0.056	0.056	Yes

2.4	4.525.00	5 50E 01	0.210	0.041	0.041	0.041	37
34	4.52E+00	5.50E-01	8.218	0.041	0.041	0.041	Yes
35	4.52E+00	5.50E-01	8.218	0.041	0.041	0.041	Yes
36	4.52E+00	5.50E-01	8.218	0.041	0.041	0.041	Yes
37	4.52E+00	5.50E-01	8.218	0.041	0.041	0.041	Yes
38	4.52E+00	5.50E-01	8.218	0.041	0.041	0.041	Yes
94	4.63E+00	5.00E-01	9.260	0.046	0.046	0.046	Yes
95	4.36E+00	4.00E-01	10.900	0.055	0.055	0.055	Yes

Table VI 15 wall 6 vertical load bearing verification after reinforcement

		Top				Middle	e		I	Bottom	ı		
Pie r	Nd	F	Nr	Nd/ Nr	Nd	F	Nr	Nd/ Nr	Nd	F	Nr	Nd/ Nr	Satisf ied
33	1.40E +05	0.6 53	6.58E +05	0.21	3.74E +05	0.6 53	6.58E +05	0.56 8	6.07E +05	0.6 53	6.58E +05	0.92	Yes
34	1.44E +02	0.7 74	1.24E +05	0.00	6.89E +02	0.7 74	1.24E +05	0.00 6	1.43E +04	0.7 74	1.24E +05	0.11 6	Yes
35	0.00E +00	0.7 74	2.34E +05	0	6.98E- 01	0.7 74	2.34E +05	0.00	1.53E +04	0.7 74	2.34E +05	0.06 5	Yes
36	0.00E +00	0.7 74	1.47E +04	0	7.76E- 02	0.7 74	1.47E +04	0.00	9.64E +02	0.7 74	1.47E +04	0.06 6	Yes
37	0.00E +00	0.7 74	2.19E +05	0	4.13E- 01	0.7 74	2.19E +05	0.00	1.38E +04	0.7 74	2.19E +05	0.06	Yes
38	6.31E +01	0.7 74	1.46E +05	0.00	1.53E +02	0.7 74	1.46E +05	0.00	1.63E +04	0.7 74	1.46E +05	0.11	Yes
94	4.79E +04	0.7 37	2.26E +06	0.02	2.29E +05	0.7 37	2.26E +06	0.10	6.03E +05	0.7 37	2.26E +06	0.26 7	Yes
95	1.65E +05	0.6 71	6.76E +05	0.24	3.74E +05	0.6 71	6.76E +05	0.55	5.99E +05	0.6 71	6.76E +05	0.88 6	Yes

VI.5.3 Wall: 7

Table VI 16 wall 7 static state after reinforcement

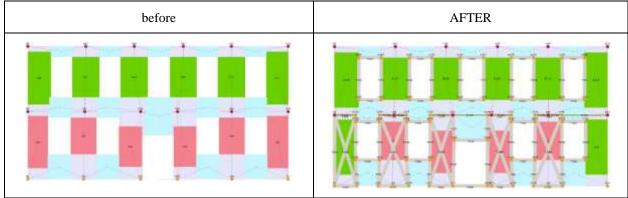


Table VI 17 wall 7 slanderness and eccentrecity verification after reinforcement

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
48	4.52E+00	6.00E-01	7.533	0.038	0.038	0.079	Yes
49	4.52E+00	6.00E-01	7.533	0.038	0.038	0.402	No
50	4.52E+00	6.00E-01	7.533	0.038	0.044	0.396	No
51	4.52E+00	6.00E-01	7.533	0.038	0.038	0.336	No
52	4.52E+00	6.00E-01	7.533	0.038	0.046	0.346	No
53	4.52E+00	6.00E-01	7.533	0.099	0.056	0.132	Yes
106	4.36E+00	6.00E-01	7.267	0.036	0.036	0.036	Yes
107	4.36E+00	6.00E-01	7.267	0.036	0.036	0.036	Yes
108	4.36E+00	6.00E-01	7.267	0.036	0.036	0.036	Yes
109	4.36E+00	6.00E-01	7.267	0.036	0.036	0.036	Yes
110	4.36E+00	6.00E-01	7.267	0.036	0.036	0.036	Yes
111	4.36E+00	6.00E-01	7.267	0.036	0.036	0.036	Yes

+04

3.80E

+04

3.73E

+04

3.57E

+04

4.57E

+04

5.26E

+04

6

10

7

10

8

10

9

11

0

11

1

09

0.8

09

0.8

09

8.0

09

0.8

09

8.0

09

+05

4.45E

+05

4.45E

+05

4.34E

+05

4.45E

+05

3.61E

+05

9

0.08

6

0.08

4

0.08

2

0.10

3

0.14

6

+05

7.78E

+04

7.71E

+04

7.45E

+04

8.55E

+04

9.51E

+04

09

0.8

09

0.8

09

0.8

09

0.8

09

0.8

09

+05

4.45E

+05

4.45E

+05

4.34E

+05

4.45E

+05

3.61E

+05

6

0.17

5

0.17

3

0.17

2

0.19

2

0.26

3

+05

1.18E

+05

1.17E

+05

1.13E

+05

1.25E

+05

1.38E

+05

09

0.8

09

0.8

09

0.8

09

0.8

09

0.8

09

+05

4.45E

+05

4.45E

+05

4.34E

+05

4.45E

+05

3.61E

+05

4

0.26

5

0.26

3

0.26

1

0.28

2

0.38

1

Yes

Yes

Yes

Yes

Yes

Table VI 18 wall 7 vertical load bearing verification after reinforcement

		Top				Middle	e		I	Bottom	1		
Pie r	Nd	F	Nr	Nd/ Nr	Nd	F	Nr	Nd/ Nr	Nd	F	Nr	Nd/ Nr	Satisf ied
48	2.33E +01	0.6 72	2.74E +05	0.00	1.11E +02	0.7 99	3.26E +05	0.00	3.84E +04	0.7 99	3.26E +05	0.11 8	Yes
49	8.23E- 01	0.0 00	0	0	1.19E +01	0.7 99	4.15E +05	0.00	3.42E +04	0.7 99	4.15E +05	0.08	Yes
50	1.38E +01	0.0 00	0	0	9.81E +01	0.7 80	3.65E +05	0.00	3.40E +04	0.7 99	3.74E +05	0.09	Yes
51	1.16E +00	0.0 00	0	0	1.69E +01	0.7 99	3.66E +05	0.00	3.32E +04	0.7 99	3.66E +05	0.09	Yes
52	2.95E +00	0.0 00	0	0	1.70E +01	0.7 75	4.03E +05	0.00	3.43E +04	0.7 99	4.16E +05	0.08	Yes
53	1.46E +05	0.5 65	2.40E +05	0.60 7	1.86E +05	0.7 43	3.16E +05	0.58 8	2.26E +05	0.6 29	2.68E +05	0.84	Yes
10	7.14E	0.8	3.79E	0.18	1.16E	0.8	3.79E	0.30	1.60E	0.8	3.79E	0.42	Yes

VI.5.4 Wall: 10

Table VI 19 wall 10 static state after reinforcement

before	AFTER

Table VI 20 wall 10 slanderness and eccentrecity verification after reinforcement

Pier	ho [m]	t [m]	ho/t	e1/t Bottom	e2/t Middle	e1/t Top	Satisfied
126	4.52E+00	5.00E-01	9.040	0.091	0.058	0.194	Yes
127	4.52E+00	5.00E-01	9.040	0.097	0.052	0.112	Yes
128	4.52E+00	5.00E-01	9.040	0.099	0.053	0.114	Yes
129	4.52E+00	5.00E-01	9.040	0.083	0.048	0.121	Yes
130	4.36E+00	5.00E-01	8.720	0.044	0.044	0.044	Yes
131	4.36E+00	5.00E-01	8.720	0.044	0.044	0.044	Yes
132	4.36E+00	5.00E-01	8.720	0.044	0.044	0.044	Yes
133	4.36E+00	5.00E-01	8.720	0.044	0.044	0.044	Yes
134	4.36E+00	5.00E-01	8.720	0.044	0.044	0.044	Yes
135	4.36E+00	5.00E-01	8.720	0.044	0.044	0.044	Yes

Table VI 21 wall 10 vertical load bearing verification after reinforcement

Table	VI ZI Wali	10 verti	icai ioau oc	aring vc	inication a	itel lell	HOICCHICH						
		Top				Middle)		-	Bottom	l		
Pie r	Nd	F	Nr	Nd/ Nr	Nd	F	Nr	Nd Ni		F	Nr	Nd/ Nr	Satisf ied
12 6	1.83E +05	0.4 12	8.14E +05	0.22 5	3.85E +05	0.7 06	1.39E +06	0.2 6		0.6 14	1.21E +06	0.48 4	Yes
12 7	1.76E +05	0.5 74	2.27E +05	0.77	2.01E +05	0.7 25	2.87E +05	0.7		0.6 03	2.39E +05	0.94 7	Yes

12 8	3.07E +05	0.5 71	4.01E +05	0.76 5	3.50E +05	0.7 22	5.07E +05	0.69 0	3.94E +05	0.6 00	4.21E +05	0.93 4	Yes
12 9	5.40E +04	0.5 57	1.66E +05	0.32 6	8.13E +04	0.7 37	2.19E +05	0.37	1.09E +05	0.6 31	1.88E +05	0.57 9	Yes
13 0	6.14E +04	0.7 56	3.03E +05	0.20	9.95E +04	0.7 56	3.03E +05	0.32	1.38E +05	0.7 56	3.03E +05	0.45	Yes
13 1	3.09E +04	0.7 56	3.37E +05	0.09	6.31E +04	0.7 56	3.37E +05	0.18 7	9.54E +04	0.7 56	3.37E +05	0.28	Yes
13 2	3.30E +04	0.7 56	3.43E +05	0.09 6	6.58E +04	0.7 56	3.43E +05	0.19	9.87E +04	0.7 56	3.43E +05	0.28 7	Yes
13	2.87E +04	0.7 56	3.43E +05	0.08	6.16E +04	0.7 56	3.43E +05	0.17 9	9.45E +04	0.7 56	3.43E +05	0.27 5	Yes
13 4	3.86E +04	0.7 56	4.69E +05	0.08	8.35E +04	0.7 56	4.69E +05	0.17 8	1.28E +05	0.7 56	4.69E +05	0.27	Yes
13 5	4.14E +04	0.7 56	1.64E +05	0.25	6.21E +04	0.7 56	1.64E +05	0.37 8	8.28E +04	0.7 56	1.64E +05	0.50	Yes

VI.6 SEISMIC VULNERABILITY ANALYSIS

After undergoing demand spectrum analysis and implementing the necessary reinforcement measures, the masonry structure should exhibit improved performance and enhanced resilience against seismic forces.

The reinforcement works, such as steel bracing, fiber wrapping, concrete jacketing, aim to increase the structure's strength, stiffness, and ductility. These measures help to redistribute and dissipate the forces generated during a seismic event, reducing the risk of structural failure and minimizing damage in the structure elements. The reinforced structure should demonstrate improved resistance to deformation, cracking, and displacement, providing a higher level of safety for occupants and preserving the integrity of the building.

VI.6.1 Results

Table VI 22 verification of the critical direction of the earthquake after reinforcement

No.	Seism dir.	Seismic load	Ecc.	Dmax ULS [m]	Du ULS [m]	q* ULS	ULS Ver.
1	+X	Uniform	0.00E+00	1.08E-03	2.77E-02	0.46	Yes
2	+X	Static forces	0.00E+00	2.16E-03	2.77E-02	0.85	Yes
3	-X	Uniform	0.00E+00	1.85E-03	3.55E-02	0.70	Yes
4	-X	Static forces	0.00E+00	5.83E-03	4.03E-02	1.39	Yes
5	+Y	Uniform	0.00E+00	1.43E-03	2.83E-02	0.32	Yes
6	+Y	Static forces	0.00E+00	2.73E-03	2.88E-02	0.64	Yes
7	-Y	Uniform	0.00E+00	1.44E-03	1.53E-02	0.36	Yes
8	-Y	Static forces	0.00E+00	2.73E-03	1.36E-01	0.66	Yes

Table VI 23 pushover critical direction of the earthquake after reinforcement

No.	Seism dir.	Seismic load	Ecc. [m]	αULS
1	+X	Uniform	0.00E+00	6.472
2	+X	Static forces	0.00E+00	3.512
3	-X	Uniform	0.00E+00	4.259
4	-X	Static forces	0.00E+00	2.153
5	+Y	Uniform	0.00E+00	6.876
6	+Y	Static forces	0.00E+00	4.178
7	-Y	Uniform	0.00E+00	4.570
8	-Y	Static forces	0.00E+00	4.557

VI.6.1.1 Seismic analysis Wall 10 for the X direction

Table VI 24 wall 10 dynamic state after reinforcement

Table VI 24 wan 10 dynamic state i	before	After
Limit Drift	0.005	0.010
Drift in Step	0.001	0.000
Damage condition	Shear damage	Undamaged

VI.6.1.1.1 General data

Table VI 25 wall 10 analysis damage results X direction after reinforcement

Code	Technical standards 2018
Wall	10
Piers	116
Analysis	4
Substep	2/32
Limit Drift	0.010
Drift in Step	0.000
Damage condition	Undamaged

VI.6.1.1.2 Input data from Model

Table VI 26 wall 10 input conditions

Typology	FRCM reinforced masonry
The material's condition	Existing
Constitutive law	Irregular masonry (Turnsek/Cacovic)

VI.6.1.1.2.1 Geometry

Table VI 27 wall 10 geometry

Name	Value	Description
h [m]	3.88E+00	Height (deformable portion)
1 [m]	8.00E+00	Length
t [m]	5.00E-01	Thickness

VI.6.1.1.2.2 Masonry: rubble

Table VI 28 wall 10 mechanical characteristics

Name	Value	Description
fm [N/m2]	2.00E+06	Average compressive strength of masonry
τ [N/m2]	3.50E+04	Average shear strength in the absence of normal stresses
CF	1.35	Confidence factor

VI.6.1.1.2.3 Reinforcement FRCM

Table VI 29 wall 10 reinforcement typology applied

Name	Value	Description
Effect typology	Shear	
Layers	2	Number of layers applied
Ef [N/m2]	6.00E+10	Young's modulus
tf [mm]	0.062	Equivalent thickness of the single layer of the FRCM system

VI.6.1.1.3 Applied forces (from pushover analysis)

Table VI 30 wall 10 applied forces for X direction after reinforcement

Name Name	Value	Description
N [N]	2.98E+05	Axial force
Vd [N]	6.88E+03	Shear
M top [Nm]	6.12E+04	Upper section bending moment
M bottom [Nm]	-8.79E+04	Lower section bending moment

VI.6.1.1.4 Resistance forces and verification

Table VI 31 wall 10 resistance forces verifications for X direction after reinforcement

Name	Value	Description
N [N]	2.98E+05	Axial force (coincident with applied)
Vf [N]	8.77E+04	Shear (principle bending) calculated by interpolation on the resistance domain
Vs [N]	4.38E+05	Shear (principle shear) calculated by interpolation on the resistance domain
Vr [N]	8.77E+04	Shear (minimum between Vf and Vs)
Vd/Vr	0.078	Safety factor

VI.6.1.1.5 Resistance domain diagram

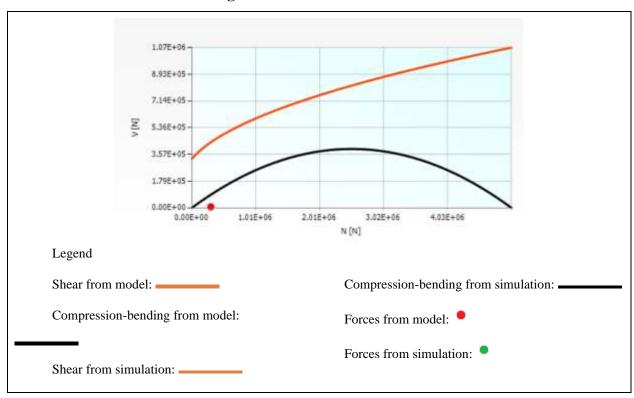


Figure VI 2 wall 10 Resistance domain diagram after reinforcement

For the calculation domain look the APPENDIX III

VI.6.1.2 Seismic analysis Wall 7 for the X direction

Table VI 32 wall 7 dynamic state after reinforcement

-	before	After
Limit Drift	0.010	0.010
Drift in Step	0.008	0.001
Damage condition	Incipient bending failure	Bending damage

VI.6.1.2.1 General data

Table VI 33 wall 7 analysis damage results X direction after reinforcement

Code	Technical standards 2018
Wall	7
Piers	72
Analysis	4
Substep	3/32
Limit Drift	0.010
Drift in Step	0.001
Damage condition	Bending damage

VI.6.1.2.2Input data from Model

Table VI 34 wall 7 input conditions

Typology	FRCM reinforced masonry
The material's condition	Existing
Constitutive law	Irregular masonry (Turnsek/Cacovic)

VI.6.1.2.2.1 Geometry

Table VI 35 wall 7 geometry

Name	Value	Description
h [m]	2.75E+00	Height (deformable portion)
l [m]	1.86E+00	Length
t [m]	6.00E-01	Thickness

VI.6.1.2.2.2 Masonry: rubble

Table VI 36 wall 7 mechanical characteristics

Name	Value	Description
fm [N/m2]	2.00E+06	Average compressive strength of masonry
τ [N/m2]	3.50E+04	Average shear strength in the absence of normal stresses
CF	1.35	Confidence factor

VI.6.1.2.2.3 Reinforcement FRCM

Table VI 37 wall 7 reinforcement typology applied

Name	Value	Description
Effect typology	Shear	
Layers	2	Number of layers applied
Ef [N/m2]	6.00E+10	Young's modulus
tf [mm]	0.062	Equivalent thickness of the single layer of the FRCM system

VI.6.1.2.3 Applied forces (from pushover analysis)

Table VI 38wall 7 applied forces for X direction after reinforcement

Name	Value	Description
N [N]	6.09E+04	Axial force
Vd [N]	2.13E+04	Shear
M top [Nm]	-4.60E+03	Upper section bending moment
M bottom [Nm]	-5.41E+04	Lower section bending moment

VI.6.1.2.4 Resistence forces and verification

Table VI 39 wall 7 resistance forces verifications for X direction after reinforcement

Name	Value	Description
N [N]	6.09E+04	Axial force (coincident with applied)
Vf [N]	2.13E+04	Shear (principle bending) calculated by interpolation on the resistance domain
Vs [N]	1.28E+05	Shear (principle shear) calculated by interpolation on the resistance domain
Vr [N]	2.13E+04	Shear (minimum between Vf and Vs)
Vd/Vr	1.000	Safety factor

VI.6.1.2.5 Resistance domain diagram

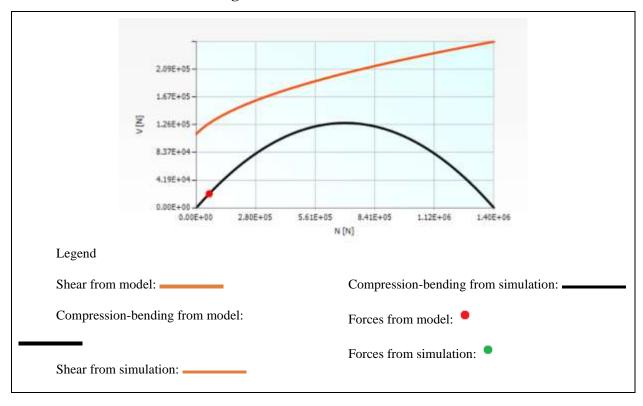


Figure VI 3 wall 7 Resistance domain diagram after reinforcement

For the calculation domain look the **APPENDIX III**

VI.6.1.2.6 Plan deformed shape

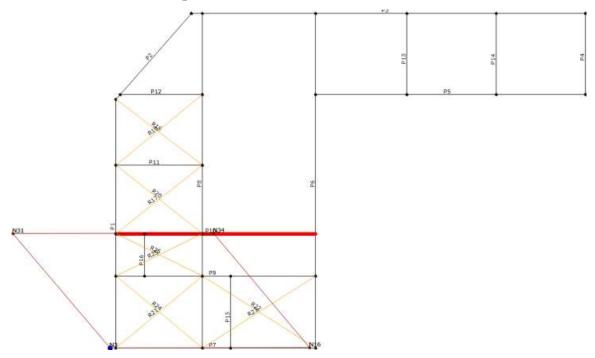


Figure VI 4 Plan deformed shape for X direction after reinforcement

VI.6.1.2.7 Pushover curve (analysis n. 4)

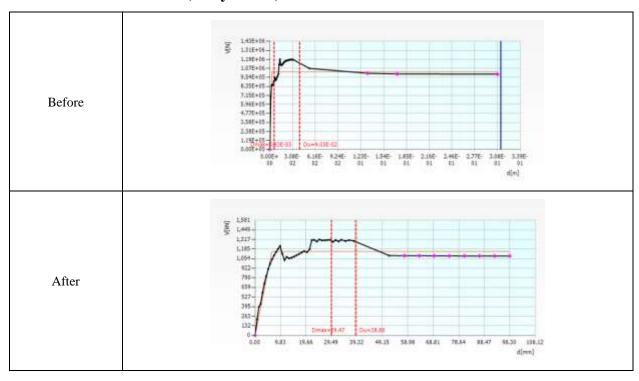


Figure VI 5 Pushover curves for X direction before and after reinforcement

VI.6.1.3 Seismic analysis Wall 8 for the Y direction

Table VI 40 wall 8 dynamic state after reinforcement

	before	After	
Limit Drift	0.005	0.010	
Drift in Step	0.003	0.000	
Damage conditio n	Shear damage	Bending damage	

VI.6.1.3.1 General data

Table VI 41 wall 8 analysis damage results Y direction after reinforcement

Code	Technical standards 2018	
Wall	8	
Piers	77	
Analysis	6	
Substep	2/46	
Limit Drift	0.010	
Drift in Step	0.000	
Damage condition	Bending damage	

VI.6.1.3.2 Input data from Model

Table VI 42 wall 8 input conditions

Typology	Common masonry	
The material's condition	Existing	
Constitutive law	Irregular masonry (Turnsek/Cacovic)	

VI.6.1.3.2.1 Geometry

Table VI 43 wall 8 geometry

Name	Value	Description
h [m]	4.63E+00	Height (deformable portion)
l [m]	2.55E+00	Length
t [m]	1.00E-01	Thickness

VI.6.1.3.2.2 Masonry: rubble

Table VI 44 wall 8 mechanical characteristics

Name	Value	Description
fm [N/m2]	2.60E+06 Average compressive strength of mason	
τ [N/m2]	5.00E+04	Average shear strength in the absence of normal stresses
CF	1.35	Confidence factor

VI.6.1.3.3 Applied forces (from pushover analysis)

Table VI 45 wall 8 applied forces for Y direction after reinforcement

Name	Value	Description
N [N]	2.24E+03	Axial force
Vd [N]	9.51E+02	Shear
M top [Nm]	1.57E+03	Upper section bending moment
M bottom [Nm]	2.83E+03	Lower section bending moment

VI.6.1.3.4 Resistence forces and verification

Table VI 46 wall 8 resistance forces verifications for Y direction after reinforcement

Name	Value	Description
N [N]	2.24E+03	Axial force (coincident with applied)
Vf [N]	9.46E+02	Shear (principle bending) calculated by interpolation on the resistance domain

Vs [N]	Shear (principle shear) 1.01E+04 calculated by interpolation on the resistance do	
Vr [N]	9.46E+02	Shear (minimum between Vf and Vs)
Vd/Vr	1.005	Safety factor

VI.6.1.3.5 Resistance domain diagram

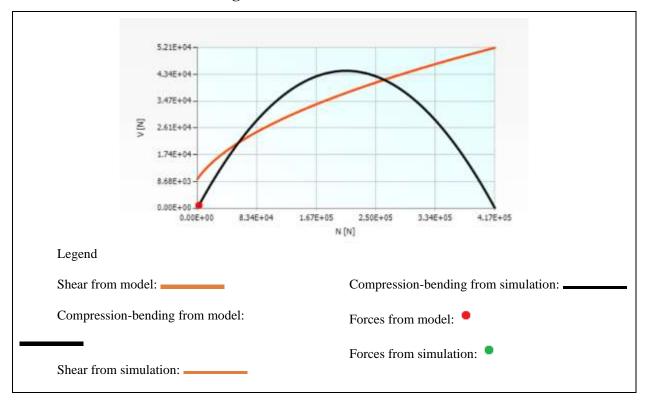


Figure VI 6 wall 8 Resistance domain diagram

For the calculation domain look the **APPENDIX III**

VI.6.1.3.6 Plan deformed shape

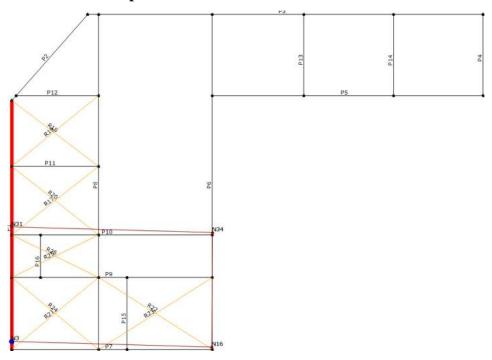


Figure VI 7 Plan deformed shape for Y direction after reinforcement

VI.6.1.3.7 Pushover curve (analysis n. 6)

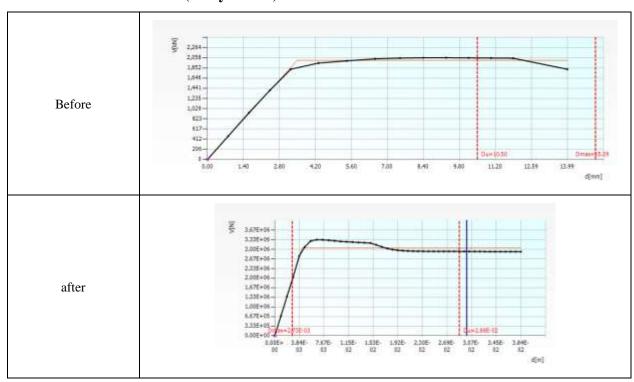


Figure VI 8 Pushover curves for Y direction before and after reinforcement

VI.7 ASSESSMENT OF THE PERFORMANCE POINT (X DIRECTION)

To assess the performance point, we have seen choosing two different methods (graphical, and empirical).

VI.7.1 Graphical "using excel table"

The method used is the (N2) approach as described in the seismic analysis part:

For all calculation look APPENDIX III

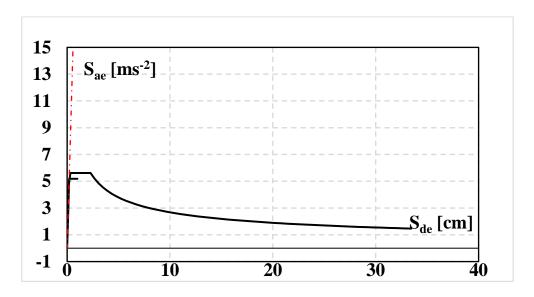


Figure VI 9 intersection of the capacity curve and the demand X direction after reinforcement

VI.7.2 Numerical

According to (Sergio Lagomarsino and al), the performance point, Sd, in terms of displacement, is determined by a closed analytical function.

Table VI 47 performance point X direction numerical method data after reinforcement

T [sec]	TC [sec]	Sae[m/s^2]	$ay[m/s^2]$	Dy [m]	Sd*[m]
0.122	0.4	7.5	0.25	0.002	0.004

Using different methods to assess the performance point gave an approximate value which around "0.4 cm"

all calculation details are in the Appendix III

VI.8 ASSESSMENT OF THE PERFORMANCE POINT (Y DIRECTION)

To assess the performance point, we have seen choosing two different methods (graphical, and empirical).

VI.8.1 Graphical "using excel table"

The method used is the (N2) approach as described in the seismic analysis part:

For all calculation look table APPENDIX III

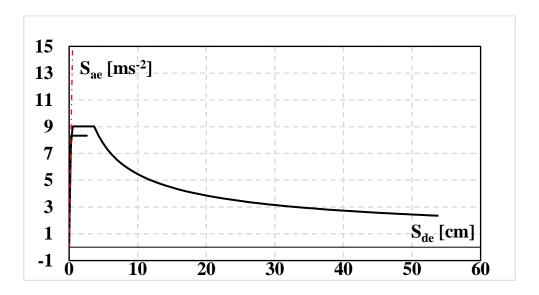


Figure VI 10 intersection of the capacity curve and the demand Y direction after reinforcement

VI.8.2 Numerical

According to (Sergio Lagomarsino and al), the performance point, Sd, in terms of displacement, is determined by a closed analytical function.

Table VI 48 performance point Y direction numerical method data after reinforcement

T [sec]	TC [sec]	Sae[m/s ²]	ay[m/s ²]	Dy [m]	Sd*[m]
0.116	0.4	7.5	0.3	0.002	0.002

Using different methods to assess the performance point gave an approximate value which around "0.02 cm"

all calculation details are in the Appendix III

VI.9 VULNERABILITY ANALYSIS

VI.9.1 Analytical functions for fragility curve

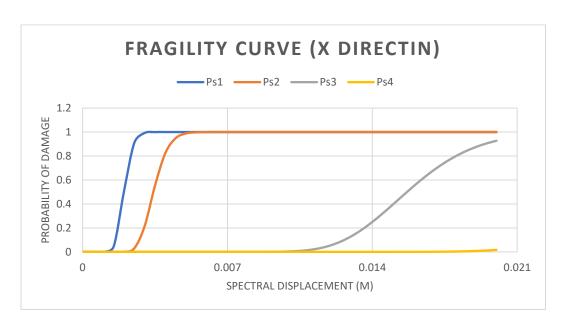


Figure VI 11 fragility curve for X directin after reinforcement

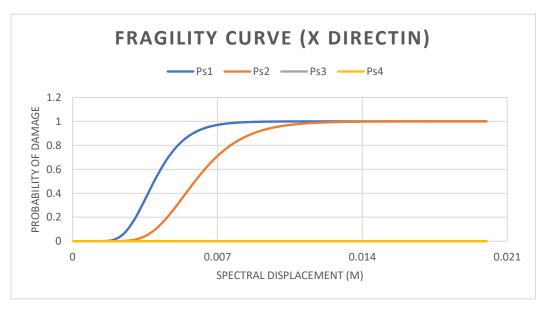


Figure VI 12 fragility curve for Y directin after reinforcement

V.1.1 Damage distribution of the studied structure

Table VI 49. Correspondence between damage level \mathbf{D}_{Sk} and damage grades \mathbf{D}_k related to structural and non structural

damage.

\mathbf{D}_{Sk}	Dk	Structural (SD) and non- structural (N-SD) damage
Slight (D _{S1})	Slight (D ₁)	No SD slight N-SD
Moderate (Ds2)	Moderate (D _{S2})	Slight SD moderate N-SD
Extensive (Ds3)	Heavy (D ₃)	Moderate SD heavy N-SD
Complete (Ds3)	Very heavy (D ₄)	Heavy SD very heavy N-SD
	Destruction (D ₅)	Very heavy SD

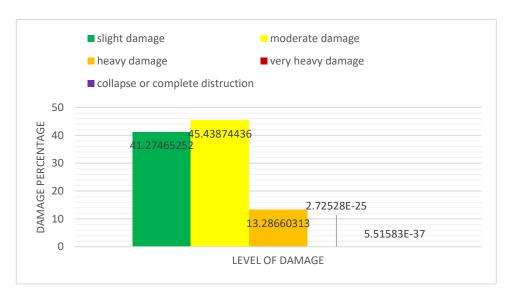


Figure VI 13 damage histogram after reinforcement (X direction)

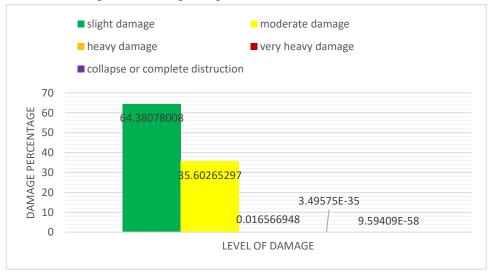
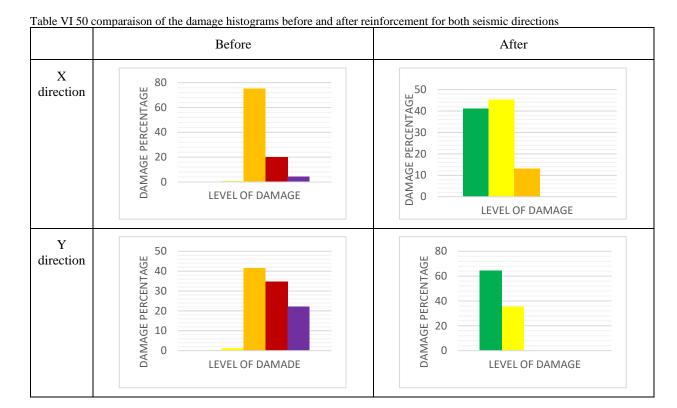


Figure VI 14 damage histogram after reinforcement (Y direction)

VI.9.2 Finds

In conclusion, the reinforcement of the masonry wall has proven to be an effective measure in reducing the vulnerability of elements to seismic demand.



Through the implementation of appropriate reinforcement techniques, the structural integrity of the wall has been enhanced, leading to improved resistance against seismic forces. This reinforcement effort serves as a vital step in ensuring the overall safety and resilience of the structure, providing greater protection for occupants and minimizing potential damage during seismic events.

VI.10 CONCLUSION

In conclusion, the reinforcement of the School of Asla Hocine's masonry structure in Annaba has significantly improved its stability and resilience. Various types of reinforcement, including wall frames, FRCM systems, and steel elements, were employed to address structural weaknesses. Static verifications confirmed the adequacy of the reinforcements, while seismic and vulnerability analyses demonstrated improved performance and reduced susceptibility to damage. The resulting histogram of the damage degree highlights the structure's enhanced resistance and durability. Overall, the successful reinforcement

efforts ensure the long-term preservation of this heritage building and provide valuable insights for similar projects in the future.

GENERAL CONCLUSION

The study focuses on the analysis and assessment of masonry structures, particularly historical buildings. It delves into various aspects such as material properties, including units and mortar, and examines the mechanisms of deterioration, encompassing both external and internal factors such as mechanical, chemical, and biodeterioration. The research further aims to estimate the mechanical properties of masonry, considering relevant codes and guidelines. Seismic behaviour and vulnerability modelling are explored, utilizing techniques such as pushover analysis to evaluate the response of structures to seismic forces. The study also investigates different strengthening methods, including surface treatment and external reinforcement, to enhance the performance and longevity of masonry structures. By conducting case studies and diagnoses, the research provides valuable insights into the behaviour of masonry under various loads and conditions. Ultimately, the findings contribute to a deeper understanding of masonry behaviour and provide valuable guidance for the effective strengthening and preservation of historical buildings.

Following the modelling and analysis of the structure, it became evident that the building was highly vulnerable to seismic actions, with severe damage observed on several elements. Consequently, the decision was made to reinforce the structure, and the outcome was remarkably positive. The behaviour of all elements, both statically and dynamically, improved significantly, addressing the vulnerabilities identified during the analysis. Notably, the damage histogram demonstrated highly satisfactory results, indicating the effectiveness of the reinforcement measures implemented. Overall, the reinforcement efforts proved successful in enhancing the structural integrity and resilience of the building, mitigating the potential damage caused by seismic events.

The findings obtained from the analysis clearly indicate the urgent need for a thorough reassessment of all structures throughout Algeria. These results serve as a wake-up call, underscoring the imperative to prioritize the preservation and careful management of our cherished heritage and historical buildings. Despite their profound significance in embodying the essence of Algerian culture, it is disheartening to observe the state of neglect that many of these structures have fallen into over the years.

Compounding the issue is the scarcity of research in this specific field, which is remarkably limited and, in some cases, virtually non-existent. The dearth of scholarly exploration into the conservation and restoration of historical buildings not only perpetuates the cycle of neglect but also inhibits our ability to develop effective strategies and approaches tailored to the unique challenges faced by these structures. This scarcity of research is further exacerbated by the absence of a dedicated

Algerian guideline or code, specifically designed to address the intricacies of preserving and maintaining heritage structures within the country.

Moreover, the prevailing laws and regulations governing heritage conservation in Algeria present a formidable obstacle to progress in this field. The stringent nature of these legal frameworks restricts innovation and hampered the development of a comprehensive approach to heritage preservation. There is an urgent need to review and revise these regulations, fostering an environment that encourages research, innovation, and collaboration in the field of heritage conservation.

By acknowledging the critical state of our historical buildings and acknowledging the lack of attention they have received, we can pave the way for transformative change. It is imperative to advocate for the establishment of a robust research framework that actively supports investigations into heritage conservation and restoration. Simultaneously, efforts must be made to formulate a comprehensive Algerian guideline or code that provides clear and practical directives for the management, maintenance, and seismic reinforcement of heritage structures.

In embracing these measures, we can foster a renewed commitment to our shared cultural legacy and ensure its preservation for generations to come. By safeguarding our historical buildings and investing in their protection, we honor our heritage, strengthen our national identity, and contribute to the sustainable development and prosperity of Algeria.

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APPENDIX I

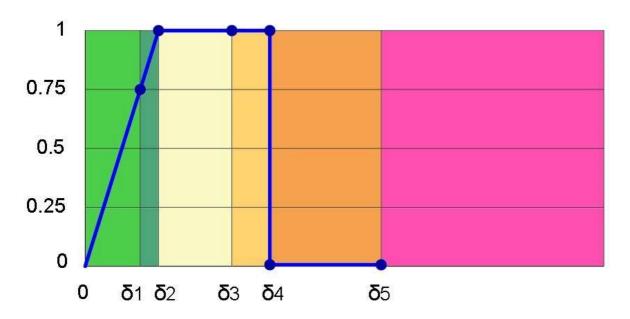
I.1 CONSTITUENT BONDS

Subsequently, the constituent bonds associated with the shear and bending mechanisms acting on the load-bearing masonry are analyzed.

The colored areas used on diagrams, refer to the color legend dedicated to "Masonry", present on 3Muri.



· Pier with shear mechanism

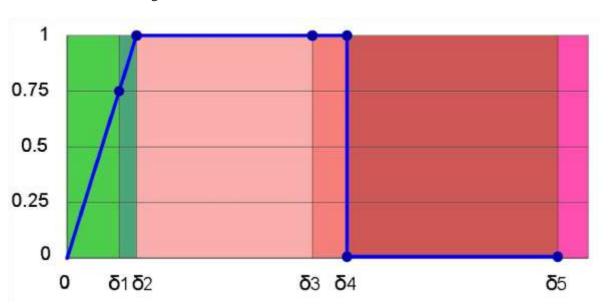


The behavior of the pier wall shear can be described through the following traits, representative of the progressive levels of damage relating to the previous diagram:

0 - δ1	elasticity
δ1 - δ2	incipient of plasticity

δ2 - δ3	plastic for shear
δ3 - δ4	shear rupture incipient
δ4 - δ5	shear rupture
δ5 - ∞	serious crisis

· Pier with bending mechanism



The behavior of the pier wall to bending, however, can be described through the following traits:

0 - δ1	elasticity
δ1 - δ2	incipient of plasticity
δ2 - δ3	plastic for bending
δ3 - δ4	bending rupture incipient
δ4 - δ5	bending rupture
δ5 - ∞	serious crisis

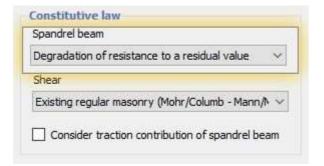
Some levels of damage are used to describe more carefully the progress of the crisis:

- · incipient of plasticity: When an element is in the elastic field but it is next to the plasticity
- · incipient of rupture : When an element is in the plastic field but is close to rupture

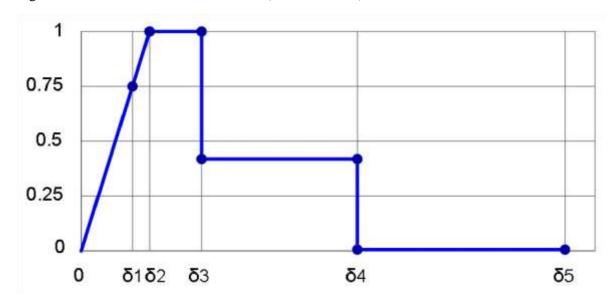
· Serious crisi: When afterwards the rupture element, the deformations become so significant that they can generate a local collapse.

These new levels of damage enable a more accurate prediction of the interventions and the degradation level of the masonry.

Through the drop-down menu, exclusively dedicated to the "Spandrel beams", present in the main screen of masonry materials, the software provides three types of analysis:



· With degradation of resistance to residual value (Multiline bond)



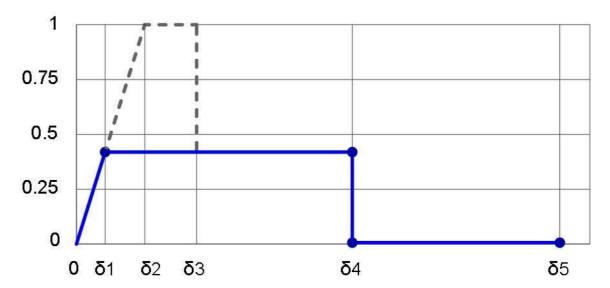
This type of bond is defined in the Circular at §C8.7.1.3.1 assuming:

 δ 1: 0.75* δ 2 (0.75 is the default value of the "incipient factor bond plasticity" defined in the parameter window.

,	[1] Materials	
	Pier drift shear	0,005
	Pier drift bending	0,01
	Spandrel beams drift shear	0,015
	Spandrel beam drift bending	0,015
	Paired spandrel beam drift	0,02
	Existing: FC-LC1	1,35
	Existing: FC-LC2	1,2
	Existing: FC-LC3	1
	Reduction factor for cracked stiffness	2
C	Concrete/steel lintel residual resistance	0,6
	Timber lintel residual resistannce	0,4
	Masonry arch residual resistance	0,1
	Incipient factor bond plasticity	0,75
•	[2] Static calculation	
	γG1	1,3
	γG2	1,5
	γQ	1,5

 δ 2: deformation in correspondence with the elastic limit defined by the stiffness and limit resistance δ 3: 0.005 δ 4: 0.015 δ 5: 2* δ 4: This deformation represents the state of "serious crisis" not directly required in the standard but useful as a "warning" for the designer.

· With resistance equal to residual value (bilinear bond)

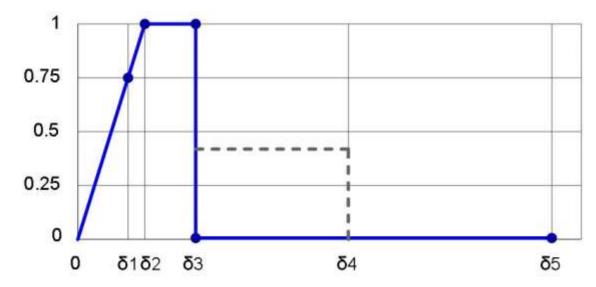


This type of bond is defined in the Circular at §C8.7.1.3.1 assuming:

 $\delta 4$: 0.015 $\delta 5$: 2* $\delta 4$: This deformation represents the state of "serious crisis" not directly required in the standard but useful as a "warning" for the designer.

This type of bond is produced by limiting the multiline bond to the residual resistance.

· Without residual resistance



This type of bond represents a logical variation of the earlier bond starting from the multiline bond but is currently not covered by current regulations.

I.1.1 Definition of residual resistance

The definition of residual resistance is explained on section C8.7.1.3.1 of the Circolare

(...) In the absence of more accurate formulations, it is possible to choose values of residual strength, such as the maximum one provided by (8.7.1.16), equal to:

-lintel in reinforced concrete or steel, as long as it is supported by an extension force in the masonry: 60%;

-wooden lintel, with good characteristics and well clamped: 40%; -masonry arch: 10%. (...)

I.1.2 Tension failure

One of the colors in the legend represents tension failure.

Reinforced masonry: The traction caused the rupture of the reinforcement, this is an irreversible state.

I.1.3 Ineffective element

One of the colors of the legend represents the ineffective element.

<u>Ordinary masonry</u>: The masonry is not effective; this is not a real rupture but a reversible temporary state that could evolve into any other type of rupture.

I.2 EUROCODE 6

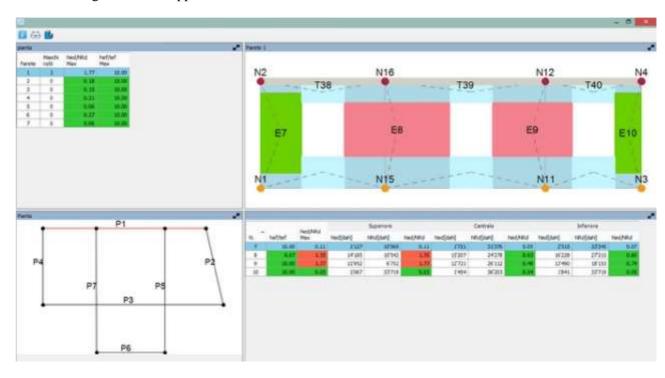
Let's present below the checks that are carried out:

Slenderness check: EN 1996-1-1 § 5.5.1.4	h _{ef} /t _{ef} ≤ λ _{lim} : di default=27
	h_{ef} : effective height of the wall equal to $\rho ext{-}h$ t_{ef} : effective thickness of the wall equal to $\rho_t ext{-}h$
Verification subjected to vertical loading EN 1996-1-1 § 6.1.2	$N_{Ed}\!\leq\!N_{Rd}\!\!=\!\!\Phi\;f_dA$
	N_{Ed} : design value of the vertical load applied to a masonry wall; A: is the loaded horizontal gross cross-sectional area of the wall; fd: design compressive strength of the masonry; Φ : is the capacity reduction factor

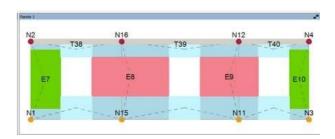
The static checks are performed in an area that is accessed using the associated button.



The following screen will appear:



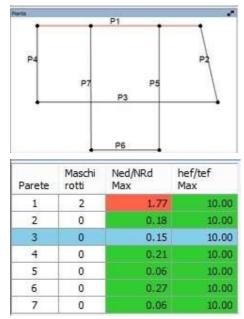
This video is very similar to that which presents the results of non-linear analysis. Let's describe it in detail.



In the upper right side appears the wall mesh.

In this case, does not exist the legend with colors indicating different phases of damage.

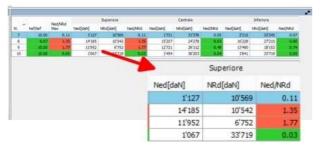
Elements that passed the check appear in green and in different color those that do not exceed the check.



At the lower left side, is shown the plan view. The wall shown in the precedent view is highlighted with a thick line.

On the upper left side there is a list of the walls in the model, with the number of elements that did not pass the check and the values associated with the individual checks. The values found in the table are for the wall elements examined in which the limit values are the most restrictive of all the piers.

Clicking on the line of a wall (highlighting it in blue) brings that wall to the view on the right side.



At the lower right side, the elements detail window is shown for the selected wall.

For each masonry element, the checks are performed for three different sections (higher, central, lower). For each section the value for normal forces strain is shown (N_{Rd} : computed based on the masses and the combinations of the loads) and the normal resistant strain ($N_{Rd} = \Phi f_d A$). The check is satisfied if the ratio $N_{Ed}/N_{Rd} \le 1$. In this case, the corresponding cell appears in green, otherwise in red color. In some cases, as shown in the example, N_{Rd} cannot be calculated (n/d: not defined). This happens when the slenderness or eccentricity checks are not satisfactory.



When a masonry pier is chosen from the list and the information button is pressed, a window will appear which contains the calculation details.

The window shows all the details of the parameters used in the computation of the various check coefficients. The text in red near the bottom gives relative informations to conditions where the check was not satisfied. This window can remain open and be moved to any point of the drawing area while working (floating window). This gives to the user the possibility to select various elements in different wall and still have the details for each individual check visible.

		Higher	Central	Lower
ID	h0/t	e1 /t	e2/t	e1 /t
35	7.50	0,328	8,144	0,263
36	7,50	0,306	0,145	0,276
37	7,50	0,360	0,172	0,331
38	7,50	0,332	0,150	0,274
39	7,50	0,451	0,187	0,268
40	7,50	0,401	0,175	0,311
41	7,50	0,448	0,202	0,369
42	7,50	0,470	0,186	0,309

Here we see the check details for slenderness and eccentricity. The green values indicate that the check was passed.

In order to help the user in the results interpretations, some of the tables offer the possibility of reordering the rows according to a characteristic shown in a column by simply clicking on the title of the column.

APPENDIX II

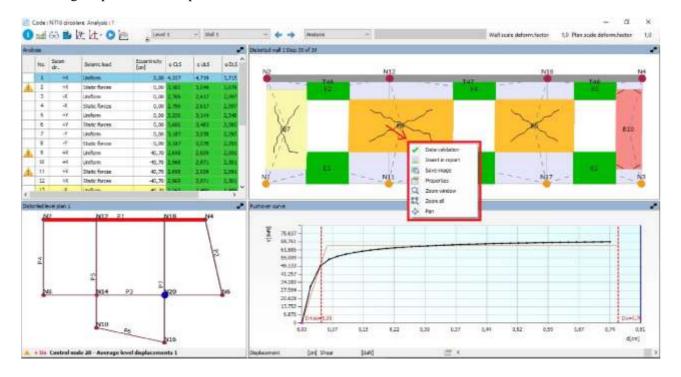
I Data validation

This validation tool allows the user to evaluate the stress state of the masonry walls in a quick, simple and intuitive way, graphically displaying, for each step of the non-linear seismic analysis, the drift value, the resistance domain and the mechanism of collapse.

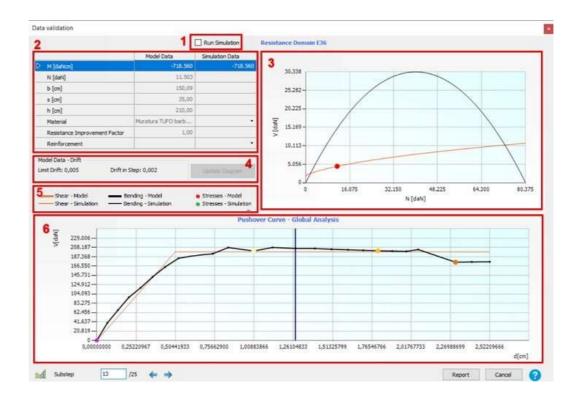
This function is designed both to help the user understand the behavior of the structure, but above all to help and guide him in the phase of validating the results provided by the software.

For this purpose, within the results window, at each point of the global pushover curve, for each masonry wall it is possible to view the state (first yielding, incipient faliure, breaking) in which the element is located. This allows the designer to have a transversal view of the behavior, and therefore of the influence, of the individual wall panels within the structure. In the event that improvements need to be made to an existing building (reinforcements with FRP and FRCM), using this validation tool, the designer can easily understand on which wall panels it is appropriate to intervene, or if the interventions are effective or if they can be optimized.

From the window containing the results of the pushover analysis, by right clicking on the wall of interest, the following dropdown menu opens:



Once you have clicked on the "data validation" option, the following window appears:



It allows to start a simulation by entering the simulation data in the third column of the table at the top left, and click on "Update diagram".

The table contains in the second column the geometric and mechanical data of the masonry wall in question, while in the third column, which can be activated by checking the "Run simulation" box, the respective parameters used to determine the simulated resistance domains can be entered.

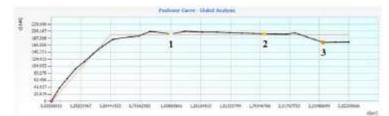
Resistance domains diagram.

Values of the element's limit drift (depends on the breaking mechanism) and the drift to the pace. As is known, the element reaches the break when the drift at the step reaches the drift limit.

Legend related to the diagrams of the resistance domains.

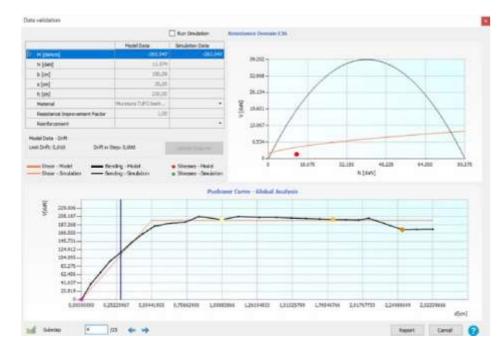
The orange line indicates the shear resistance domain, while the black line indicates the bending resistance domain. The solid lines represent the resistance domain evaluated for the geometric and mechanical characteristics of the modeled masonry wall, while the dashed lines indicate the simulated resistance domains. The two circular indicators, red and green, respectively indicate the stress state of the element resulting from the pushover analysis and the simulated stress state.

Global pushover curve on which there are colored indicators that indicate the calculation step in which the state change of the wall occurs (beginning of plastification, incipient breaking, breaking).

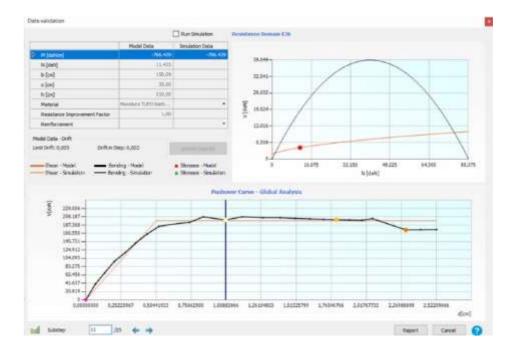


The colored indicators, which designate the state in which the wall under examination is located, allow us to quickly understand that the wall under examination exhibits an elastic behavior until point 1 is reached, step in which the first plastification by shear takes place. Moving further along the curve, the wall changes state in correspondence with the step identified by point 2, that is when he reaches 75% of the drift limit. In this step, in fact, the color legend indicates that the element is in a state of incipient breakage due to shear, which occurs at the step identified in point 3, when the drift limit is reached. As can be easily understood from this result, it can be deduced that the wall in question is well sized and effectively contributes to the strength of the building as its breakage is close to the collapse of the entire building, coinciding with the last point of the curve.

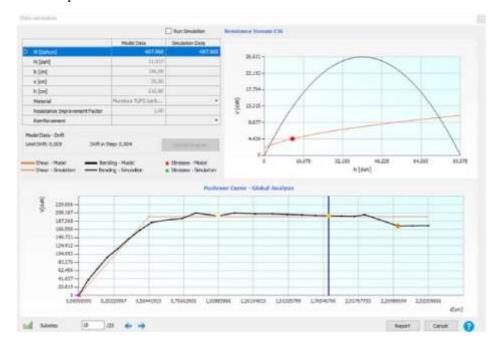
For each point of the pushover curve, it is also possible to visualize the resistance domains of the masonry wall. As already said, in the stretch of curve between step 0 and point 1, the masonry wall is in the elastic phase, in fact, from the resistance domain we can observe that the point indicating the state of stress at the step (red indicator), is placed within the domain.



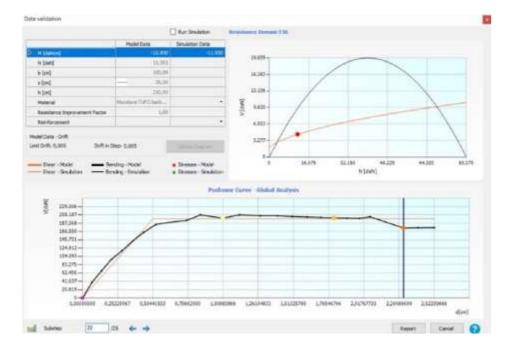
Positioning instead in correspondence with the step of the pushover curve where the first yielding occurs (point 1), from the graph it can be observed that the stressing point (red indicator) is exactly on the curve corresponding to the shear resistance criteria of the masonry wall (curve orange), but if we observe the drift value, it is lower than the breaking value (drift in step = 0.001; drift limit = 0.005).



By creating the diagrams of the resistance domains for the step of the pushover curve corresponding to point 2 (incipient collapse due to shear), it is observed that the red indicator always coincides with the orange curve, while the drift at the step is equal to 0.004 or coincides with 75% of the drift limit rounded to three decimal places.



Finally, positioning in correspondence with the step of the curve in which the breaking of the wall occurs, we observe that the red indicator always coincides with the orange curve, while the drift at the step is equal to 0.005 or coincides with the drift limit.



At the bottom left, using the following buttons, you can access the damage status legend and move between the various points of the pushover curve.



I.1 RUN SIMULATION Run Simulation

This function offers the possibility of simulating the resistance domain of a masonry wall in real time, simply by varying a few parameters that define its geometric and mechanical characteristics, or those of any reinforcement applied, without having to modify anything in the global model and without having to re-calculate.

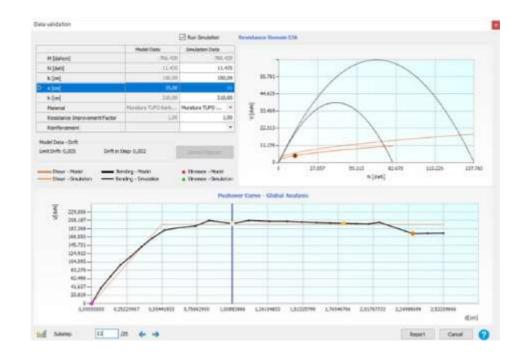
If you want to start a simulation, you need to select the step of interest of the pushover curve, check the "Run simulation" box, enter the simulation data in the third column of the table at the top left, and click on "Calculate domain".

I.1.1 Example

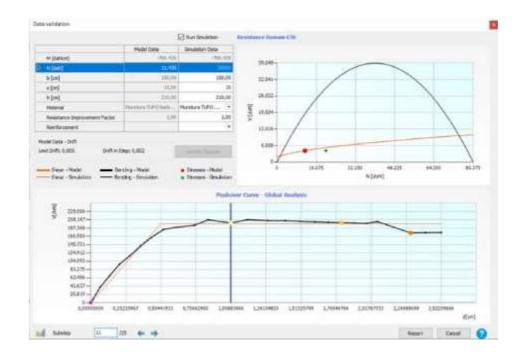
In the following example, the simulation is started by positioning at point 1 of the pushover curve and increasing the thickness of the masonry.

As it can be seen from the following figure, the increase in thickness of the masonry wall has the effect of increasing its resistance, and therefore, under the same stress (the red indicator coincides with the green one due to the fact that in the simulation the normal stress has not been changed), in the simulation the element is in the elastic phase, while from the data entered in the model it would be in the plastic phase.

Ultimately, if the masonry wall had the geometric characteristics introduced with the simulation, it would be able to withstand a greater shear force.



A similar result could be obtained by simulating the case in which the normal stress is greater, for example by increasing the weight of the floor that rests on this wall as a consequence of a reinforcement intervention on a floor which on the one hand improves the performance of the slab itself, and on the other hand it increases the load on the walls. In this case the curves of the domains remain unchanged as they are a function only of the geometric and mechanical parameters of the masonry and of the possible presence of the reinforcement, while the green indicator, which indicates the state of simulated stress, has moved to the right, re-entering the domain.



What is described above should make us reflect on all those cases in which we try to make an improvement on the structure by lightening the floors.

This could bring the solicitor closer to the origin of the domain and consequently expose them outside the domain itself, creating a deterioration rather than the desired improvement.

These observations make us understand that the most efficient improvement choices should be made after having examined the resistance domain to clarify on which area it is good to act.

I.1.2 Quantifying the extent of improvement of a reinforcement

The application of a reinforcement (reinforced masonry, FRP or FRCM) acts on two different ways:

- · Resistance
- · Ductility (displacements)

The concept of "improvement" is therefore produced by the union of the two characteristics listed above, which can occur simultaneously or one of the two can have a greater weight than the other.

Strength affects plasticity, ductility affects rupture; ductility itself can be indirectly influenced by resistance by postponing the plasticity of the element due to greater resistance.

Modifying resistance and / or ductility alters the stiffness of the building as a whole and consequently the load that can potentially act on the element in question.

According to the theory of resistance domains, the performance of the element depends on the vertical load acting on it. It therefore follows a significant alteration of the shape of the resistance domains and of the element's ultimate ductility.

It is therefore impossible to numerically quantify the extent of the improvement resulting from the intervention as load, strength and ductility are linked to each other and cannot be schematized in a simplified way through a simple improvement factor of the compressive strength.

To define the benefits produced by an intervention of this nature, it is therefore necessary to simultaneously examine both the changes in the resistance domain (and not just the compressive capacity) and the increase in ductility provided by the reinforcement itself.

In some cases it may happen that the result obtained by recalculating the global analysis does not reflect what was previously simulated through the change of some characteristics.

In fact, when the simulation is carried out on an element, it is considered as an isolated element exempt from the interactions with the rest of the structure that will come into play only following the global calculation.

The modification of geometric or mechanical characteristics or the addition of any reinforcements have an influence not only on the element itself but on the behavior of the entire structure, modifying its configuration in

terms of ductility, stiffness and load. It is therefore important to consider the simulation result as approximate (compared to what would be obtained by redoing the global analysis of the structure) and to use the tool as an aid to the designer who otherwise, faced with an element that is not verified, would have to make changes to the structure based on more or less vague criteria, sometimes modifying the structure in an ineffective way, and spending time redoing the mesh each time and recomputing the seismic analysis.

II DOMAIN COORDINATES FROM MODEL WALL, SEISMIC ANALYSIS NO. 4 WALL 10 X DIRECTION

II.1 BENDING DOMAIN

Table 1wall 10 bending domain

N [kN]	V [kN]
0	0
51	67
102	132
153	196
203	258
254	319
305	379
356	438
407	495
458	550
509	605
560	658
610	709
661	760
712	808
763	856
814	902
865	947
916	991
967	1,033
1,017	1,073
1,068	1,113
1,119	1,151
1,170	1,188
1,221	1,223
1,272	1,257

1,323	1,289
1,374	1,321
1,424	1,351
1,475	1,379
1,526	1,406
1,577	1,432
1,628	1,457
1,679	1,480
1,730	1,501
1,780	1,522
1,831	1,541
1,882	1,558
1,933	1,575
1,984	1,590
2,035	1,603
2,086	1,616
2,137	1,626
2,187	1,636
2,238	1,644
2,289	1,651
2,340	1,656
2,391	1,660
2,442	1,663
2,493	1,664
2,544	1,664
2,594	1,663
2,645	1,660
2,696	1,656
2,747	1,651
2,798	1,644
2,849	1,636
2,900	1,626
2,950	1,616
3,001	1,603
3,052	1,590
3,103	1,575
3,154	1,558
3,205	1,541
3,256	1,522
3,307	1,501
3,357	1,480

3,408	1,457
	1,437
3,459	
3,510	1,406
3,561	1,379
3,612	1,351
3,663	1,321
3,714	1,289
3,764	1,257
3,815	1,223
3,866	1,188
3,917	1,151
3,968	1,113
4,019	1,073
4,070	1,033
4,121	991
4,171	947
4,222	902
4,273	856
4,324	808
4,375	760
4,426	709
4,477	658
4,527	605
4,578	550
4,629	495
4,680	438
4,731	379
4,782	319
4,833	258
4,884	196
4,934	132
4,985	67
5,036	0

II.2 SHEAR DOMAIN

Table 2 wall 10 shear domain

N [kN]	V [kN]
0	156
51	179

102	200
153	219
203	236
254	252
305	268
356	282
407	296
458	309
509	321
560	333
610	345
661	356
712	367
763	378
814	388
865	398
916	408
967	418
1,017	427
1,068	436
1,119	445
1,170	454
1,221	463
1,272	471
1,323	479
1,374	488
1,424	496
1,475	504
1,526	511
1,577	519
1,628	527
1,679	534
1,730	541
1,780	549
1,831	556
1,882	563
1,933	570
1,984	577
2,035	584
2,086	590
2,137	597
· · · · · · · · · · · · · · · · · · ·	

2,187	604
2,238	610
2,289	617
2,340	623
2,391	629
2,442	636
2,493	642
2,544	648
2,594	654
2,645	660
2,696	666
2,747	672
2,798	678
2,849	684
2,900	689
2,950	695
3,001	701
3,052	706
3,103	712
3,154	717
3,205	723
3,256	728
3,307	734
3,357	739
3,408	745
3,459	750
3,510	755
3,561	760
3,612	765
3,663	771
3,714	776
3,764	781
3,815	786
3,866	791
3,917	796
3,968	801
4,019	806
4,070	811
4,121	816
4,171	820
4,222	825
4,222	023

4,273	830
4,324	835
4,375	839
4,426	844
4,477	849
4,527	853
4,578	858
4,629	863
4,680	867
4,731	872
4,782	876
4,833	881
4,884	885
4,934	890
4,985	894
5,036	899
3,030	077

IIIDOMAIN COORDINATES FROM MODEL WALL, SEISMIC ANALYSIS NO. 4 WALL 7 X DIRECTION

III.1 BENDING DOMAIN

Table 3 wall 7 bending domain

N [kN]	V [kN]
0	0
12	5
24	10
36	15
48	20
60	25
72	30
84	34
96	39
109	43
121	47
133	52
145	56
157	60
169	63

101	67
181	67
193	71
205	74
217	78
229	81
241	84
253	87
265	90
277	93
289	96
301	99
314	101
326	104
338	106
350	108
362	110
374	112
386	114
398	116
410	118
422	119
434	121
446	122
458	124
470	125
482	126
494	127
506	128
519	128
531	129
543	130
555	130
567	130
579	131
591	131
603	131
615	131
627	130
639	130
651	130
663	129

675 687 128 687 128 699 127 711 126 724 125 736 124 748 122 760 121 772 119 784 118 796 116 808 808 114 820 112 832 110 844 108 855 106 868 8104 880 101 881 885 104 880 101 887 990 991 991 991 991 991 991 991 991 991		
699 127 711 126 724 125 736 124 748 122 760 121 772 119 784 118 796 116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,073 47 1,085 43 1,097 39 1,109 34 1,1121 30 1,134 <	675	128
711 126 724 125 736 124 748 122 760 121 772 119 784 118 796 116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109	687	128
724 125 736 124 748 122 760 121 772 119 784 118 796 116 808 114 820 112 832 110 844 108 855 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 <td>699</td> <td>127</td>	699	127
736 124 748 122 760 121 772 119 784 118 796 116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 <td>711</td> <td>126</td>	711	126
748 122 760 121 772 119 784 118 796 116 808 114 820 112 832 110 844 108 856 106 888 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,1134 25 1,146 20	724	125
760 121 772 119 784 118 796 1116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	736	124
772 119 784 118 796 116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	748	122
784 118 796 116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,1109 34 1,121 30 1,134 25 1,146 20	760	121
796 116 808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	772	119
808 114 820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	784	118
820 112 832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	796	116
832 110 844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	808	114
844 108 856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	820	112
856 106 868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,049 56 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	832	110
868 104 880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	844	108
880 101 892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	856	106
892 99 904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	868	104
904 96 916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	880	101
916 93 929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	892	99
929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	904	96
929 90 941 87 953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	916	93
953 84 965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	929	90
965 81 977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	941	87
977 78 989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	953	84
989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		
989 74 1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	977	78
1,001 71 1,013 67 1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		
1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	1,001	
1,025 63 1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20	1,013	67
1,037 60 1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		63
1,049 56 1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		60
1,061 52 1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		56
1,073 47 1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		
1,085 43 1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		
1,097 39 1,109 34 1,121 30 1,134 25 1,146 20		
1,109 34 1,121 30 1,134 25 1,146 20		
1,121 30 1,134 25 1,146 20		
1,134 25 1,146 20		
1,146		
1,100	1,158	15

1 170	10
1,170	10
1,182	5
1,194	0

III.2 SHEAR DOMAIN

Table 4 wall 7 shear domain

N [kN]	V [kN]
0	25
12	28
24	32
36	35
48	37
60	40
72	42
84	45
96	47
109	49
121	51
133	53
145	55
157	56
169	58
181	60
193	61
205	63
217	65
229	66
241	67
253	69
265	70
277	72
289	73
301	74
314	76
326	77
338	78
350	80
362	81
374	82

386	83
398	84
410	86
422	87
434	88
446	89
458	90
470	91
482	92
494	93
506	94
519	95
531	96
543	97
555	98
567	99
579	100
591	101
603	102
615	103
627	104
639	105
651	106
663	107
675	108
687	109
699	110
711	111
724	112
736	113
748	113
760	114
772	115
784	116
796	117
808	118
820	118
832	119
844	120
856	121
868	122

880	123
892	123
904	124
916	125
929	126
941	127
953	127
965	128
977	129
989	130
1,001	130
1,013	131
1,025	132
1,037	133
1,049	133
1,061	134
1,073	135
1,085	136
1,097	136
1,109	137
1,121	138
1,134	138
1,146	139
1,158	140
1,170	141
1,182	141
1,194	142

$\begin{array}{c} \textbf{IV\,Domain\,coordinates\,from\,model\,wall\,, Seismic\,analysis} \\ \textbf{no.\,5\,Wall\,8\,\,Y\,direction} \end{array}$

IV.1 BENDING DOMAIN

Table 5 wall 8 bending domain

N [kN]	V [kN]
0	0
14	11
28	23
42	34

56	44
71	55
85	65
99	75
113	85
127	95
141	104
155	113
169	122
183	131
198	139
212	148
226	155
240	163
254	171
268	178
282	185
296	192
310	198
324	205
339	211
353	217
367	222
381	228
395	233
409	238
423	242
437	247
451	251
466	255
480	259
494	262
508	266
522	269
536	271
550	274
564	276
578	278
593	280
607	282
621	283
\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	200

625	204
635	284
649	285
663	286
677	287
691	287
705	287
719	287
734	286
748	285
762	284
776	283
790	282
804	280
818	278
832	276
846	274
861	271
875	269
889	266
903	262
917	259
931	255
945	251
959	247
973	242
988	238
1,002	233
1,016	228
1,030	222
1,044	217
1,058	211
1,072	205
1,086	198
1,100	198
1,114	185
1,129	178
1,143	171
1,157	163
1,171	155
1,185	148
1,199	139

1,213	131
1,227	122
1,241	113
1,256	104
1,270	95
1,284	85
1,298	75
1,312	65
1,326	55
1,340	44
1,354	34
1,368	23
1,383	11
1,397	0

IV.2 SHEAR DOMAIN

Table 6 wall 8 shear domain

N [kN]	V [kN]
0	35
14	41
28	46
42	50
56	54
71	58
85	61
99	64
113	67
127	70
141	73
155	76
169	79
183	81
198	84
212	86
226	88
240	91
254	93
268	95
282	97

296	99
310	101
324	103
339	105
353	107
367	109
381	111
395	113
409	115
423	117
437	118
451	120
466	122
480	123
494	125
508	127
522	128
536	130
550	131
564	133
578	135
593	136
607	138
621	139
635	140
649	142
663	143
677	145
691	146
705	148
719	149
734	150
748	152
762	153
776	154
790	156
804	157
818	158
832	160
846	161
861	162

875	163
889	165
903	166
917	167
931	168
945	170
959	171
973	172
988	173
1,002	174
1,016	176
1,030	177
1,044	178
1,058	179
1,072	180
1,086	181
1,100	182
1,114	184
1,129	185
1,143	186
1,157	187
1,171	188
1,185	189
1,199	190
1,213	191
1,227	192
1,241	193
1,256	194
1,270	195
1,284	197
1,298	198
1,312	199
1,326	200
1,340	201
1,354	202
1,368	203
1,383	204
1,397	205

V ASSESSMENT OF THE PERFORMANCE FOR THE (X DIRECTION)

V.1 SDOF TO MDOF

For the conversion of forces and displacements of a system, the following equations are used to have the **SDOF** from the **MDOF** capacity curve:

$$F *= F/\Gamma$$

$$d *= d/\Gamma$$

 Γ : participation factor

$$\Gamma = \frac{m *}{\sum mi \ \varphi^2}$$
 in wich $m *= \sum mi \ \varphi i$

K: the rigidity

$$k = \frac{F(0.Fu)}{d(0.6Fu)}$$

T: the period

$$T *= 2\pi \sqrt{\left(\frac{m*}{k}\right)} \text{ or } 2\pi \sqrt{\left(\frac{m*d*}{F*}\right)}$$

interpolation is made to determine the value of the displacement d0.6 associated with the force 0.6Fu.

Гх								
-	0,6*F _∪ =F _y	d (0,6*F _u)	dy to d* _Y	k*	m*	T*	du	Fu
1.74	[KN]	[m]	[m]	[KN/m]	[ton]	[sec]	[m]	[KN]
	440.00	0.0024	0.003700	183333.0	390	0.29	0.022	744.8

Table 7 The bi-linear equivalent capacity curve domain for X direction

Bi-lir	iear	Note
d _i [m]	F _i [KN]	Note
0	0	0
0.0024	440	Correspond to F (0.6 Fu), d (0.6 Fu)
0.003700	661	Correspond to Fy, dy
0.0219	661	horizontal plateau, Fy, du

Table 8. transformation of the capacity curve from MDOF to SDOF

	MDOF	SDOF			
Step	Displacement	BaseForce	D*=Δ/Гx	F*=V/Γx	
	m	KN	m	KN	
0	0	0	0.000000	0	
1	0.00074	221	0.000425	127.0115	
2	0.00146	392	0.000839	225.2874	
3	0.00212	433	0.001218	248.8506	
4	0.00283	587	0.001626	337.3563	
5	0.00356	712	0.002046	409.1954	
6	0.0043	817	0.002471	469.5402	
7	0.00505	910	0.002902	522.9885	
8	0.0058	986	0.003333	566.6667	
9	0.00655	1046	0.003764	601.1494	
10	0.00731	1099	0.004201	631.6092	
11	0.00807	1144	0.004638	657.4713	
12	0.00884	1188	0.005080	682.7586	
13	0.00963	1229	0.005534	706.3218	
14	0.01046	1124	0.006011	645.977	
15	0.01135	1034	0.006523	594.2529	
16	0.0122	1077	0.007011	618.9655	
17	0.01313	1058	0.007546	608.046	
18	0.01406	1068	0.008080	613.7931	
19	0.01501	1083	0.008626	622.4138	
20	0.01597	1100	0.009178	632.1839	
21	0.01695	1119	0.009741	643.1034	
22	0.01793	1138	0.010305	654.023	
23	0.01893	1158	0.010879	665.5172	
24	0.02001	1144	0.011500	657.4713	
25	0.02103	1184	0.012086	680.4598	
26	0.02187	1307	0.012569	751.1494	
27	0.0228	1313	0.013103	754.5977	
28	0.02383	1290	0.013695	741.3793	
29	0.02478	1317	0.014241	756.8966	

30	0.02582	1305	0.014839	750
31	0.02687	1306	0.015443	750.5747
32	0.02791	1309	0.016040	752.2989
33	0.02894	1313	0.016632	754.5977
34	0.03006	1286	0.017276	739.0805
35	0.03109	1310	0.017868	752.8736
36	0.03221	1291	0.018511	741.954
37	0.03325	1313	0.019109	754.5977
38	0.03488	1296	0.020046	744.8276
39	0.0363	1308	0.020862	751.7241
40	0.03818	1296	0.021943	744.8276
41	0.05173	1097	0.029730	630.4598
42	0.05767	1093	0.033144	628.1609
43	0.06336	1094	0.036414	628.7356
44	0.06917	1093	0.039753	628.1609
45	0.07499	1092	0.043098	627.5862
46	0.08082	1091	0.046448	627.0115
47	0.08664	1091	0.049793	627.0115
48	0.09247	1091	0.053144	627.0115
49	0.0983	1091	0.056494	627.0115
50	0.1086	919	0.062414	528.1609

V.2 THE BI-LINEAR EQUIVALENT CAPACITY CURVE THE SHEAR FORCES OF THE BI LINEAR TO SAG

Table 9. bi-linear capacity curve (Sd,Sag)

	BILINEARE SDOF				
	S [cm] V [KN] S _{ag} [ms ⁻²]				
Δ_0	0	0	0.00		
Δ _{0,6}	0.24	440	1.13		
Δ_{y}	0.37	661	1.70		
Δu	2.2	661	1.70		

V.3 THE SPECTRE OR THE DEMAND CURVE SHOULD BE TRANSFORMED ALSO TO THE (ADRS) FORM AS FOLLOW:

q	*	Sae(T*)	Sde (T*) =demax [cm]	Tc	d*max [cm]	u	Ru
					Performance point		
3.	6	6.1	1.39	0.4	1.68	4.587677	3.597247

$$q *= \frac{Sag}{Sae(T *)}$$

 S_{ae} : the spectral acceleration correspond to (T^*)

 S_{ag} : max spectral acceleration of the structure

 q^* : the behaviour factor

$$\begin{cases} R_u = \frac{(u-1)T}{Tc} + 1 &, T > TC \\ R_u = u &, T \leq Tc \end{cases}$$

$$u = \begin{cases} 1 + \frac{(q-1)T}{TC} &, T \leq Tc \\ q &, T > TC \end{cases}$$

 μ : The ductility capacity for the building

R_u: strength reduction factor due to ductility

$$S_a = \frac{S_{ae}}{Ru}$$

$$S_d = \frac{u}{Ru} S_{de} = \frac{uT^2}{4\pi^2} Sa$$

Sa: spectral acceleration.

Sd: spectral displacement.

Table 10. transformation of the demand curve to (ADRS) form.

T [sec]	Sae [g]	Sae [ms ⁻²]	S _{de} [cm]	sae/Ru	sde/Ru
0	0.250	3.25	0	0.903469	0
0.05	0.375	4.875	0.030902623	1.355203	0.008591
0.1	0.500	6.5	0.164813988	1.806938	0.045817
0.15	0.625	8.125	0.463539342	2.258672	0.128859
0.2	0.625	8.125	0.824069942	2.258672	0.229084
0.25	0.625	8.125	1.287609284	2.258672	0.357943
0.3	0.625	8.125	1.854157369	2.258672	0.515438

0.35 0.625 8.125 2.523714197 2.258672 0.701568 0.4 0.625 8.125 3.296279768 2.258672 0.916334 0.45 0.578 7.511413805 3.85680275 1.946464 1.233864 0.5 0.539 7.001912743 4.438512175 1.946464 1.233864 0.5 0.505 6.570850268 5.039966647 1.826633 1.401062 0.6 0.477 6.20053548 5.659947597 1.723689 1.573411 0.65 0.452 5.878336719 6.297408779 1.634121 1.750619 0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.4656513 2.503413 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.1						
0.45 0.578 7.511413805 3.85680275 2.088101 1.072154 0.5 0.539 7.001912743 4.438512175 1.946464 1.233864 0.55 0.505 6.570850268 5.039966647 1.826633 1.401062 0.6 0.477 6.20053548 5.659947597 1.723689 1.573411 0.65 0.452 5.878336719 6.297408779 1.634121 1.750619 0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 1.044501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196	0.35	0.625	8.125	2.523714197	2.258672	0.701568
0.5 0.539 7.001912743 4.438512175 1.946464 1.233864 0.55 0.505 6.570850268 5.039966647 1.826633 1.401062 0.6 0.477 6.20053548 5.659947597 1.723689 1.573411 0.65 0.452 5.878336719 6.297408779 1.634121 1.750619 0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.86953	0.4	0.625	8.125	3.296279768	2.258672	0.916334
0.55 0.505 6.570850268 5.039966647 1.826633 1.401062 0.6 0.477 6.20053548 5.659947597 1.723689 1.573411 0.65 0.452 5.878336719 6.297408779 1.634121 1.750619 0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707	0.45	0.578	7.511413805	3.85680275	2.088101	1.072154
0.6 0.477 6.20053548 5.659947597 1.723689 1.573411 0.65 0.452 5.878336719 6.297408779 1.634121 1.750619 0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.6992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107	0.5	0.539	7.001912743	4.438512175	1.946464	1.233864
0.65 0.452 5.878336719 6.297408779 1.634121 1.750619 0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.534656 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856	0.55	0.505	6.570850268	5.039966647	1.826633	1.401062
0.7 0.430 5.594973113 6.951440285 1.555349 1.932434 0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.0599655 1.056703	0.6	0.477	6.20053548	5.659947597	1.723689	1.573411
0.75 0.411 5.343459494 7.621242154 1.48543 2.118632 0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432	0.65	0.452	5.878336719	6.297408779	1.634121	1.750619
0.8 0.394 5.118429265 8.306104532 1.422874 2.309017 0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.61111111 16.68741633 1.003854	0.7	0.430	5.594973113	6.951440285	1.555349	1.932434
0.85 0.378 4.915685394 9.005392453 1.366513 2.503413 0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.61111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808	0.75	0.411	5.343459494	7.621242154	1.48543	2.118632
0.9 0.364 4.731894184 9.718533939 1.315421 2.701659 0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.8012306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.61111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.43113684 18.35557863 0.957153	0.8	0.394	5.118429265	8.306104532	1.422874	2.309017
0.95 0.351 4.564371241 10.44501056 1.268851 2.903613 1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763	0.85	0.378	4.915685394	9.005392453	1.366513	2.503413
1 0.339 4.410928627 11.18434984 1.226196 3.109142 1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529	0.9	0.364	4.731894184	9.718533939	1.315421	2.701659
1.05 0.328 4.269763606 11.93611905 1.186953 3.318126 1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355	0.95	0.351	4.564371241	10.44501056	1.268851	2.903613
1.1 0.318 4.139376284 12.69992014 1.150707 3.530456 1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154	1	0.339	4.410928627	11.18434984	1.226196	3.109142
1.15 0.309 4.018507689 13.47538546 1.117107 3.746028 1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.234 3.037418717 23.58638996 0.844373	1.05	0.328	4.269763606	11.93611905	1.186953	3.318126
1.2 0.300 3.906092586 14.26217424 1.085856 3.964747 1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097<	1.1	0.318	4.139376284	12.69992014	1.150707	3.530456
1.25 0.292 3.80122306 15.05996955 1.056703 4.186527 1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663	1.15	0.309	4.018507689	13.47538546	1.117107	3.746028
1.3 0.285 3.703120086 15.86847576 1.029432 4.411284 1.35 0.278 3.611111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.9 0.221 2.875373703 26.31977735 0.799326	1.2	0.300	3.906092586	14.26217424	1.085856	3.964747
1.35 0.278 3.61111111 16.68741633 1.003854 4.638941 1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326	1.25	0.292	3.80122306	15.05996955	1.056703	4.186527
1.4 0.271 3.524612199 17.51653189 0.979808 4.869428 1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 </th <th>1.3</th> <th>0.285</th> <th>3.703120086</th> <th>15.86847576</th> <th>1.029432</th> <th>4.411284</th>	1.3	0.285	3.703120086	15.86847576	1.029432	4.411284
1.45 0.265 3.443113684 18.35557863 0.957153 5.102675 1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455	1.35	0.278	3.611111111	16.68741633	1.003854	4.638941
1.5 0.259 3.366168548 19.20432683 0.935763 5.338618 1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.4	0.271	3.524612199	17.51653189	0.979808	4.869428
1.55 0.253 3.293382942 20.06255963 0.915529 5.577199 1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.45	0.265	3.443113684	18.35557863	0.957153	5.102675
1.6 0.248 3.224408387 20.93007188 0.896355 5.818359 1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.5	0.259	3.366168548	19.20432683	0.935763	5.338618
1.65 0.243 3.158935325 21.80666919 0.878154 6.062045 1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.55	0.253	3.293382942	20.06255963	0.915529	5.577199
1.7 0.238 3.096687751 22.69216703 0.860849 6.308204 1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.6	0.248	3.224408387	20.93007188	0.896355	5.818359
1.75 0.234 3.037418717 23.58638996 0.844373 6.55679 1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.65	0.243	3.158935325	21.80666919	0.878154	6.062045
1.8 0.229 2.980906544 24.48917097 0.828663 6.807754 1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.7	0.238	3.096687751	22.69216703	0.860849	6.308204
1.85 0.225 2.926951626 25.40035078 0.813664 7.061054 1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.75	0.234	3.037418717	23.58638996	0.844373	6.55679
1.9 0.221 2.875373703 26.31977735 0.799326 7.316645 1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.8	0.229	2.980906544	24.48917097	0.828663	6.807754
1.95 0.217 2.826009536 27.24730532 0.785604 7.574489 2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.85	0.225	2.926951626	25.40035078	0.813664	7.061054
2 0.214 2.778710913 28.18279558 0.772455 7.834546 2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.9	0.221	2.875373703	26.31977735	0.799326	7.316645
2.05 0.210 2.733342934 29.12611486 0.759843 8.09678	1.95	0.217	2.826009536	27.24730532	0.785604	7.574489
	2	0.214	2.778710913	28.18279558	0.772455	7.834546
2.1 0.207 2.689782523 30.07713529 0.747734 8.361155	2.05	0.210	2.733342934	29.12611486	0.759843	8.09678
	2.1	0.207	2.689782523	30.07713529	0.747734	8.361155

2.15	0.204	2.647917139	31.03573414	0.736096	8.627636
2.2	0.201	2.607643657	32.00179343	0.7249	8.896191
2.25	0.198	2.568867387	32.97519966	0.71412	9.166789
2.3	0.195	2.531501213	33.95584359	0.703733	9.439398
2.35	0.192	2.495464843	34.94361991	0.693715	9.713991
2.4	0.189	2.460684136	35.93842708	0.684047	9.990538
2.45	0.187	2.427090522	36.94016709	0.674708	10.26901
2.5	0.184	2.394620474	37.94874529	0.665681	10.54939
2.55	0.182	2.363215049	38.96407019	0.656951	10.83164
2.6	0.179	2.332819473	39.98605328	0.648501	11.11574
2.65	0.177	2.303382774	41.01460893	0.640318	11.40167
2.7	0.175	2.274857451	42.04965419	0.632389	11.6894
2.75	0.173	2.247199181	43.09110869	0.6247	11.97891
2.8	0.171	2.220366551	44.13889449	0.617241	12.27019
2.85	0.169	2.19432082	45.19293598	0.61	12.5632
2.9	0.167	2.169025704	46.25315979	0.602968	12.85793
2.95	0.165	2.144447178	47.31949463	0.596136	13.15436
3	0.163	2.120553306	48.39187125	0.589493	13.45248

b) Even the bi-linear equivalent capacity curve should be transformed to spectral parameters using:

$$Sag = \frac{V}{m*} \text{ or } \frac{F}{\Gamma \times m*}$$

VIASSESSMENT OF THE PERFORMANCE FOR THE (Y DIRECTION)

VI.1 SDOF TO MDOF

For the conversion of forces and displacements of a system, to have the **SDOF** from the **MDOF** capacity curve:

interpolation is made to determine the value of the displacement d0.6 associated with the force 0.6Fu.

Гх								
-	0,6*F _∪ =F _y	d (0,6*F _u)	dy to d* _Y	k*	m*	T*	du	Fu
1.74	[KN]	[m]	[m]	[KN/m]	[ton]	[sec]	[m]	[KN]
	744	0.0013	0.0021	572196.5	503	0.186	0.0105	1239.8

Table 11 The bi-linear equivalent capacity curve domain for Y direction

Bi-linear		
d _i [m]	F _i [KN]	Note
0	0	0
0.0013	744	Correspond to F (0.6 Fu), d (0.6 Fu)
0.002100	1201.6	Correspond to Fy, dy
0.0105 1201.6		horizontal plateau, Fy, du

Table 12. transformation of the capacity curve from MDOF to SDOF

	MDOF	SDOF		
Step	Displacement	BaseForce	D*=Δ/Γx	F*=V/Γx
	m	KN	m	KN
0	0	0	0.000000	0
1	0.00081	473	0.000488	284.9398
2	0.00162	947	0.000976	570.4819
3	0.00243	1399	0.001464	842.7711
4	0.00324	1825	0.001952	1099.398
5	0.00431	1950	0.002596	1174.699
6	0.00542	1995	0.003265	1201.807
7	0.00651	2036	0.003922	1226.506
8	0.00748	2050	0.004506	1234.94
9	0.00839	2057	0.005054	1239.157
10	0.00928	2058	0.005590	1239.759
11	0.01016	2055	0.006120	1237.952
12	0.01103	2052	0.006645	1236.145
13	0.01189	2048	0.007163	1233.735
14	0.01399	1826	0.008428	1100
15	0.01708	1506	0.010289	907.2289

VI.2 THE BI-LINEAR EQUIVALENT CAPACITY CURVE THE SHEAR FORCES OF THE BI LINEAR TO SAG

Table 13. bi-linear capacity curve (Sd,Sag)

	BILINEARE SDOF					
	S [cm]	S [cm] V [KN] Sag [ms ⁻²]				
Δ_0	0	0	0.00			
Δ0,6	0.13	744	1.48			
Δ_{y}	0.21	1202	2.39			
Δ_{u}	1.1	1202	2.39			

VI.3 THE SPECTRE OR THE DEMAND CURVE SHOULD BE TRANSFORMED ALSO TO THE (ADRS) FORM AS FOLLOW:

q*	Sae(T*)	Sde (T*) =demax [cm]	Тс	d*max [cm] Performance	u	Ru
				point		
2.6	6.1	0.6	0.4	1	4.362	2.5643

Table 14. transformation of the demand curve to (ADRS) form.

T [sec]	Sae [g]	Sae [ms-2]	S _{de} [cm]	sae/Ru	sde/Ru
0	0.250	2.4525	0	0.956412	0
0.05	0.375	3.67875	0.023319595	1.434619	0.009094
0.1	0.500	4.905	0.124371171	1.912825	0.048502
0.15	0.625	6.13125	0.349793919	2.391031	0.136411
0.2	0.625	6.13125	0.621855856	2.391031	0.242508
0.25	0.625	6.13125	0.971649775	2.391031	0.378919
0.3	0.625	6.13125	1.399175676	2.391031	0.545643
0.35	0.625	6.13125	1.90443356	2.391031	0.74268
0.4	0.625	6.13125	2.487423425	2.391031	0.970032
0.45	0.578	5.668228418	2.91040269	2.210464	1.134983
0.5	0.539	5.283751077	3.349369572	2.060528	1.306169
0.55	0.505	4.958464702	3.803236369	1.933675	1.483165
0.6	0.477	4.679019466	4.271083533	1.824698	1.665614
0.65	0.452	4.435883324	4.752121548	1.729881	1.853206
0.7	0.430	4.222052788	5.245663785	1.646493	2.045675

0.75 0.411 4.032256742 5.751106579 1.572477 2.242785 0.8 0.394 3.862445469 6.267914266 1.506255 2.444327 0.85 0.378 3.709451824 6.795607689 1.446591 2.650113 0.9 0.364 3.57076015 7.333755226 1.392505 2.859977 0.95 0.351 3.44434476 7.8819656622 1.343207 3.073765 1 0.339 3.222029306 9.007179069 1.256509 3.51257 1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.3644871 1.118627 4.431859 1.3 0.285 2.79431338 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268						
0.85 0.378 3.709451824 6.795607689 1.446591 2.650113 0.9 0.364 3.57076015 7.333755226 1.392505 2.859977 0.95 0.351 3.44434476 7.881965662 1.343207 3.073765 1 0.339 3.328554602 8.439882456 1.298051 3.291339 1.05 0.328 3.222029306 9.007179069 1.256509 3.51257 1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.6559726591 13.21824445 1.037225 <t< th=""><th>0.75</th><th>0.411</th><th>4.032256742</th><th>5.751106579</th><th>1.572477</th><th>2.242785</th></t<>	0.75	0.411	4.032256742	5.751106579	1.572477	2.242785
0.9 0.364 3.57076015 7.333755226 1.392505 2.859977 0.95 0.351 3.44434476 7.881965662 1.343207 3.073765 1 0.339 3.328554602 8.439882456 1.298051 3.291339 1.05 0.328 3.222029306 9.007179069 1.256509 3.51257 1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.9749594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242	0.8	0.394	3.862445469	6.267914266	1.506255	2.444327
0.95 0.351 3.4443476 7.881965662 1.343207 3.073765 1 0.339 3.328554602 8.439882456 1.298051 3.291339 1.05 0.328 3.222029306 9.007179069 1.256509 3.51257 1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 <th< th=""><th>0.85</th><th>0.378</th><th>3.709451824</th><th>6.795607689</th><th>1.446591</th><th>2.650113</th></th<>	0.85	0.378	3.709451824	6.795607689	1.446591	2.650113
1 0.339 3.328554602 8.439882456 1.298051 3.291339 1.05 0.328 3.222029306 9.007179069 1.256509 3.51257 1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118677 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.4918048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 <t< th=""><th>0.9</th><th>0.364</th><th>3.57076015</th><th>7.333755226</th><th>1.392505</th><th>2.859977</th></t<>	0.9	0.364	3.57076015	7.333755226	1.392505	2.859977
1.05 0.328 3.222029306 9.007179069 1.256509 3.51257 1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.94881	0.95	0.351	3.44434476	7.881965662	1.343207	3.073765
1.1 0.318 3.123637027 9.583555119 1.218139 3.737342 1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.94881 6.159317 1.65 0.243 2.338781195 16.45564806 0.929614	1	0.339	3.328554602	8.439882456	1.298051	3.291339
1.15 0.309 3.032427725 10.16873318 1.182569 3.965546 1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.3380808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854	1.05	0.328	3.222029306	9.007179069	1.256509	3.51257
1.2 0.300 2.947597559 10.7624561 1.149488 4.197083 1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.3380808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223	1.1	0.318	3.123637027	9.583555119	1.218139	3.737342
1.25 0.292 2.868461401 11.36448471 1.118627 4.431859 1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.338781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.861345	1.15	0.309	3.032427725	10.16873318	1.182569	3.965546
1.3 0.285 2.794431388 11.97459594 1.089757 4.669787 1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345	1.2	0.300	2.947597559	10.7624561	1.149488	4.197083
1.35 0.278 2.725 12.59258109 1.06268 4.910785 1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.217 2.132550273 20.56123578 0.83164	1.25	0.292	2.868461401	11.36448471	1.118627	4.431859
1.4 0.271 2.659726591 13.21824445 1.037225 5.154778 1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721	1.3	0.285	2.794431388	11.97459594	1.089757	4.669787
1.45 0.265 2.598226557 13.85140202 1.013242 5.401693 1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721	1.35	0.278	2.725	12.59258109	1.06268	4.910785
1.5 0.259 2.540162574 14.49188048 0.990599 5.651463 1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551	1.4	0.271	2.659726591	13.21824445	1.037225	5.154778
1.55 0.253 2.485237435 15.13951615 0.969179 5.904025 1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231	1.45	0.265	2.598226557	13.85140202	1.013242	5.401693
1.6 0.248 2.433188175 15.79415425 0.948881 6.159317 1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.80437 8.571254 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231	1.5	0.259	2.540162574	14.49188048	0.990599	5.651463
1.65 0.243 2.383781195 16.45564806 0.929614 6.417283 1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379	1.55	0.253	2.485237435	15.13951615	0.969179	5.904025
1.7 0.238 2.336808218 17.12385835 0.911296 6.677868 1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968	1.6	0.248	2.433188175	15.79415425	0.948881	6.159317
1.75 0.234 2.292082893 17.79865273 0.893854 6.94102 1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972	1.65	0.243	2.383781195	16.45564806	0.929614	6.417283
1.8 0.229 2.249437938 18.47990517 0.877223 7.206691 1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367	1.7	0.238	2.336808218	17.12385835	0.911296	6.677868
1.85 0.225 2.208722727 19.16749547 0.861345 7.474834 1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132	1.75	0.234	2.292082893	17.79865273	0.893854	6.94102
1.9 0.221 2.169801233 19.8613089 0.846167 7.745403 1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	1.8	0.229	2.249437938	18.47990517	0.877223	7.206691
1.95 0.217 2.132550273 20.56123578 0.83164 8.018357 2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	1.85	0.225	2.208722727	19.16749547	0.861345	7.474834
2 0.214 2.096858005 21.26717113 0.817721 8.293654 2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	1.9	0.221	2.169801233	19.8613089	0.846167	7.745403
2.05 0.210 2.06262263 21.97901437 0.80437 8.571254 2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	1.95	0.217	2.132550273	20.56123578	0.83164	8.018357
2.1 0.207 2.029751273 22.69666902 0.791551 8.851121 2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2	0.214	2.096858005	21.26717113	0.817721	8.293654
2.15 0.204 1.99815901 23.42004246 0.779231 9.133219 2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.05	0.210	2.06262263	21.97901437	0.80437	8.571254
2.2 0.201 1.967768021 24.14904566 0.767379 9.417511 2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.1	0.207	2.029751273	22.69666902	0.791551	8.851121
2.25 0.198 1.938506851 24.88359298 0.755968 9.703966 2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.15	0.204	1.99815901	23.42004246	0.779231	9.133219
2.3 0.195 1.910309762 25.62360197 0.744972 9.992551 2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.2	0.201	1.967768021	24.14904566	0.767379	9.417511
2.35 0.192 1.883116162 26.36899318 0.734367 10.28323 2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.25	0.198	1.938506851	24.88359298	0.755968	9.703966
2.4 0.189 1.856870106 27.11968997 0.724132 10.57599 2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.3	0.195	1.910309762	25.62360197	0.744972	9.992551
2.45 0.187 1.831519848 27.8756184 0.714246 10.87078	2.35	0.192	1.883116162	26.36899318	0.734367	10.28323
	2.4	0.189	1.856870106	27.11968997	0.724132	10.57599
2.5 0.184 1.80701745 28.63670702 0.704691 11.16758	2.45	0.187	1.831519848	27.8756184	0.714246	10.87078
	2.5	0.184	1.80701745	28.63670702	0.704691	11.16758

2.55	0.182	1.783318433	29.40288681	0.695449	11.46638
2.6	0.179	1.760381464	30.17409098	0.686504	11.76713
2.65	0.177	1.738168078	30.95025489	0.677841	12.06981
2.7	0.175	1.71664243	31.73131597	0.669447	12.3744
2.75	0.173	1.695771075	32.51721356	0.661307	12.68088
2.8	0.171	1.675522759	33.30788884	0.653411	12.98923
2.85	0.169	1.65586825	34.10328477	0.645746	13.29941
2.9	0.167	1.636780166	34.90334596	0.638302	13.61141
2.95	0.165	1.618232832	35.70801864	0.631069	13.92522
3	0.163	1.600202148	36.51725053	0.624038	14.2408

c) Even the bi-linear equivalent capacity curve should be transformed to spectral parameters using:

$$Sag = \frac{V}{m*} \text{ or } \frac{F}{\Gamma \times m*}$$

APPENDIX III

I DOMAIN COORDINATES FROM MODEL WALL, SEISMIC ANALYSIS X DIRECTION WALL 10

I.1 BENDING DOMAIN

Table 1 bending domain for wall 10 after reinforcement for X direction

N [N]	V [N]
0.00E+00	0.00E+00
5.09E+04	1.57E+04
1.02E+05	3.12E+04
1.53E+05	4.63E+04
2.03E+05	6.11E+04
2.54E+05	7.55E+04
3.05E+05	8.97E+04
3.56E+05	1.03E+05
4.07E+05	1.17E+05
4.58E+05	1.30E+05
5.09E+05	1.43E+05
5.60E+05	1.56E+05
6.10E+05	1.68E+05
6.61E+05	1.80E+05
7.12E+05	1.91E+05
7.63E+05	2.02E+05
8.14E+05	2.13E+05
8.65E+05	2.24E+05
9.16E+05	2.34E+05
9.67E+05	2.44E+05
1.02E+06	2.54E+05
1.07E+06	2.63E+05
1.12E+06	2.72E+05
1.17E+06	2.81E+05
1.22E+06	2.89E+05
1.27E+06	2.97E+05
1.32E+06	3.05E+05
1.37E+06	3.12E+05
1.42E+06	3.19E+05
1.48E+06	3.26E+05
1.53E+06	3.33E+05
1.58E+06	3.39E+05
1.63E+06	3.45E+05
1.68E+06	3.50E+05
1.73E+06	3.55E+05

1.78E+06	3.60E+05
1.83E+06	3.64E+05
1.88E+06	3.69E+05
1.93E+06	3.73E+05
1.98E+06	3.76E+05
2.03E+06	3.79E+05
2.09E+06	3.82E+05
2.14E+06	3.85E+05
2.19E+06	3.87E+05
2.24E+06	3.89E+05
2.29E+06	3.91E+05
2.34E+06	3.92E+05
2.39E+06	3.93E+05
2.44E+06	3.93E+05
2.49E+06	3.94E+05
2.54E+06	3.94E+05
2.59E+06	3.93E+05
2.65E+06	3.93E+05
2.70E+06	3.92E+05
2.75E+06	3.91E+05
2.80E+06	3.89E+05
2.85E+06	3.87E+05
2.90E+06	3.85E+05
2.95E+06	3.82E+05
3.00E+06	3.79E+05
3.05E+06	3.76E+05
3.10E+06	3.73E+05
3.15E+06	3.69E+05
3.20E+06	3.64E+05
3.26E+06	3.60E+05
3.31E+06	3.55E+05
3.36E+06	3.50E+05
3.41E+06	3.45E+05
3.46E+06	3.39E+05
3.51E+06	3.33E+05
3.56E+06	3.26E+05
3.61E+06	3.19E+05
3.66E+06	3.12E+05
3.71E+06	3.05E+05
3.76E+06	2.97E+05
3.82E+06	2.89E+05
3.87E+06	2.81E+05
3.92E+06	2.72E+05
3.97E+06	2.72E+03 2.63E+05
4.02E+06	2.63E+03 2.54E+05
4.07E+06	2.34E+03 2.44E+05
4.12E+06	2.34E+05
4.17E+06	2.24E+05

4.22E+06	2.13E+05
4.27E+06	2.02E+05
4.32E+06	1.91E+05
4.37E+06	1.80E+05
4.43E+06	1.68E+05
4.48E+06	1.56E+05
4.53E+06	1.43E+05
4.58E+06	1.30E+05
4.63E+06	1.17E+05
4.68E+06	1.03E+05
4.73E+06	8.97E+04
4.78E+06	7.55E+04
4.83E+06	6.11E+04
4.88E+06	4.63E+04
4.93E+06	3.12E+04
4.99E+06	1.57E+04
5.04E+06	0.00E+00

I.2 SHEAR DOMAIN

Table 2 shear domain for wall 10 after reinforcement for X direction

N [N]	V [N]
0.00E+00	3.28E+05
5.09E+04	3.52E+05
1.02E+05	3.73E+05
1.53E+05	3.91E+05
2.03E+05	4.09E+05
2.54E+05	4.25E+05
3.05E+05	4.40E+05
3.56E+05	4.55E+05
4.07E+05	4.68E+05
4.58E+05	4.81E+05
5.09E+05	4.94E+05
5.60E+05	5.06E+05
6.10E+05	5.18E+05
6.61E+05	5.29E+05
7.12E+05	5.40E+05
7.63E+05	5.51E+05
8.14E+05	5.61E+05
8.65E+05	5.71E+05
9.16E+05	5.81E+05
9.67E+05	5.90E+05
1.02E+06	6.00E+05
1.07E+06	6.09E+05
1.12E+06	6.18E+05

1.17E+06	6.27E+05
1.22E+06	6.35E+05
1.27E+06	6.44E+05
1.32E+06	6.52E+05
1.37E+06	6.60E+05
1.42E+06	6.68E+05
1.48E+06	6.76E+05
1.53E+06	6.84E+05
1.58E+06	6.92E+05
1.63E+06	6.99E+05
1.68E+06	7.07E+05
1.73E+06	7.14E+05
1.78E+06	7.21E+05
1.83E+06	7.28E+05
1.88E+06	7.36E+05
1.93E+06	7.43E+05
1.98E+06	7.49E+05
2.03E+06	7.56E+05
2.09E+06	7.63E+05
2.14E+06	7.70E+05
2.19E+06	7.76E+05
2.24E+06	7.83E+05
2.29E+06	7.89E+05
2.34E+06	7.96E+05
2.39E+06	8.02E+05
2.44E+06	8.08E+05
2.49E+06	8.14E+05
2.54E+06	8.20E+05
2.59E+06	8.27E+05
2.65E+06	8.33E+05
2.70E+06	
	8.39E+05
2.75E+06	8.44E+05
2.80E+06	8.50E+05
2.85E+06	8.56E+05
2.90E+06	8.62E+05
2.95E+06	8.68E+05
3.00E+06	8.73E+05
3.05E+06	8.79E+05
3.10E+06	8.84E+05
3.15E+06	8.90E+05
3.20E+06	8.96E+05
3.26E+06	9.01E+05
3.31E+06	9.06E+05
3.36E+06	9.12E+05
3.41E+06	9.17E+05
3.46E+06	9.22E+05
3.51E+06	9.28E+05
3.56E+06	9.33E+05

3.61E+06	9.38E+05
3.66E+06	9.43E+05
3.71E+06	9.48E+05
3.76E+06	9.53E+05
3.82E+06	9.58E+05
3.87E+06	9.63E+05
3.92E+06	9.68E+05
3.97E+06	9.73E+05
4.02E+06	9.78E+05
4.07E+06	9.83E+05
4.12E+06	9.88E+05
4.17E+06	9.93E+05
4.22E+06	9.98E+05
4.27E+06	1.00E+06
4.32E+06	1.01E+06
4.37E+06	1.01E+06
4.43E+06	1.02E+06
4.48E+06	1.02E+06
4.53E+06	1.03E+06
4.58E+06	1.03E+06
4.63E+06	1.04E+06
4.68E+06	1.04E+06
4.73E+06	1.04E+06
4.78E+06	1.05E+06
4.83E+06	1.05E+06
4.88E+06	1.06E+06
4.93E+06	1.06E+06
4.99E+06	1.07E+06
5.04E+06	1.07E+06

II.1 BENDING DOMAIN

Table 3 bending domain for wall 7 after reinforcement for X direction

N [N]	V [N]
0.00E+00	0.00E+00
1.42E+04	5.13E+03
2.83E+04	1.02E+04
4.25E+04	1.51E+04
5.66E+04	1.99E+04
7.08E+04	2.46E+04
8.49E+04	2.92E+04

9.91E+04	3.37E+04
1.13E+05	3.81E+04
1.27E+05	4.24E+04
1.42E+05	4.66E+04
1.56E+05	5.07E+04
1.70E+05	5.46E+04
1.84E+05	5.85E+04
1.98E+05	6.23E+04
2.12E+05	6.59E+04
2.27E+05	6.95E+04
2.41E+05	7.30E+04
2.55E+05	7.63E+04
2.69E+05	7.96E+04
2.83E+05	8.27E+04
2.97E+05	8.57E+04
3.11E+05	8.87E+04
3.26E+05	9.15E+04
3.40E+05	9.42E+04
3.54E+05	9.68E+04
3.68E+05	9.93E+04
3.82E+05	1.02E+05
3.96E+05	1.04E+05
4.11E+05	1.06E+05
4.25E+05	1.08E+05
4.39E+05	1.10E+05
4.53E+05	1.12E+05
4.67E+05	1.14E+05
4.81E+05	1.16E+05
4.96E+05	1.17E+05
5.10E+05	1.19E+05
5.24E+05	1.20E+05
5.38E+05	1.21E+05
5.52E+05	1.22E+05
5.66E+05	1.24E+05
5.80E+05	1.24E+05
5.95E+05	1.25E+05
6.09E+05	1.26E+05
6.23E+05	1.27E+05
6.37E+05	1.27E+05
6.51E+05	1.28E+05
6.65E+05	1.28E+05
6.80E+05	1.28E+05
6.94E+05	1.28E+05
7.08E+05	1.28E+05
7.22E+05	1.28E+05
7.36E+05	1.28E+05
7.50E+05	1.28E+05
7.50E+05 7.65E+05	1.26E+05 1.27E+05
1.03L103	1.271.100

7.700.05	1 275 - 05
7.79E+05	1.27E+05
7.93E+05	1.26E+05
8.07E+05	1.25E+05
8.21E+05	1.24E+05
8.35E+05	1.24E+05
8.49E+05	1.22E+05
8.64E+05	1.21E+05
8.78E+05	1.20E+05
8.92E+05	1.19E+05
9.06E+05	1.17E+05
9.20E+05	1.16E+05
9.34E+05	1.14E+05
9.49E+05	1.12E+05
9.63E+05	1.10E+05
9.77E+05	1.08E+05
9.91E+05	1.06E+05
1.01E+06	1.04E+05
1.02E+06	1.02E+05
1.03E+06	9.93E+04
1.05E+06	9.68E+04
1.06E+06	9.42E+04
1.08E+06	9.15E+04
1.09E+06	8.87E+04
1.10E+06	8.57E+04
1.12E+06	8.27E+04
1.13E+06	7.96E+04
1.15E+06	7.63E+04
1.16E+06	7.30E+04
1.18E+06	6.95E+04
1.19E+06	6.59E+04
1.20E+06	6.23E+04
1.22E+06	5.85E+04
1.23E+06	5.46E+04
1.25E+06	5.07E+04
1.26E+06	4.66E+04
1.27E+06	4.24E+04
1.29E+06	3.81E+04
1.30E+06	3.37E+04
1.32E+06	2.92E+04
1.33E+06	2.46E+04
1.34E+06	1.99E+04
1.36E+06	1.51E+04
1.37E+06	1.02E+04
1.37E+00 1.39E+06	5.13E+03
1.40E+06	0.00E+00
1.₹0₽₹00	0.00ET00

II.2 SHEAR DOMAIN

Table 4 shear domain for wall 7 after reinforcement for X direction

N [N]	V [N]
0.00E+00	1.12E+05
1.42E+04	1.16E+05
2.83E+04	1.20E+05
4.25E+04	1.24E+05
5.66E+04	1.27E+05
7.08E+04	1.30E+05
8.49E+04	1.33E+05
9.91E+04	1.35E+05
1.13E+05	1.38E+05
1.27E+05	1.40E+05
1.42E+05	1.43E+05
1.56E+05	1.45E+05
1.70E+05	1.47E+05
1.84E+05	1.49E+05
1.98E+05	1.51E+05
2.12E+05	1.53E+05
2.27E+05	1.55E+05
2.41E+05	1.57E+05
2.55E+05	1.59E+05
2.69E+05	1.61E+05
2.83E+05	1.63E+05
2.97E+05	1.64E+05
3.11E+05	1.66E+05
3.26E+05	1.68E+05
3.40E+05	1.69E+05
3.54E+05	1.71E+05
3.68E+05	1.72E+05
3.82E+05	1.74E+05
3.96E+05	1.76E+05
4.11E+05	1.77E+05
4.25E+05	1.78E+05
4.39E+05	1.80E+05
4.53E+05	1.81E+05
4.67E+05	1.83E+05
4.81E+05	1.84E+05
4.96E+05	1.85E+05
5.10E+05	1.87E+05
5.24E+05	1.88E+05
5.38E+05	1.89E+05
5.52E+05	1.91E+05
5.66E+05	1.92E+05
5.80E+05	1.93E+05
5.95E+05	1.95E+05
6.09E+05	1.96E+05

6 22E+05	1.07E+05
6.23E+05 6.37E+05	1.97E+05 1.98E+05
6.3/E+05 6.51E+05	
	1.99E+05
6.65E+05	2.01E+05
6.80E+05	2.02E+05
6.94E+05	2.03E+05
7.08E+05	2.04E+05
7.22E+05	2.05E+05
7.36E+05	2.06E+05
7.50E+05	2.07E+05
7.65E+05	2.09E+05
7.79E+05	2.10E+05
7.93E+05	2.11E+05
8.07E+05	2.12E+05
8.21E+05	2.13E+05
8.35E+05	2.14E+05
8.49E+05	2.15E+05
8.64E+05	2.16E+05
8.78E+05	2.17E+05
8.92E+05	2.18E+05
9.06E+05	2.19E+05
9.20E+05	2.20E+05
9.34E+05	2.21E+05
9.49E+05	2.22E+05
9.63E+05	2.23E+05
9.77E+05	2.24E+05
9.91E+05	2.25E+05
1.01E+06	2.26E+05
1.02E+06	2.27E+05
1.03E+06	2.28E+05
1.05E+06	2.29E+05
1.06E+06	2.30E+05
1.08E+06	2.31E+05
1.09E+06	2.32E+05
1.10E+06	2.33E+05
1.12E+06	2.34E+05
1.13E+06	2.35E+05
1.15E+06	2.36E+05
1.16E+06	2.36E+05
1.18E+06	2.37E+05
1.19E+06	2.38E+05
1.20E+06	2.39E+05
1.22E+06	2.40E+05
1.23E+06	2.41E+05
1.25E+06	2.42E+05
1.25E+06 1.26E+06	2.43E+05
1.20E+00 1.27E+06	2.44E+05
1.2/E+06 1.29E+06	2.44E+05
1.27E+00	2. 44 D+UJ

1.30E+06	2.45E+05
1.32E+06	2.46E+05
1.33E+06	2.47E+05
1.34E+06	2.48E+05
1.36E+06	2.49E+05
1.37E+06	2.49E+05
1.39E+06	2.50E+05
1.40E+06	2.51E+05

IIIDOMAIN COORDINATES FROM MODEL WALL, SEISMIC ANALYSIS Y DIRECTION WALL 8

III.1 BENDING DOMAIN

Table 5 bending domain for wall 8 after reinforcement for Y direction

N [N]	V [N]			
0.00E+00	0.00E+00			
4.21E+03	1.78E+03			
8.43E+03	3.53E+03			
1.26E+04	5.24E+03			
1.69E+04	6.92E+03			
2.11E+04	8.56E+03			
2.53E+04	1.02E+04			
2.95E+04	1.17E+04			
3.37E+04	1.33E+04			
3.79E+04	1.47E+04			
4.21E+04	1.62E+04			
4.64E+04	1.76E+04			
5.06E+04	1.90E+04			
5.48E+04	2.04E+04			
5.90E+04	2.17E+04			
6.32E+04	2.29E+04			
6.74E+04	2.42E+04			
7.16E+04	2.54E+04			
7.59E+04	2.65E+04			
8.01E+04	2.77E+04			
8.43E+04	2.88E+04			
8.85E+04	2.98E+04			
9.27E+04	3.08E+04			
9.69E+04	3.18E+04			
1.01E+05	3.28E+04			
1.05E+05	3.37E+04			
1.10E+05	3.46E+04			
1.14E+05	3.54E+04			

1.18E+05 3.02E+04 1.22E+05 3.70E+04 1.26E+05 3.70E+04 1.26E+05 3.70E+04 1.31E+05 3.84E+04 1.35E+05 3.90E+04 1.39E+05 3.90E+04 1.39E+05 3.96E+04 1.39E+05 4.02E+04 1.48E+05 4.02E+04 1.48E+05 4.02E+04 1.52E+05 4.18E+05 4.02E+04 1.52E+05 4.18E+04 1.56E+05 4.18E+04 1.56E+05 4.18E+04 1.56E+05 4.22E+04 1.60E+05 4.22E+04 1.60E+05 4.22E+04 1.60E+05 4.23E+04 1.77E+05 4.30E+04 1.77E+05 4.36E+04 1.77E+05 4.36E+04 1.88E+05 4.38E+04 1.88E+05 4.38E+04 1.90E+05 4.42E+04 1.90E+05 4.42E+04 1.90E+05 4.42E+04 4.44E+04 1.90E+05 4.45E+04 4.46E+04 4.20E+05 4.46E+04 4.36E+04 4.20E+05 4.36E+04 4.20E+05 4.36E+04 4.20E+05 4.36E+04 4.20E+05 4.36E+04 4.20E+05 4.36E+04 4.20E+05 4.2		
1.26E+05 3.77E+04 1.31E+05 3.84E+04 1.35E+05 3.90E+04 1.39E+05 3.96E+04 1.48E+05 4.02E+04 1.48E+05 4.08E+04 1.52E+05 4.13E+04 1.56E+05 4.12E+04 1.56E+05 4.12E+04 1.60E+05 4.22E+04 1.60E+05 4.22E+04 1.60E+05 4.33E+04 1.73E+05 4.33E+04 1.77E+05 4.33E+04 1.81E+05 4.38E+04 1.81E+05 4.38E+04 1.81E+05 4.22E+04 1.90E+05 4.42E+04 1.90E+05 4.42E+04 1.90E+05 4.42E+04 1.90E+05 4.45E+04 2.02E+05 4.46E+04 2.07E+05 4.46E+04 2.11E+05 4.46E+04 2.28E+05 4.43E+04 2.28E+05 4.33E+04 2.28E+05 3.90E+04 3.38E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08	1.18E+05	3.62E+04
1.31E+05 3.84E+04 1.35E+05 3.90E+04 1.39E+05 3.90E+04 1.43E+05 4.02E+04 1.43E+05 4.08E+04 1.52E+05 4.13E+04 1.56E+05 4.13E+04 1.60E+05 4.22E+04 1.64E+05 4.26E+04 1.69E+05 4.30E+04 1.77E+05 4.33E+04 1.77E+05 4.38E+04 1.81E+05 4.42E+04 1.81E+05 4.38E+04 1.81E+05 4.42E+04 1.90E+05 4.46E+04 2.02E+05 4.46E+04 2.15E+05 4.46E+04 2.15E+05 4.46E+04 2.15E+05 4.46E+04 2.15E+05 4.46E+04 2.23E+05 4.45E+04 2.23E+05 4.45E+04 2.23E+05 4.45E+04 2.23E+05 4.45E+04 2.24E+05 4.45E+04 2.25E+05 4.45E+04 2.26E+05 4.38E+04 2.26E+05 4.26E+04 2.26	1.22E+05	3.70E+04
1.35E+05 3.90E+04 1.39E+05 3.96E+04 1.48E+05 4.02E+04 1.48E+05 4.08E+04 1.52E+05 4.18E+04 1.56E+05 4.18E+04 1.60E+05 4.22E+04 1.60E+05 4.20E+04 1.69E+05 4.30E+04 1.77E+05 4.38E+04 1.77E+05 4.38E+04 1.81E+05 4.38E+04 1.81E+05 4.38E+04 1.81E+05 4.38E+04 1.81E+05 4.41E+04 1.90E+05 4.42E+04 1.90E+05 4.42E+04 1.90E+05 4.45E+04 1.90E+05 4.45E+04 1.90E+05 4.45E+04 1.90E+05 4.46E+04 1.90E+05 4.46E+04 1.90E+05 4.46E+04 2.10E+05 4.46E+04 2.10E+05 4.46E+04 2.11E+05 4.46E+04 2.11E+05 4.48E+04 2.23E+05 4.46E+04 2.23E+05 4.46E+04 2.32E+05 4.43E+04 2.32E+05 4.43E+04 2.32E+05 4.43E+04 2.34E+05 4.38E+04 2.36E+05 4.36E+04 2.36E+05 3.96E+04 2.36E+05 3.46E+04 2.36E+05 3.46E+04 2.36E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08E+05 3.46E+04 3.08	1.26E+05	3.77E+04
1.39E+05	1.31E+05	3.84E+04
1.43E+05	1.35E+05	3.90E+04
1.48E+05	1.39E+05	3.96E+04
1.52E+05	1.43E+05	4.02E+04
1.56E+05	1.48E+05	4.08E+04
1.60E+05	1.52E+05	4.13E+04
1.64E+05	1.56E+05	4.18E+04
1.69E+05	1.60E+05	4.22E+04
1.73E+05	1.64E+05	4.26E+04
1.77E+05	1.69E+05	4.30E+04
1.81E+05	1.73E+05	4.33E+04
1.81E+05		
1.85E+05		
1.90E+05 4.42E+04 1.94E+05 4.44E+04 1.98E+05 4.45E+04 2.02E+05 4.46E+04 2.07E+05 4.46E+04 2.11E+05 4.46E+04 2.15E+05 4.46E+04 2.19E+05 4.45E+04 2.23E+05 4.44E+04 2.23E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.36E+04 2.53E+05 4.26E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.57E+05 4.22E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.78E+05 3.96E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.95E+05 3.62E+04 3.03E+05 3.54E+04 3.03E+05 3.46E+04		
1.94E+05		
1.98E+05 4.45E+04 2.02E+05 4.46E+04 2.07E+05 4.46E+04 2.11E+05 4.46E+04 2.15E+05 4.46E+04 2.19E+05 4.45E+04 2.23E+05 4.44E+04 2.28E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.38E+04 2.49E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.18E+04 2.70E+05 4.08E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.03E+05 3.54E+04		
2.02E+05		
2.07E+05		
2.11E+05 4.46E+04 2.15E+05 4.46E+04 2.19E+05 4.45E+04 2.23E+05 4.44E+04 2.28E+05 4.41E+04 2.36E+05 4.31E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.15E+05 2.19E+05 4.46E+04 2.19E+05 4.45E+04 2.23E+05 4.44E+04 2.28E+05 4.42E+04 2.32E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.45E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.18E+04 2.66E+05 4.18E+04 2.70E+05 4.26E+04 2.70E+05 4.28E+05 3.96E+04 2.78E+05 3.96E+04 2.87E+05 3.96E+04 2.87E+05 3.96E+04 2.87E+05 3.77E+04 2.99E+05 3.03E+04 3.03E+05 3.03E+05 3.03E+06		
2.19E+05 4.45E+04 2.23E+05 4.44E+04 2.28E+05 4.42E+04 2.32E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.74E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.03E+05 3.46E+04		
2.23E+05 4.44E+04 2.28E+05 4.42E+04 2.32E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.28E+05 4.42E+04 2.32E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 3.96E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.32E+05 4.41E+04 2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.36E+05 4.38E+04 2.40E+05 4.36E+04 2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.40E+05 4.36E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.03E+05 3.46E+04		
2.44E+05 4.33E+04 2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.49E+05 4.30E+04 2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.53E+05 4.26E+04 2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.57E+05 4.22E+04 2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.61E+05 4.18E+04 2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.66E+05 4.13E+04 2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.70E+05 4.08E+04 2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.74E+05 4.02E+04 2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.78E+05 3.96E+04 2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.82E+05 3.90E+04 2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.87E+05 3.84E+04 2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.91E+05 3.77E+04 2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.95E+05 3.70E+04 2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
2.99E+05 3.62E+04 3.03E+05 3.54E+04 3.08E+05 3.46E+04		
3.03E+05 3.54E+04 3.08E+05 3.46E+04		
3.08E+05 3.46E+04		
3 12F±05		
	3.12E+05	3.37E+04
3.16E+05 3.28E+04	3.16E+05	3.28E+04

	,
3.20E+05	3.18E+04
3.25E+05	3.08E+04
3.29E+05	2.98E+04
3.33E+05	2.88E+04
3.37E+05	2.77E+04
3.41E+05	2.65E+04
3.46E+05	2.54E+04
3.50E+05	2.42E+04
3.54E+05	2.29E+04
3.58E+05	2.17E+04
3.62E+05	2.04E+04
3.67E+05	1.90E+04
3.71E+05	1.76E+04
3.75E+05	1.62E+04
3.79E+05	1.47E+04
3.84E+05	1.33E+04
3.88E+05	1.17E+04
3.92E+05	1.02E+04
3.96E+05	8.56E+03
4.00E+05	6.92E+03
4.05E+05	5.24E+03
4.09E+05	3.53E+03
4.13E+05	1.78E+03
4.17E+05	0.00E+00

III.2 SHEAR DOMAIN

Table 6 shear domain for wall 8 after reinforcement for Y direction

N [N]	V [N]
0.00E+00	9.44E+03
4.21E+03	1.08E+04
8.43E+03	1.19E+04
1.26E+04	1.30E+04
1.69E+04	1.40E+04
2.11E+04	1.49E+04
2.53E+04	1.58E+04
2.95E+04	1.66E+04
3.37E+04	1.74E+04
3.79E+04	1.81E+04
4.21E+04	1.88E+04
4.64E+04	1.95E+04
5.06E+04	2.02E+04
5.48E+04	2.08E+04
5.90E+04	2.15E+04
6.32E+04	2.21E+04
6.74E+04	2.27E+04

5.44T-0.4	2.227.04
7.16E+04	2.32E+04
7.59E+04	2.38E+04
8.01E+04	2.44E+04
8.43E+04	2.49E+04
8.85E+04	2.54E+04
9.27E+04	2.59E+04
9.69E+04	2.64E+04
1.01E+05	2.69E+04
1.05E+05	2.74E+04
1.10E+05	2.79E+04
1.14E+05	2.84E+04
1.18E+05	2.88E+04
1.22E+05	2.93E+04
1.26E+05	2.97E+04
1.31E+05	3.02E+04
1.35E+05	3.06E+04
1.39E+05	3.11E+04
1.43E+05	3.15E+04
1.48E+05	3.19E+04
1.52E+05	3.23E+04
1.56E+05	3.27E+04
1.60E+05	3.31E+04
1.64E+05	3.35E+04
1.69E+05	3.39E+04
1.73E+05	3.43E+04
1.77E+05	3.47E+04
1.81E+05	3.51E+04
1.85E+05	3.54E+04
1.90E+05	3.58E+04
1.94E+05	3.62E+04
1.98E+05	3.65E+04
2.02E+05	3.69E+04
2.07E+05	3.73E+04
2.11E+05	3.76E+04
2.15E+05	3.80E+04
2.19E+05	3.83E+04
2.23E+05	3.87E+04
2.28E+05	3.90E+04
2.32E+05	3.93E+04
2.36E+05	3.97E+04
2.40E+05	4.00E+04
2.44E+05	4.03E+04
2.49E+05	4.07E+04
2.53E+05	4.10E+04
2.57E+05	4.13E+04
2.61E+05	4.16E+04
2.66E+05	4.20E+04
2.70E+05	4.23E+04

2.74E+05	4.26E+04
2.78E+05	4.29E+04
2.82E+05	4.32E+04
2.87E+05	4.35E+04
2.91E+05	4.38E+04
2.95E+05	4.41E+04
2.99E+05	4.44E+04
3.03E+05	4.47E+04
3.08E+05	4.50E+04
3.12E+05	4.53E+04
3.16E+05	4.56E+04
3.20E+05	4.59E+04
3.25E+05	4.62E+04
3.29E+05	4.65E+04
3.33E+05	4.67E+04
3.37E+05	4.70E+04
3.41E+05	4.73E+04
3.46E+05	4.76E+04
3.50E+05	4.79E+04
3.54E+05	4.81E+04
3.58E+05	4.84E+04
3.62E+05	4.87E+04
3.67E+05	4.90E+04
3.71E+05	4.92E+04
3.75E+05	4.95E+04
3.79E+05	4.98E+04
3.84E+05	5.00E+04
3.88E+05	5.03E+04
3.92E+05	5.06E+04
3.96E+05	5.08E+04
4.00E+05	5.11E+04
4.05E+05	5.13E+04
4.09E+05	5.16E+04
4.13E+05	5.18E+04
4.17E+05	5.21E+04

IV ASSESSMENT OF THE PERFORMANCE FOR THE (X DIRECTION)

IV.1 SDOF TO MDOF

For the conversion of forces and displacements of a system, the following equations are used to have the **SDOF** from the **MDOF** capacity curve:

$$d *= d/\Gamma$$

Γ: participation factor

$$\Gamma = \frac{m *}{\sum mi \ \phi^2} \quad \text{ in wich } \ m *= \sum mi \ \phi i$$

K: the rigidity

$$k = \frac{F(0.Fu)}{d(0.6Fu)}$$

T: the period

$$T *= 2\pi \sqrt{\left(\frac{m*}{k}\right)} \text{ or } 2\pi \sqrt{\left(\frac{m*d*}{F*}\right)}$$

interpolation is made to determine the value of the displacement d0.6 associated with the force 0.6Fu.

$\Gamma_{\mathbf{x}}$								
-	$0,6*F_U=F_y$	d (0,6*F _u)	dy to d* _Y	k *	m*	T*	du	Fu
1 27	[KN]	[m]	[m]	[KN/m]	[ton]	[sec]	[m]	[KN]
1.37	521.17	0.00110	0.001970	473789.0	180	0.122	0.224	868.6131387

Table 7. transformation of the capacity curve from MDOF to SDOF

	MDOF	SDO	OF	
	Displacement	BaseForce	D*=Δ/Γ x	$F*=V/\Gamma x$
Step	m	KN	m	KN
0	0	0.00E+00	0.000000	0
1	1.17E-03	7.00E+02	0.000854	510.9489
2	2.32E-03	8.50E+02	0.001693	620.438
3	3.39E-03	8.48E+02	0.002474	618.9781
4	4.46E-03	8.66E+02	0.003255	632.1168
5	5.56E-03	9.01E+02	0.004058	657.6642
6	6.68E-03	9.51E+02	0.004876	694.1606
7	7.86E-03	9.17E+02	0.005737	669.3431
8	9.05E-03	9.35E+02	0.006606	682.4818
9	1.03E-02	9.65E+02	0.007518	704.3796
10	1.15E-02	9.97E+02	0.008394	727.7372
11	1.26E-02	1.12E+03	0.009197	817.5182
12	1.37E-02	1.19E+03	0.010000	868.6131
13	1.48E-02	1.12E+03	0.010803	817.5182

14	1.59E-02	1.11E+03	0.011606	810.219
15	1.71E-02	1.13E+03	0.012482	824.8175
16	1.83E-02	1.14E+03	0.013358	832.1168
17	1.94E-02	1.16E+03	0.014161	846.7153
18	2.06E-02	1.17E+03	0.015036	854.0146
19	2.17E-02	1.17E+03	0.015839	854.0146
20	2.29E-02	1.18E+03	0.016715	861.3139
21	2.40E-02	1.18E+03	0.017518	861.3139
22	2.52E-02	1.18E+03	0.018394	861.3139
23	2.63E-02	1.19E+03	0.019197	868.6131
24	2.75E-02	1.19E+03	0.020073	868.6131
25	2.87E-02	1.19E+03	0.020949	868.6131
26	2.98E-02	1.19E+03	0.021752	868.6131
27	3.13E-02	1.19E+03	0.022847	868.6131
28	5.37E-02	1.07E+03	0.039197	781.0219
29	1.32E-01	1.01E+03	0.096350	737.2263
30	1.72E-01	9.99E+02	0.125547	729.1971
31	3.08E-01	9.96E+02	0.224818	727.0073
32	3.13E-01	8.09E+02	0.228467	590.5109

IV.2 THE BI-LINEAR EQUIVALENT CAPACITY CURVE

Table 8 BI-LINEAR EQUIVALENT CAPACITY CURVE domain X direction

]	Bi-linear		
d _i [m]	F _i [KN]	Note	
0	0	0	
0.00110	521.17	Correspond to F (0.6 Fu), d (0.6 Fu)	
0.001970	933.3642999	Correspond to Fy, dy	
0.0100	933.3642999	horizontal plateau, Fy, du	

IV.3 THE SPECTRE OR THE DEMAND CURVE SHOULD BE TRANSFORMED ALSO TO THE (ADRS) FORM AS FOLLOW:

				d*max [cm]		
q*	Sae(T*)	Sde (T*) =demax [cm]	Tc	Performance	u	Ru
				point		

1.4	7.5	0.25	0.4	0.4	2.4587	1.446

$$q *= \frac{Sag}{Sae(T *)}$$

 S_{ae} : the spectral acceleration correspond to (T^*)

 S_{ag} : max spectral acceleration of the structure

 q^* : the behaviour factor

$$\begin{cases} R_u = \frac{(u-1)T}{Tc} + 1 &, T > TC \\ R_u = u &, T \leq Tc \end{cases}$$

$$u = \begin{cases} 1 + \frac{(q-1)T}{TC} &, T \leq Tc \\ q &, T > TC \end{cases}$$

 μ : The ductility capacity for the building

R_u: strength reduction factor due to ductility

$$S_{a} = \frac{S_{ae}}{Ru}$$

$$S_{d} = \frac{u}{Ru} S_{de} = \frac{uT^{2}}{4\pi^{2}} Sa$$

Sa: spectral acceleration.

Sd: spectral displacement.

b) Table 9. transformation of the demand curve to (ADRS) form.

T [sec]	Sae [g]	S _{ae} [ms ⁻²]	S _{de} [cm]	sae/Ru	sde/Ru
0	0.250	3.25	0	2.246988	0
0.05	0.375	4.875	0.030902623	3.370482	0.021365
0.1	0.500	6.5	0.164813988	4.493976	0.113949
0.15	0.625	8.125	0.463539342	5.61747	0.320482
0.2	0.625	8.125	0.824069942	5.61747	0.569746
0.25	0.625	8.125	1.287609284	5.61747	0.890229
0.3	0.625	8.125	1.854157369	5.61747	1.281929
0.35	0.625	8.125	2.523714197	5.61747	1.744848
0.4	0.625	8.125	3.296279768	5.61747	2.278985
0.45	0.578	7.511413805	3.85680275	5.193249	2.66652
0.5	0.539	7.001912743	4.438512175	4.840989	3.068703
0.55	0.505	6.570850268	5.039966647	4.542961	3.484537
0.6	0.477	6.20053548	5.659947597	4.286932	3.91318

0.65	0.452	5.878336719	6.297408779	4.06417	4.353909
0.7	0.430	5.594973113	6.951440285	3.868258	4.806093
0.75	0.411	5.343459494	7.621242154	3.694366	5.269182
0.8	0.394	5.118429265	8.306104532	3.538785	5.742683
0.85	0.378	4.915685394	9.005392453	3.398611	6.226157
0.9	0.364	4.731894184	9.718533939	3.271542	6.719209
0.95	0.351	4.564371241	10.44501056	3.155719	7.221481
1	0.339	4.410928627	11.18434984	3.049632	7.732647
1.05	0.328	4.269763606	11.93611905	2.952033	8.252405
1.1	0.318	4.139376284	12.69992014	2.861886	8.780483
1.15	0.309	4.018507689	13.47538546	2.77832	9.316625
1.2	0.300	3.906092586	14.26217424	2.700598	9.860596
1.25	0.292	3.80122306	15.05996955	2.628093	10.41218
1.3	0.285	3.703120086	15.86847576	2.560267	10.97116
1.35	0.278	3.611111111	16.68741633	2.496653	11.53736
1.4	0.271	3.524612199	17.51653189	2.43685	12.1106
1.45	0.265	3.443113684	18.35557863	2.380503	12.6907
1.5	0.259	3.366168548	19.20432683	2.327305	13.27751
1.55	0.253	3.293382942	20.06255963	2.276982	13.87087
1.6	0.248	3.224408387	20.93007188	2.229295	14.47065
1.65	0.243	3.158935325	21.80666919	2.184028	15.07672
1.7	0.238	3.096687751	22.69216703	2.140991	15.68893
1.75	0.234	3.037418717	23.58638996	2.100013	16.30718
1.8	0.229	2.980906544	24.48917097	2.060942	16.93135
1.85	0.225	2.926951626	25.40035078	2.023639	17.56132
1.9	0.221	2.875373703	26.31977735	1.987979	18.19699
1.95	0.217	2.826009536	27.24730532	1.953849	18.83827
2	0.214	2.778710913	28.18279558	1.921148	19.48505
2.05	0.210	2.733342934	29.12611486	1.889781	20.13724
2.1	0.207	2.689782523	30.07713529	1.859664	20.79476
2.15	0.204	2.647917139	31.03573414	1.83072	21.45752
2.2	0.201	2.607643657	32.00179343	1.802875	22.12543
2.25	0.198	2.568867387	32.97519966	1.776066	22.79843
2.3	0.195	2.531501213	33.95584359	1.750232	23.47642
2.35	0.192	2.495464843	34.94361991	1.725317	24.15935
2.4	0.189	2.460684136	35.93842708	1.70127	24.84714

2.45	0.187	2.427090522	36.94016709	1.678044	25.53973
2.5	0.184	2.394620474	37.94874529	1.655595	26.23704
2.55	0.182	2.363215049	38.96407019	1.633882	26.93902
2.6	0.179	2.332819473	39.98605328	1.612867	27.6456
2.65	0.177	2.303382774	41.01460893	1.592515	28.35672
2.7	0.175	2.274857451	42.04965419	1.572793	29.07233
2.75	0.173	2.247199181	43.09110869	1.553671	29.79237
2.8	0.171	2.220366551	44.13889449	1.535119	30.51679
2.85	0.169	2.19432082	45.19293598	1.517112	31.24554
2.9	0.167	2.169025704	46.25315979	1.499623	31.97855
2.95	0.165	2.144447178	47.31949463	1.48263	32.7158
3	0.163	2.120553306	48.39187125	1.46611	33.45722

b) Even the bi-linear equivalent capacity curve should be transformed to spectral parameters using:

$$Sag = \frac{V}{m*} \text{ or } \frac{F}{\Gamma \times m*}$$

V ASSESSMENT OF THE PERFORMANCE FOR THE (Y DIRECTION)

V.1 SDOF TO MDOF

For the conversion of forces and displacements of a system, the following equations are used to have the **SDOF** from the **MDOF** capacity curve:

$$F *= F/\Gamma$$

$$d *= d/\Gamma$$

Γ: participation factor

$$\Gamma = \frac{m *}{\sum mi \, \phi^2} \quad \text{in wich} \quad m *= \sum mi \, \phi i$$

K: the rigidity

$$k = \frac{F(0.Fu)}{d(0.6Fu)}$$

T: the period

$$T *= 2\pi \sqrt{\left(\frac{m*}{k}\right)} \text{ or } 2\pi \sqrt{\left(\frac{m*d*}{F*}\right)}$$

interpolation is made to determine the value of the displacement d0.6 associated with the force 0.6Fu.

Гх									
-	0,6*F _U =	= F _y	d (0,6*F _u)	dy to d* _Y	k *	m*	T*	du	Fu
1.74	[KN]		[m]	[m]	[KN/m]	[ton]	[sec]	[m]	[KN]
1./4	1340.9	14	0.00185	0.002850	724832.2	248	0.116	0.005007	2234.899329

Table 10. transformation of the capacity curve from MDOF to SDOF

	MDOF	SDOF		
a,	Displacement	BaseForce	D* =Δ/Γx	F*=V/Γx
Step	m	KN	m	KN
0	0	0.00E+00	0.000000	0
1	9.52E-04	6.84E+02	0.000639	459.0604
2	1.90E-03	1.37E+03	0.001275	919.4631
3	2.86E-03	2.04E+03	0.001919	1369.128
4	3.81E-03	2.77E+03	0.002557	1859.06
5	4.65E-03	3.08E+03	0.003121	2067.114
6	5.58E-03	3.29E+03	0.003745	2208.054
7	6.52E-03	3.33E+03	0.004376	2234.899
8	7.46E-03	3.33E+03	0.005007	2234.899
9	8.40E-03	3.31E+03	0.005638	2221.477
10	9.33E-03	3.29E+03	0.006262	2208.054
11	1.03E-02	3.27E+03	0.006913	2194.631
12	1.12E-02	3.26E+03	0.007517	2187.919
13	1.21E-02	3.25E+03	0.008121	2181.208
14	1.30E-02	3.24E+03	0.008725	2174.497
15	1.40E-02	3.23E+03	0.009396	2167.785
16	1.49E-02	3.22E+03	0.010000	2161.074
17	1.58E-02	3.15E+03	0.010604	2114.094
18	1.67E-02	3.08E+03	0.011208	2067.114
19	1.75E-02	3.03E+03	0.011745	2033.557
20	1.83E-02	2.99E+03	0.012282	2006.711
21	1.92E-02	2.97E+03	0.012886	1993.289
22	2.00E-02	2.95E+03	0.013423	1979.866
23	2.08E-02	2.94E+03	0.013960	1973.154
24	2.16E-02	2.94E+03	0.014497	1973.154
25	2.24E-02	2.93E+03	0.015034	1966.443

26	2.32E-02	2.93E+03	0.015570	1966.443
27	2.40E-02	2.93E+03	0.016107	1966.443
28	2.48E-02	2.93E+03	0.016644	1966.443
29	2.56E-02	2.93E+03	0.017181	1966.443
30	2.64E-02	2.93E+03	0.017718	1966.443
31	2.72E-02	2.93E+03	0.018255	1966.443
32	2.80E-02	2.93E+03	0.018792	1966.443

V.2 THE BI-LINEAR EQUIVALENT CAPACITY CURVE

Table 11 BI-LINEAR EQUIVALENT CAPACITY CURVE domain Y direction

Bi-linear			
d _i [m]	Fi[KN]	Note	
0	0	0	
0.00185	1340.94	Correspond to F (0.6 Fu), d (0.6 Fu)	
0.002850	2065.771812	Correspond to Fy, dy	
0.0258	2065.771812	horizontal plateau, Fy, du	

V.3 THE SPECTRE OR THE DEMAND CURVE SHOULD BE TRANSFORMED ALSO TO THE (ADRS) FORM AS FOLLOW:

q*	Sae(T*)	Sde (T*) =demax [cm]	Тс	d*max [cm] Performance point	u	Ru
0.9	7.5	0.116	0.4	0.2	0.657	0.9

$$q *= \frac{Sag}{Sae(T *)}$$

 S_{ae} : the spectral acceleration correspond to (T^*)

 S_{ag} : max spectral acceleration of the structure

 q^* : the behaviour factor

$$\begin{cases} R_u = \frac{(u-1)T}{Tc} + 1 & , & T > TC \\ R_u = u & , & T \leq Tc \end{cases}$$

$$u = \begin{cases} 1 + \frac{(q-1)T}{TC} & , & T \leq Tc \\ q & , & T > TC \end{cases}$$

μ: The ductility capacity for the building

R_u: strength reduction factor due to ductility

$$S_{a} = \frac{S_{ae}}{Ru}$$

$$S_{d} = \frac{u}{Ru} S_{de} = \frac{uT^{2}}{4\pi^{2}} Sa$$

Sa: spectral acceleration.

Sd: spectral displacement.

c) Table 12. transformation of the demand curve to (ADRS) form.

T [sec]	Sae [g]	Sae [ms ⁻²]	S _{de} [cm]	sae/Ru	sde/Ru
0	0.250	3.25	0	3.609548	0
0.05	0.375	4.875	0.030902623	5.414321	0.034321
0.1	0.500	6.5	0.164813988	7.219095	0.183047
0.15	0.625	8.125	0.463539342	9.023869	0.514821
0.2	0.625	8.125	0.824069942	9.023869	0.915237
0.25	0.625	8.125	1.287609284	9.023869	1.430058
0.3	0.625	8.125	1.854157369	9.023869	2.059283
0.35	0.625	8.125	2.523714197	9.023869	2.802913
0.4	0.625	8.125	3.296279768	9.023869	3.660947
0.45	0.578	7.511413805	3.85680275	8.342402	4.283481
0.5	0.539	7.001912743	4.438512175	7.776534	4.929545
0.55	0.505	6.570850268	5.039966647	7.297783	5.597538
0.6	0.477	6.20053548	5.659947597	6.886501	6.286108
0.65	0.452	5.878336719	6.297408779	6.528657	6.994091
0.7	0.430	5.594973113	6.951440285	6.213945	7.720478
0.75	0.411	5.343459494	7.621242154	5.934606	8.46438
0.8	0.394	5.118429265	8.306104532	5.684681	9.225009
0.85	0.378	4.915685394	9.005392453	5.459508	10.00166
0.9	0.364	4.731894184	9.718533939	5.255384	10.7937
0.95	0.351	4.564371241	10.44501056	5.069328	11.60054
1	0.339	4.410928627	11.18434984	4.89891	12.42167
1.05	0.328	4.269763606	11.93611905	4.742128	13.25661
1.1	0.318	4.139376284	12.69992014	4.597316	14.10491

1.15 0.309 4.018507689 13.47538546 4.463075 14.96617 1.2 0.300 3.906092586 14.26217424 4.338224 15.84 1.25 0.292 3.80122306 15.05996555 4.221752 16.72605 1.3 0.285 3.703120086 15.86847576 4.112796 17.62401 1.35 0.278 3.611111111 16.68741633 4.010608 18.53355 1.4 0.271 3.524612199 17.51653189 3.91454 19.45439 1.45 0.265 3.443113684 18.35557863 3.824025 20.38626 1.5 0.259 3.366168548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.234 3.037418717 23.58638996 3.373448						
1.25 0.292 3.80122306 15.05996955 4.221752 16.72605 1.3 0.285 3.703120086 15.86847576 4.112796 17.62401 1.35 0.278 3.611111111 16.68741633 4.010608 18.53355 1.4 0.271 3.524612199 17.51653189 3.91454 19.45439 1.45 0.265 3.43113684 18.35557863 3.824025 20.38626 1.5 0.259 3.366168548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.22408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.37448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684	1.15	0.309	4.018507689	13.47538546	4.463075	14.96617
1.3 0.285 3.703120086 15.86847576 4.112796 17.62401 1.35 0.278 3.611111111 16.68741633 4.010608 18.53355 1.4 0.271 3.524612199 17.51653189 3.91454 19.45439 1.45 0.265 3.443113684 18.35557863 3.824025 20.38626 1.5 0.259 3.366188548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.59216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.255 2.926951626 25.40035078 3.25076	1.2	0.300	3.906092586	14.26217424	4.338224	15.84
1.35 0.278 3.611111111 16.68741633 4.010608 18.53355 1.4 0.271 3.524612199 17.51653189 3.91454 19.45439 1.45 0.265 3.443113684 18.35557863 3.824025 20.38626 1.5 0.259 3.366168548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.5863896 3.373448 26.1957 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.95 0.217 2.826009536 27.24730532 3.138651	1.25	0.292	3.80122306	15.05996955	4.221752	16.72605
1.4 0.271 3.524612199 17.51653189 3.91454 19.45439 1.45 0.265 3.443113684 18.35557863 3.824025 20.38626 1.5 0.259 3.366168548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.98090544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.87537303 26.3197735 3.193476 29.23153 1.95 0.217 2.826009536 27.2473032 3.138651	1.3	0.285	3.703120086	15.86847576	4.112796	17.62401
1.45 0.265 3.443113684 18.35557863 3.824025 20.38626 1.5 0.259 3.366168548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.7778710913 28.18279558 3.08612	1.35	0.278	3.611111111	16.68741633	4.010608	18.53355
1.5 0.259 3.366168548 19.20432683 3.738568 21.3289 1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733	1.4	0.271	3.524612199	17.51653189	3.91454	19.45439
1.55 0.253 3.293382942 20.06255963 3.65773 22.28208 1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353	1.45	0.265	3.443113684	18.35557863	3.824025	20.38626
1.6 0.248 3.224408387 20.93007188 3.581125 23.24557 1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856	1.5	0.259	3.366168548	19.20432683	3.738568	21.3289
1.65 0.243 3.158935325 21.80666919 3.508408 24.21914 1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.68978253 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127	1.55	0.253	3.293382942	20.06255963	3.65773	22.28208
1.7 0.238 3.096687751 22.69216703 3.439274 25.2026 1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.68978253 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061	1.6	0.248	3.224408387	20.93007188	3.581125	23.24557
1.75 0.234 3.037418717 23.58638996 3.373448 26.19575 1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561	1.65	0.243	3.158935325	21.80666919	3.508408	24.21914
1.8 0.229 2.980906544 24.48917097 3.310684 27.19841 1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538	1.7	0.238	3.096687751	22.69216703	3.439274	25.2026
1.85 0.225 2.926951626 25.40035078 3.25076 28.21039 1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291	1.75	0.234	3.037418717	23.58638996	3.373448	26.19575
1.9 0.221 2.875373703 26.31977735 3.193476 29.23153 1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956	1.8	0.229	2.980906544	24.48917097	3.310684	27.19841
1.95 0.217 2.826009536 27.24730532 3.138651 30.26167 2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537	1.85	0.225	2.926951626	25.40035078	3.25076	28.21039
2 0.214 2.778710913 28.18279558 3.08612 31.30066 2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658	1.9	0.221	2.875373703	26.31977735	3.193476	29.23153
2.05 0.210 2.733342934 29.12611486 3.035733 32.34834 2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899	1.95	0.217	2.826009536	27.24730532	3.138651	30.26167
2.1 0.207 2.689782523 30.07713529 2.987353 33.40457 2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.526525	2	0.214	2.778710913	28.18279558	3.08612	31.30066
2.15 0.204 2.647917139 31.03573414 2.940856 34.46922 2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525	2.05	0.210	2.733342934	29.12611486	3.035733	32.34834
2.2 0.201 2.607643657 32.00179343 2.896127 35.54215 2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807	2.1	0.207	2.689782523	30.07713529	2.987353	33.40457
2.25 0.198 2.568867387 32.97519966 2.853061 36.62325 2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006	2.15	0.204	2.647917139	31.03573414	2.940856	34.46922
2.3 0.195 2.531501213 33.95584359 2.811561 37.71238 2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079	2.2	0.201	2.607643657	32.00179343	2.896127	35.54215
2.35 0.192 2.495464843 34.94361991 2.771538 38.80943 2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.25	0.198	2.568867387	32.97519966	2.853061	36.62325
2.4 0.189 2.460684136 35.93842708 2.73291 39.9143 2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.3	0.195	2.531501213	33.95584359	2.811561	37.71238
2.45 0.187 2.427090522 36.94016709 2.6956 41.02686 2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.35	0.192	2.495464843	34.94361991	2.771538	38.80943
2.5 0.184 2.394620474 37.94874529 2.659537 42.14702 2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.4	0.189	2.460684136	35.93842708	2.73291	39.9143
2.55 0.182 2.363215049 38.96407019 2.624658 43.27467 2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.45	0.187	2.427090522	36.94016709	2.6956	41.02686
2.6 0.179 2.332819473 39.98605328 2.590899 44.40971 2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.5	0.184	2.394620474	37.94874529	2.659537	42.14702
2.65 0.177 2.303382774 41.01460893 2.558206 45.55206 2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.55	0.182	2.363215049	38.96407019	2.624658	43.27467
2.7 0.175 2.274857451 42.04965419 2.526525 46.70161 2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.6	0.179	2.332819473	39.98605328	2.590899	44.40971
2.75 0.173 2.247199181 43.09110869 2.495807 47.85828 2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.65	0.177	2.303382774	41.01460893	2.558206	45.55206
2.8 0.171 2.220366551 44.13889449 2.466006 49.02198 2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.7	0.175	2.274857451	42.04965419	2.526525	46.70161
2.85 0.169 2.19432082 45.19293598 2.437079 50.19263	2.75	0.173	2.247199181	43.09110869	2.495807	47.85828
	2.8	0.171	2.220366551	44.13889449	2.466006	49.02198
2.9 0.167 2.169025704 46.25315979 2.408985 51.37015	2.85	0.169	2.19432082	45.19293598	2.437079	50.19263
	2.9	0.167	2.169025704	46.25315979	2.408985	51.37015

2.95	0.165	2.144447178	47.31949463	2.381687	52.55445
3	0.163	2.120553306	48.39187125	2.35515	53.74546

c) Even the bi-linear equivalent capacity curve should be transformed to spectral parameters using:

$$Sag = \frac{V}{m*} \text{ or } \frac{F}{\Gamma \times m*}$$